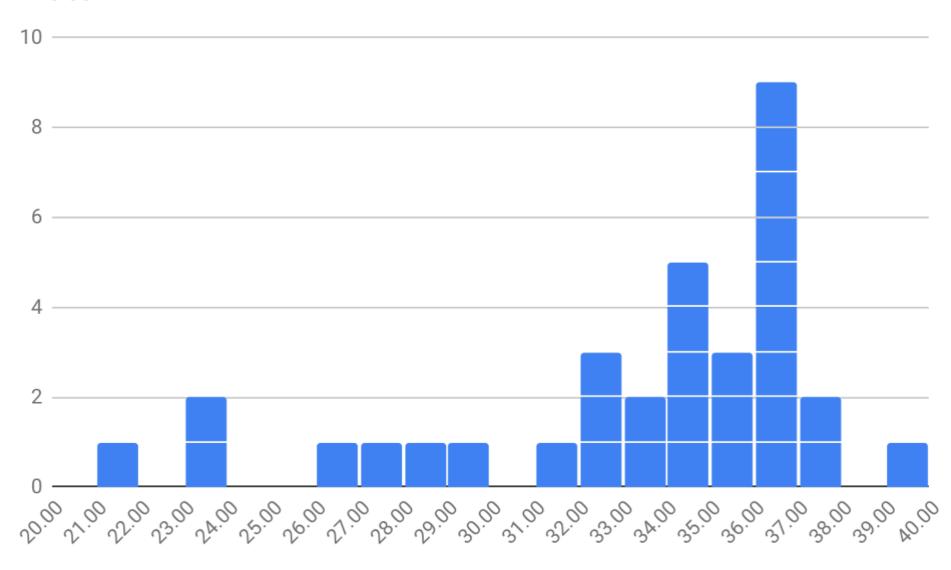
Generative Models

Instructor: Alan Ritter

Slides Adapted from Fei-Fei Li & Justin Johnson & Serena Yeung

Midterm



Overview

- Unsupervised Learning
- Generative Models
 - PixelRNN and PixelCNN
 - Variational Autoencoders (VAE)
 - Generative Adversarial Networks (GAN)

Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

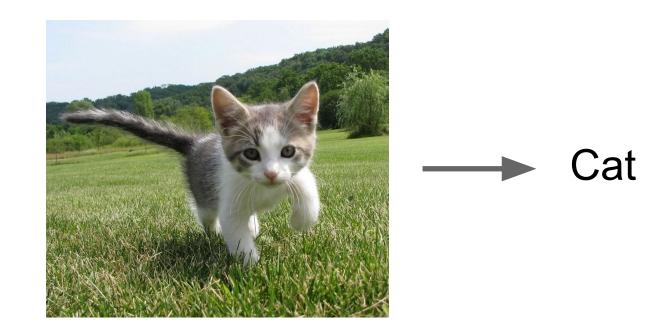
Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.



Classification

Supervised Learning

Data: (x, y)

x is data, y is label

Goal: Learn a function to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.



A cat sitting on a suitcase on the floor

Image captioning

Unsupervised Learning

Data: x
Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

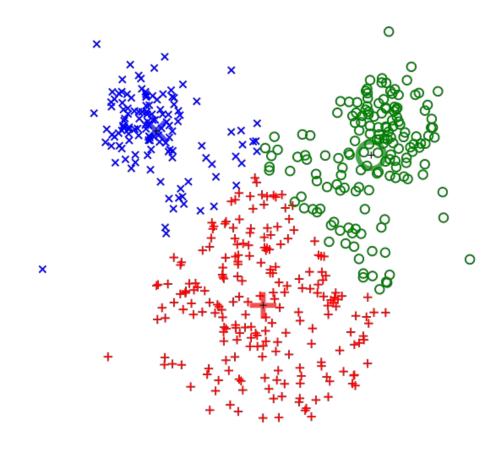
Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

Unsupervised Learning

Data: x
Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.



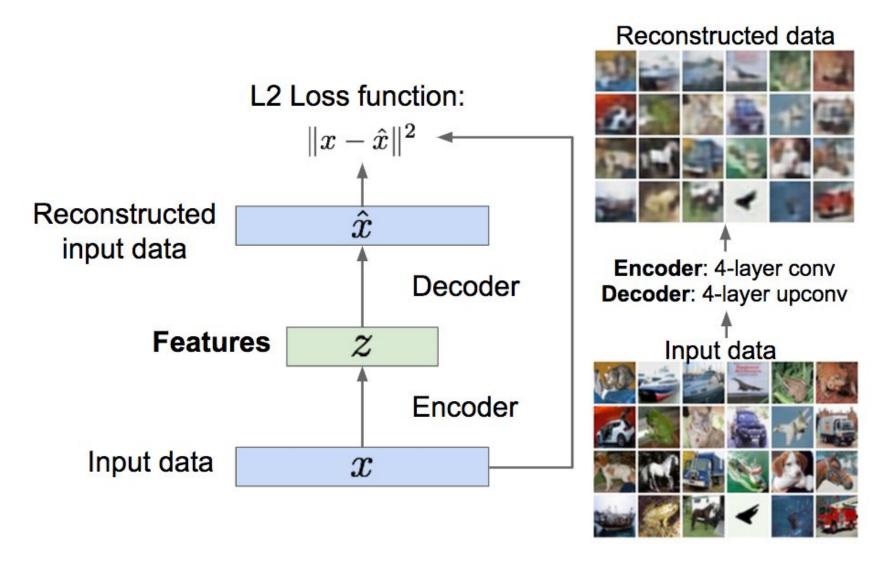
K-means clustering

Unsupervised Learning

Data: x
Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.



Autoencoders (Feature learning)

Unsupervised Learning

Data: x
Just data, no labels!

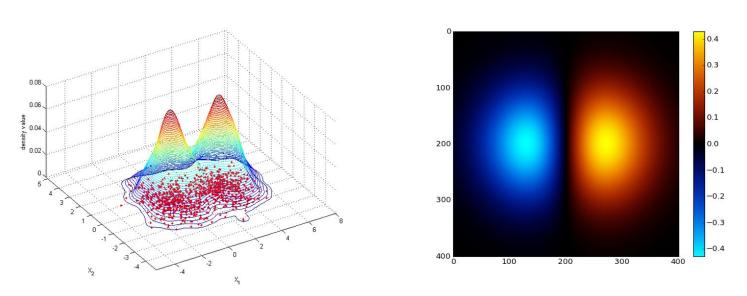
Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.



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1-d density estimation



2-d density estimation

Supervised Learning

Data: (x, y)

x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

Unsupervised Learning

Data: x

Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

Unsupervised Learning

Training data is cheap

Data: X

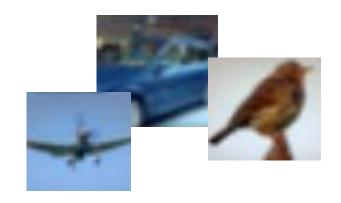
Holy grail: Solve unsupervised learning

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

Generative Models

Given training data, generate new samples from same distribution



Training data $\sim p_{data}(x)$

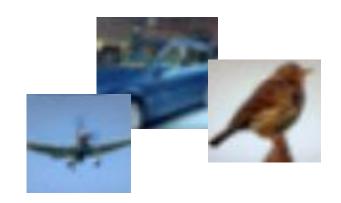


Generated samples $\sim p_{\text{model}}(x)$

Want to learn $p_{model}(x)$ similar to $p_{data}(x)$

Generative Models

Given training data, generate new samples from same distribution







Generated samples $\sim p_{model}(x)$

Want to learn $p_{model}(x)$ similar to $p_{data}(x)$

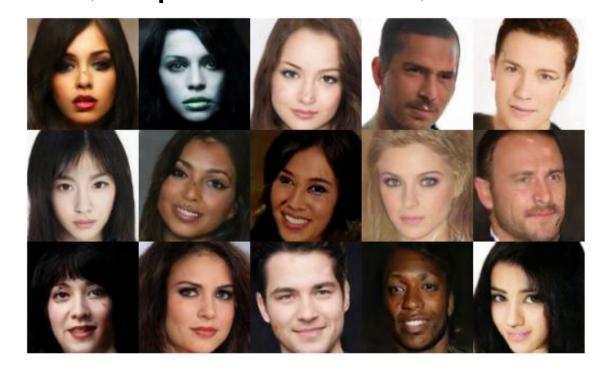
Addresses density estimation, a core problem in unsupervised learning **Several flavors**:

- Explicit density estimation: explicitly define and solve for p_{model}(x)
- Implicit density estimation: learn model that can sample from p_{model}(x) w/o explicitly defining it

Why Generative Models?

- Realistic samples for artwork, super-resolution, colorization, etc.







- Generative models of time-series data can be used for simulation and planning (reinforcement learning applications!)
- Training generative models can also enable inference of latent representations that can be useful as general features

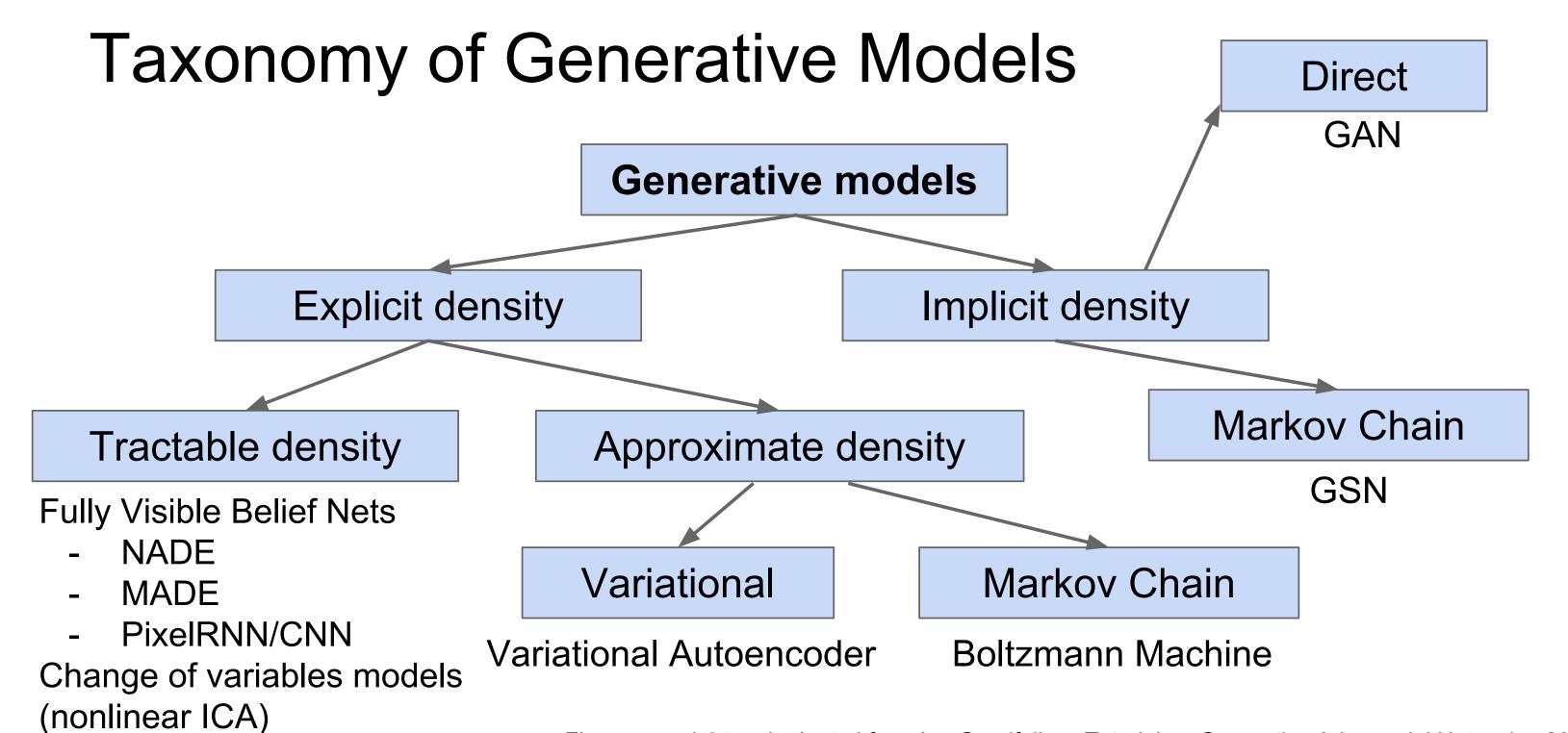


Figure copyright and adapted from Ian Goodfellow, Tutorial on Generative Adversarial Networks, 2017.

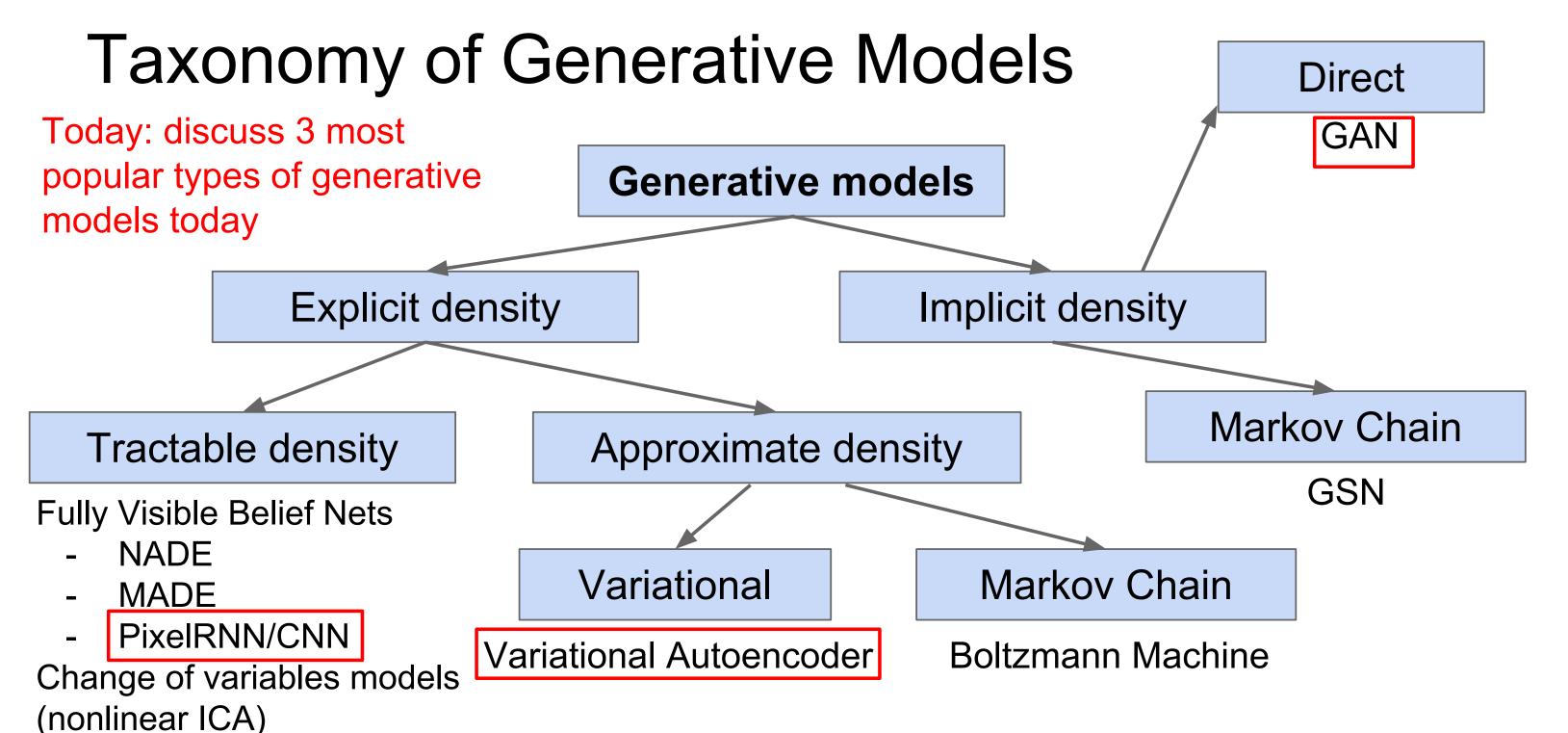


Figure copyright and adapted from Ian Goodfellow, Tutorial on Generative Adversarial Networks, 2017.

PixelRNN and PixelCNN

Fully visible belief network

Explicit density model

Use chain rule to decompose likelihood of an image x into product of 1-d distributions:

$$p(x) = \prod_{i=1}^n p(x_i|x_1,...,x_{i-1})$$
 \uparrow
Likelihood of image x

Probability of i'th pixel value given all previous pixels

Then maximize likelihood of training data

Fully visible belief network

Explicit density model

Use chain rule to decompose likelihood of an image x into product of 1-d distributions:

$$p(x) = \prod_{i=1}^n p(x_i|x_1,...,x_{i-1})$$

Likelihood of image x

Probability of i'th pixel value given all previous pixels

given all previous pixels

Complex distribution over pixel

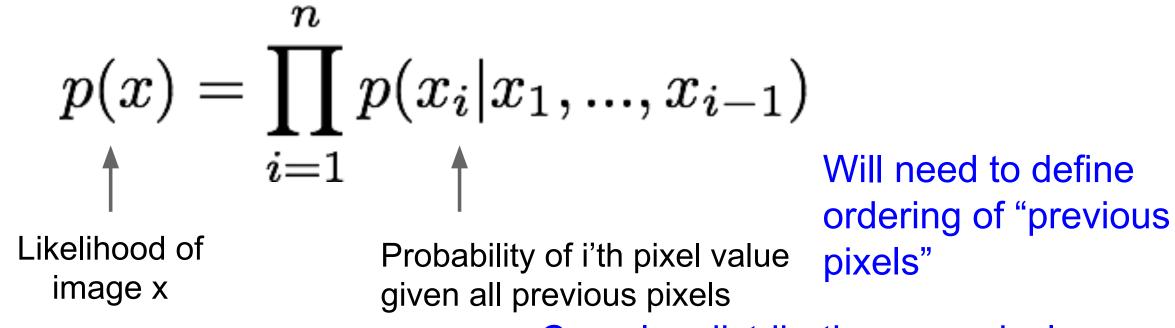
values => Express using a neural network!

Then maximize likelihood of training data

Fully visible belief network

Explicit density model

Use chain rule to decompose likelihood of an image x into product of 1-d distributions:

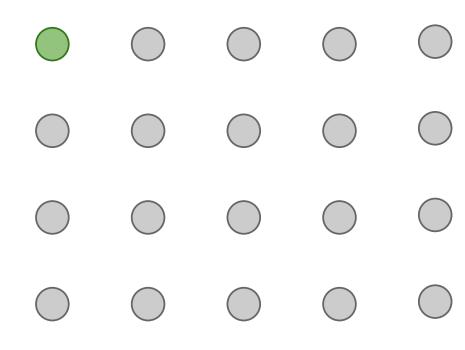


Then maximize likelihood of training data

Complex distribution over pixel values => Express using a neural network!

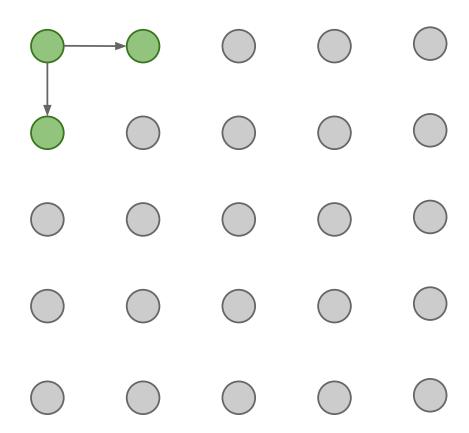
Generate image pixels starting from corner

Dependency on previous pixels modeled using an RNN (LSTM)



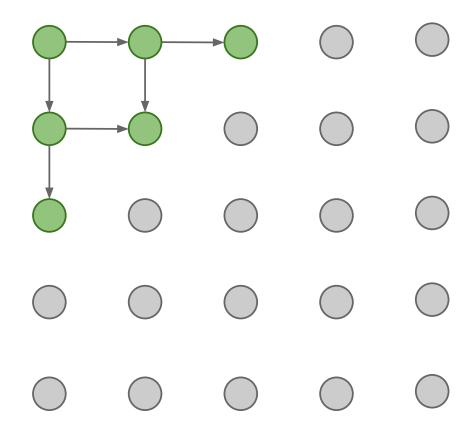
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Dependency on previous pixels modeled using an RNN (LSTM)



Generate image pixels starting from corner

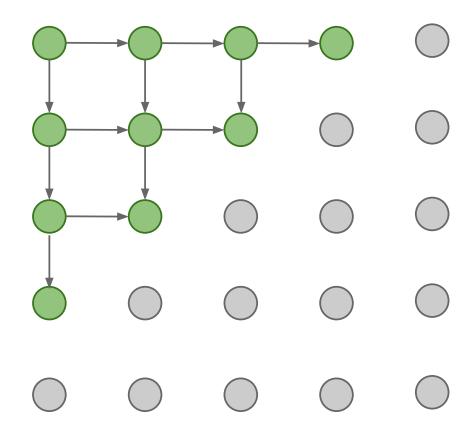
Dependency on previous pixels modeled using an RNN (LSTM)



Generate image pixels starting from corner

Dependency on previous pixels modeled using an RNN (LSTM)

Drawback: sequential generation is slow!



Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region

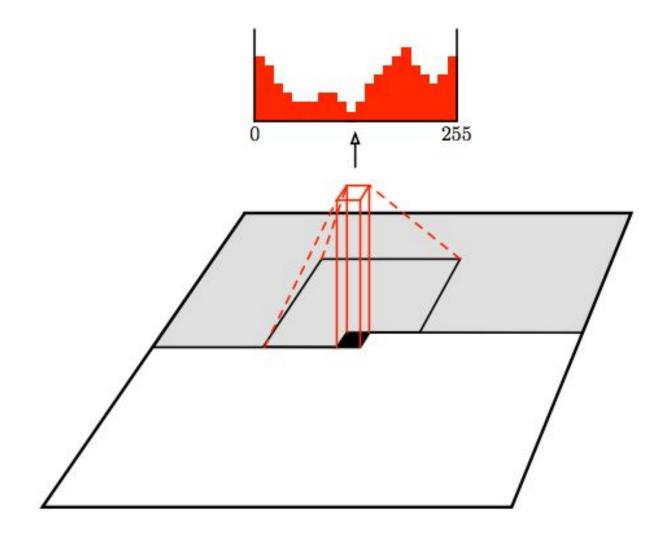


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Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region

Training: maximize likelihood of training images

$$p(x) = \prod_{i=1}^{n} p(x_i|x_1, ..., x_{i-1})$$

Softmax loss at each pixel

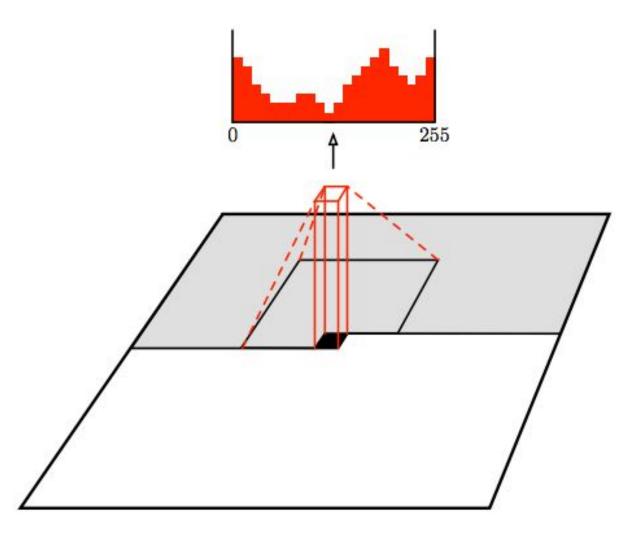


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Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region

Training is faster than PixelRNN (can parallelize convolutions since context region values known from training images)

Generation must still proceed sequentially => still slow

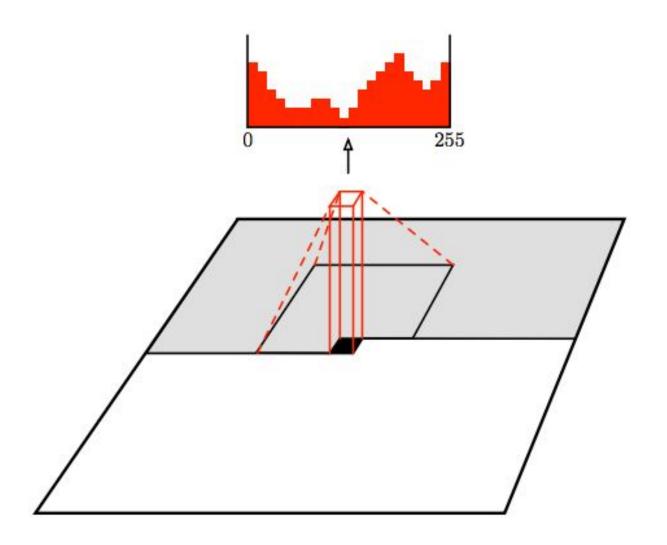
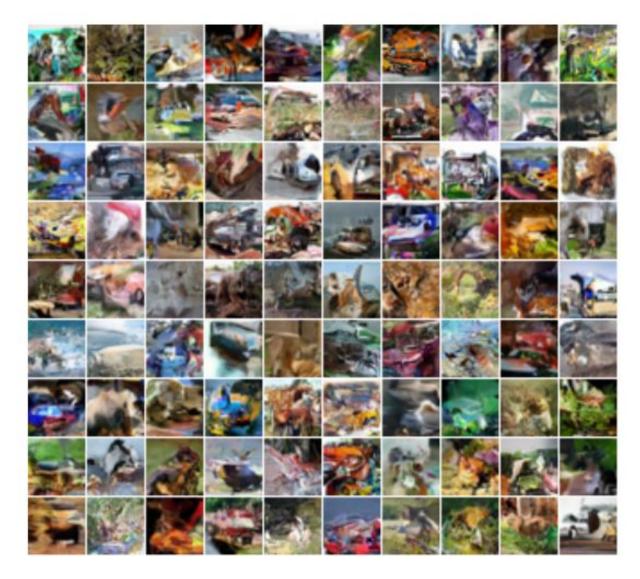
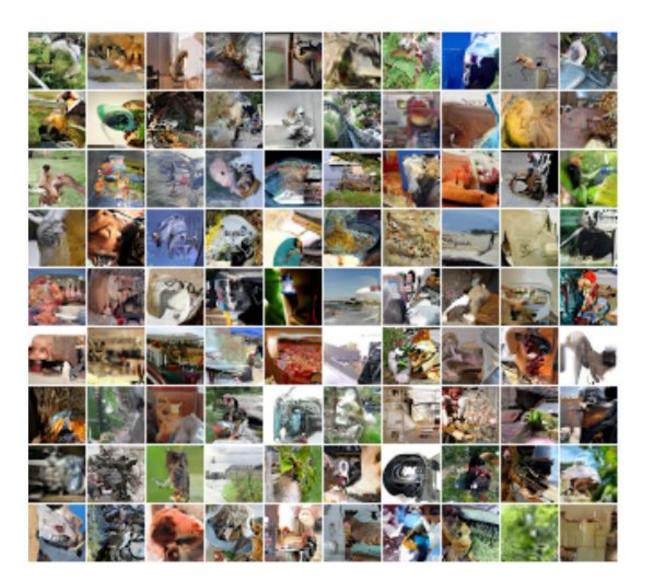


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Generation Samples



32x32 CIFAR-10



32x32 ImageNet

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PixelRNN and PixelCNN

Pros:

- Can explicitly compute likelihood p(x)
- Explicit likelihood of training data gives good evaluation metric
- Good samples

Con:

Sequential generation => slow

Improving PixelCNN performance

- Gated convolutional layers
- Short-cut connections
- Discretized logistic loss
- Multi-scale
- Training tricks
- Etc...

See

- Van der Oord et al. NIPS 2016
- Salimans et al. 2017 (PixelCNN++)

Variational Autoencoders (VAE)

So far...

PixelCNNs define tractable density function, optimize likelihood of training data:

$$p_{\theta}(x) = \prod_{i=1}^{n} p_{\theta}(x_i|x_1, ..., x_{i-1})$$

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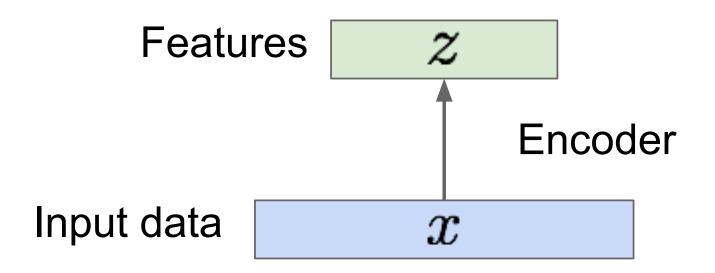
VAEs define intractable density function with latent **z**:

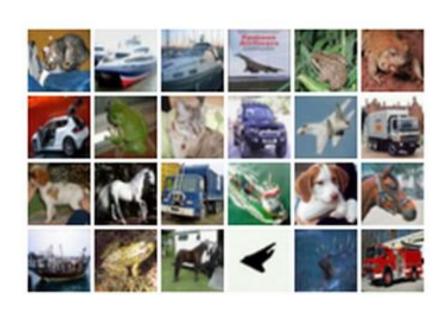
$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$

Cannot optimize directly, derive and optimize lower bound on likelihood instead

Some background first: Autoencoders

Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data





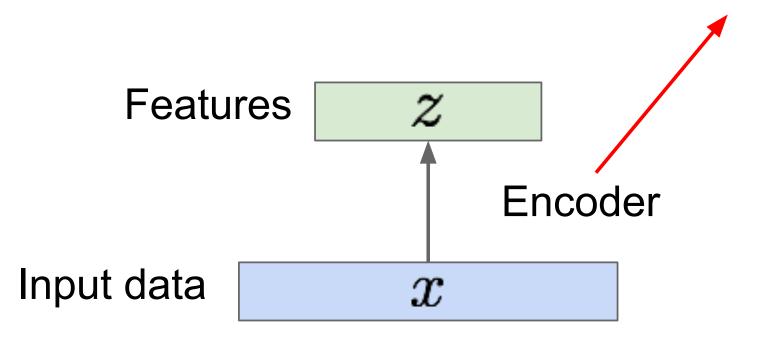
Some background first: Autoencoders

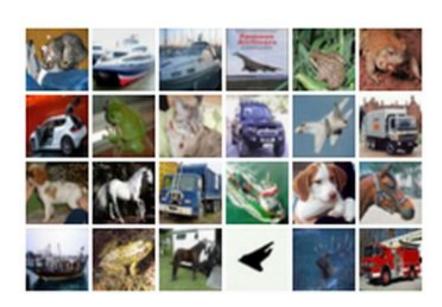
Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data

Originally: Linear + nonlinearity (sigmoid)

Later: Deep, fully-connected

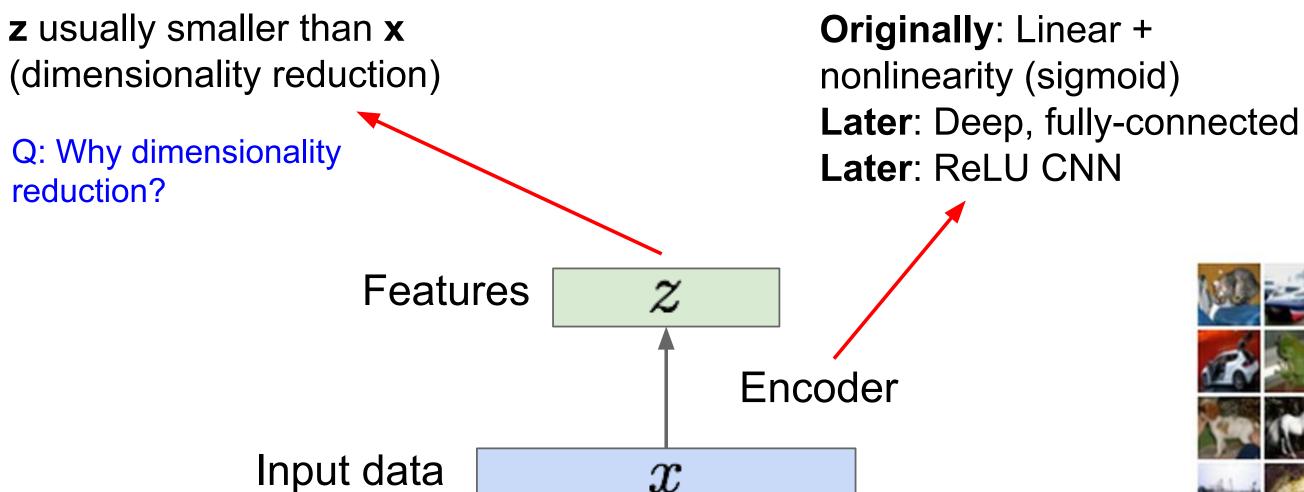
Later: ReLU CNN

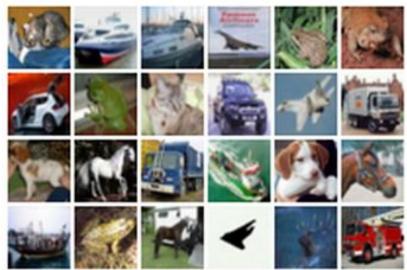




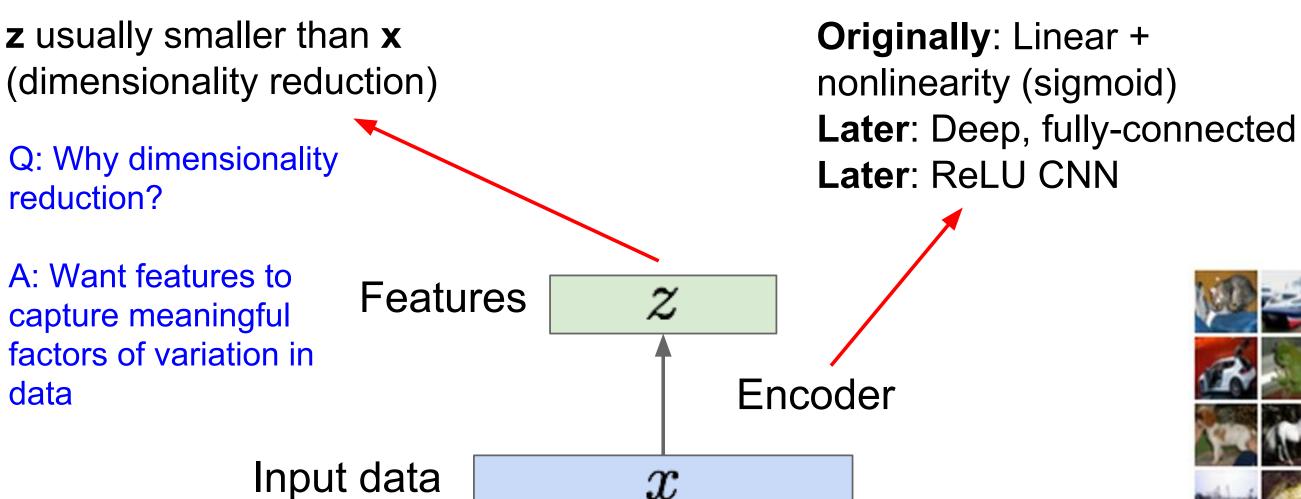
Some background first: Autoencoders

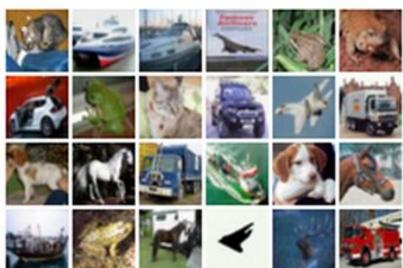
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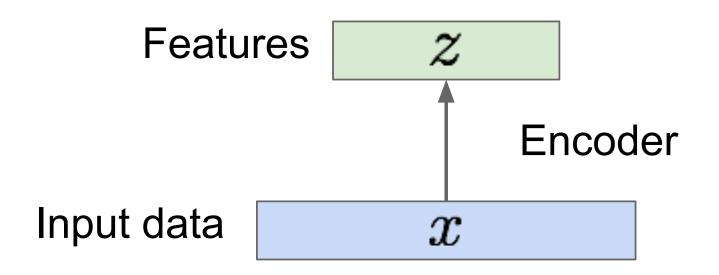


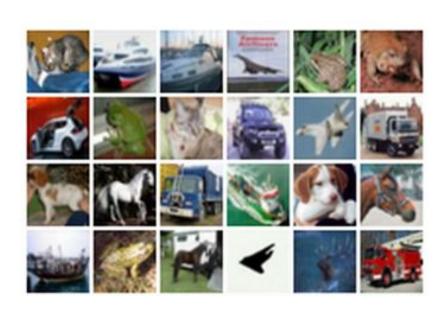
Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data





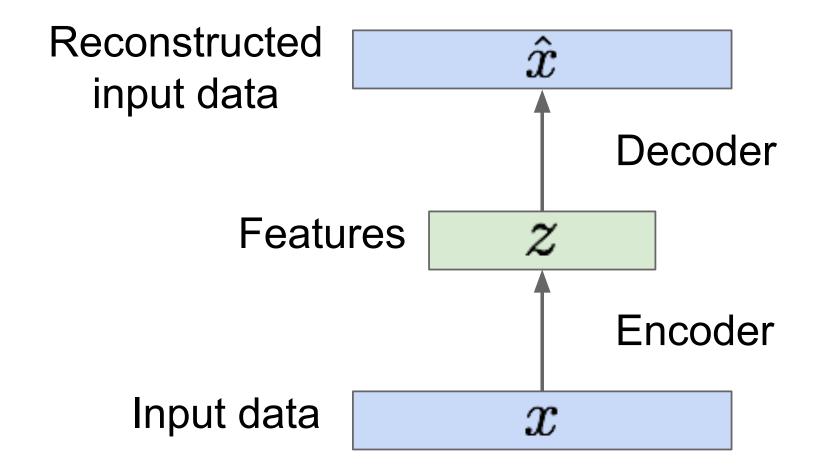
How to learn this feature representation?

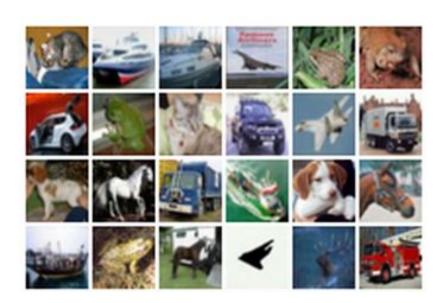




How to learn this feature representation?

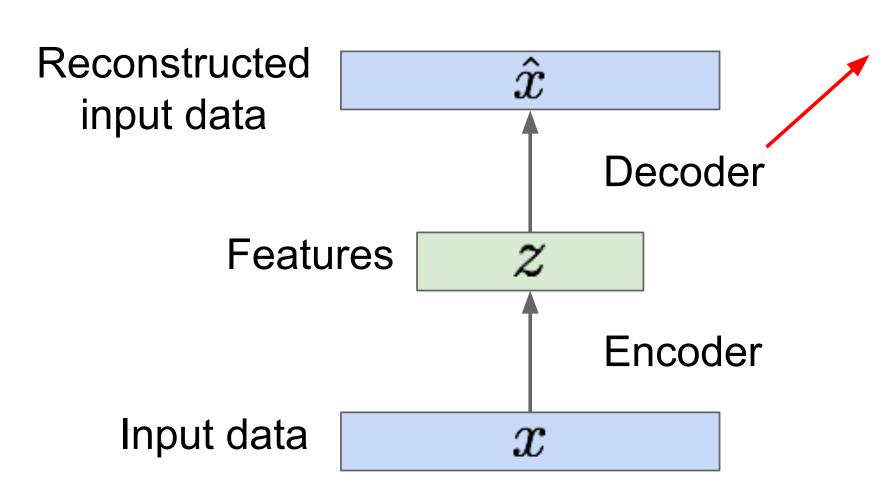
Train such that features can be used to reconstruct original data "Autoencoding" - encoding itself





How to learn this feature representation?

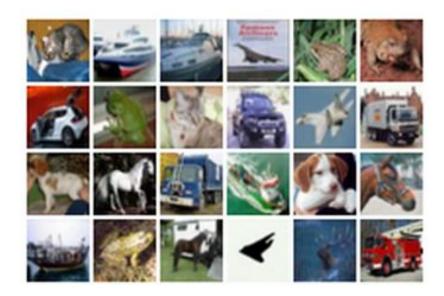
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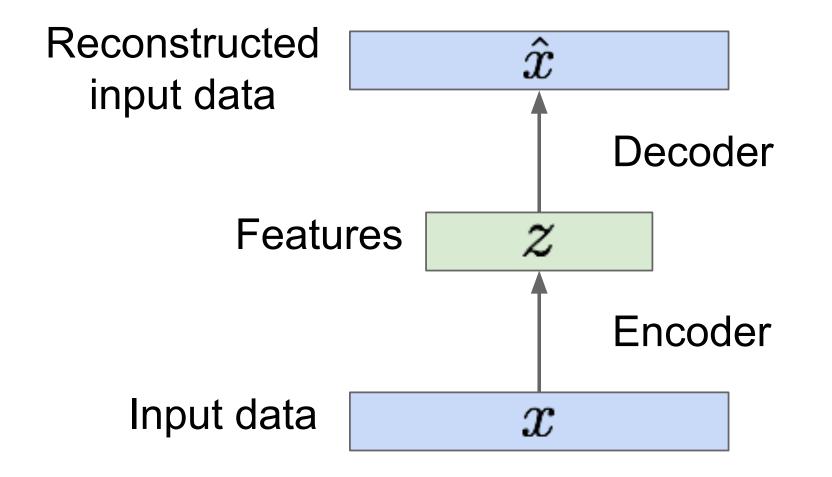
Later: Deep, fully-connected

Later: ReLU CNN (upconv)



How to learn this feature representation?

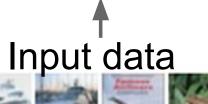
Train such that features can be used to reconstruct original data "Autoencoding" - encoding itself

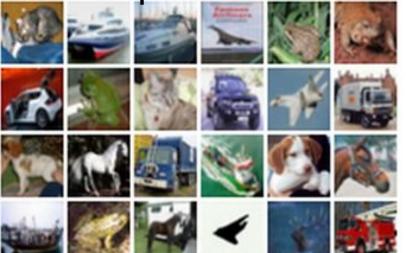


Reconstructed data



Encoder: 4-layer conv Decoder: 4-layer upconv





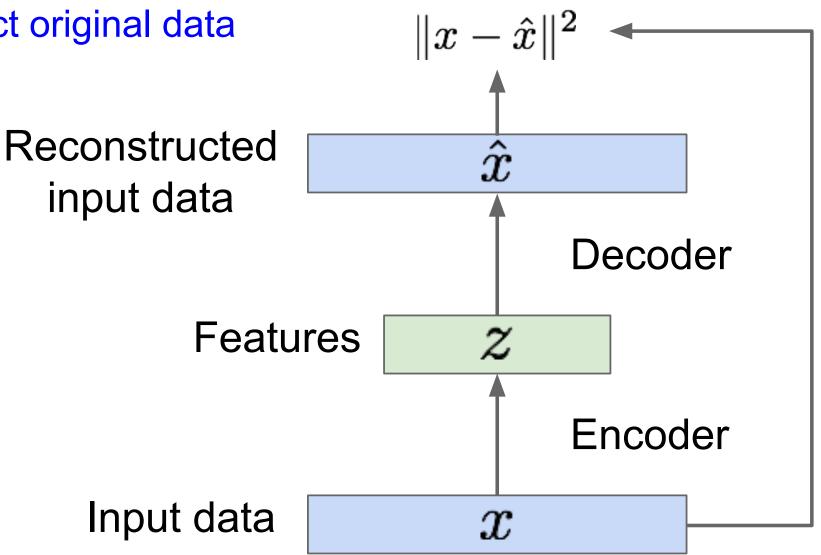
Train such that features L2 Loss function: can be used to reconstruct original data $||x - \hat{x}||^2$ Reconstructed \hat{x} input data Decoder Features Encoder Input data x

Reconstructed data Encoder: 4-layer conv Decoder: 4-layer upconv Input data

Train such that features can be used to reconstruct original data

Doesn't use labels!

L2 Loss function:



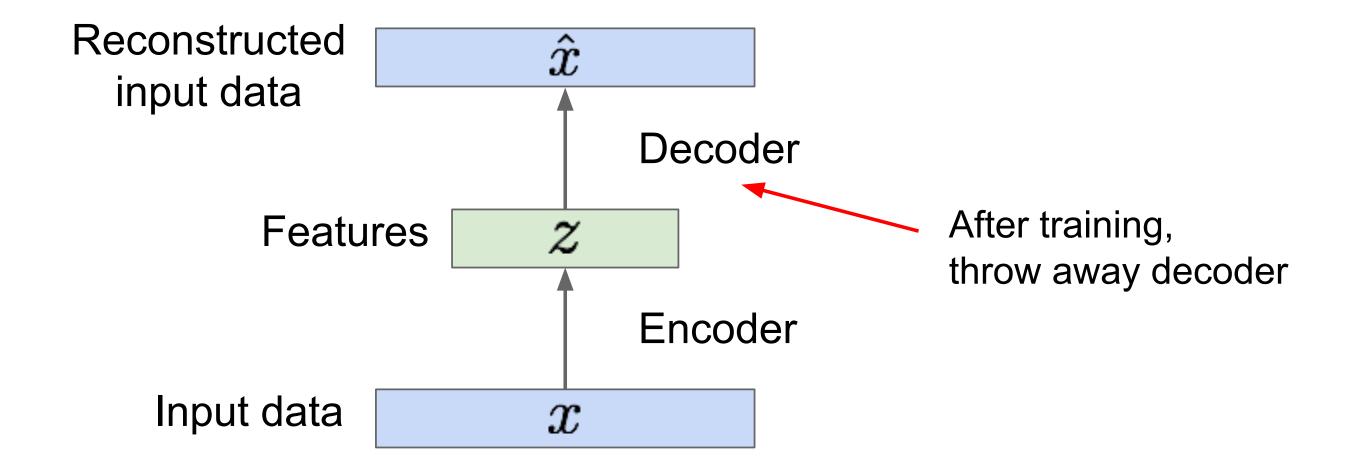
Reconstructed data



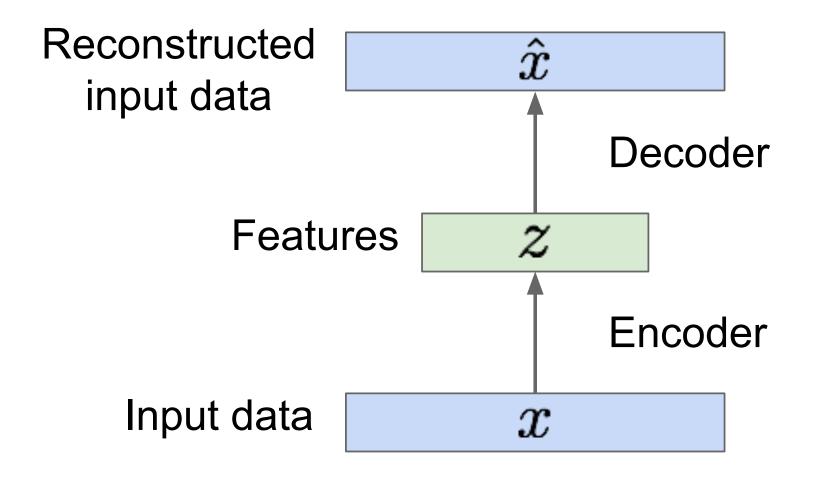
Encoder: 4-layer conv Decoder: 4-layer upconv







Loss function bird plane (Softmax, etc) deer truck dog \hat{y} y**Predicted Label** Train for final task Fine-tune Classifier (sometimes with encoder Encoder can be small data) jointly with **Features** zused to initialize a classifier **supervised** model Encoder Input data x



Autoencoders can reconstruct data, and can learn features to initialize a supervised model

Features capture factors of variation in training data. Can we generate new images from an autoencoder?

Probabilistic spin on autoencoders - will let us sample from the model to generate data!

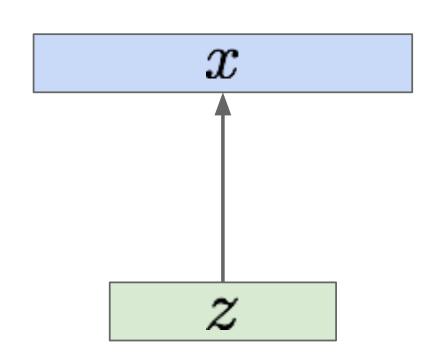
Probabilistic spin on autoencoders - will let us sample from the model to generate data!

Assume training data $\{x^{(i)}\}_{i=1}^N$ is generated from underlying unobserved (latent) representation **z**

Sample from true conditional

$$p_{\theta^*}(x \mid z^{(i)})$$

Sample from true prior $p_{\theta^*}(z)$



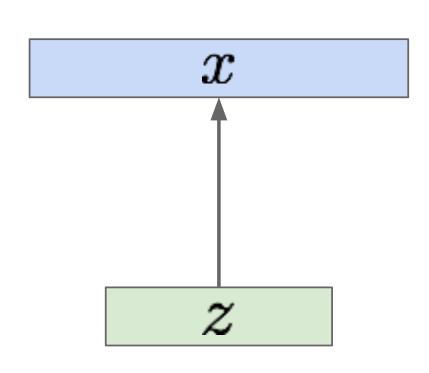
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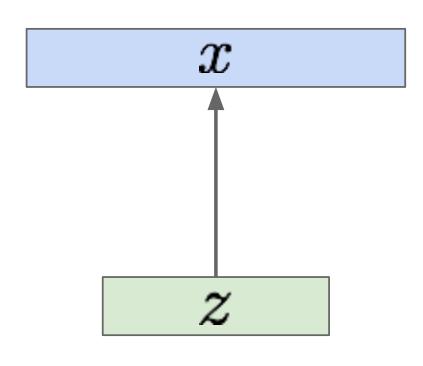


Intuition (remember from autoencoders!): **x** is an image, **z** is latent factors used to generate **x**: attributes, orientation, etc.

Sample from true conditional

$$p_{\theta^*}(x \mid z^{(i)})$$

Sample from true prior $p_{\theta^*}(z)$

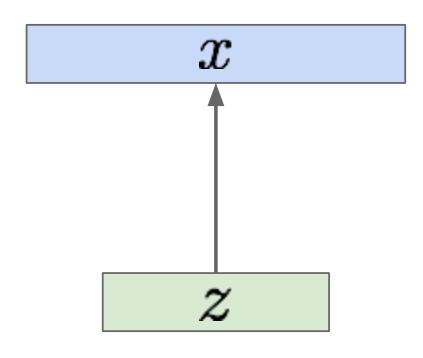


We want to estimate the true parameters θ^* of this generative model.

Sample from true conditional

$$p_{\theta^*}(x \mid z^{(i)})$$

Sample from true prior $p_{\theta^*}(z)$



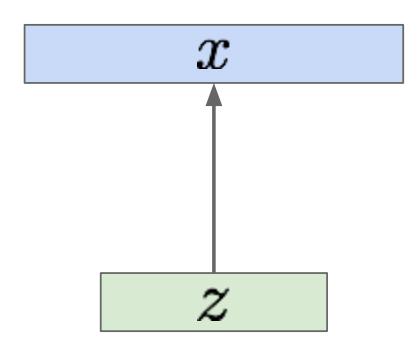
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How should we represent this model?

Sample from true conditional

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We want to estimate the true parameters θ^* of this generative model.

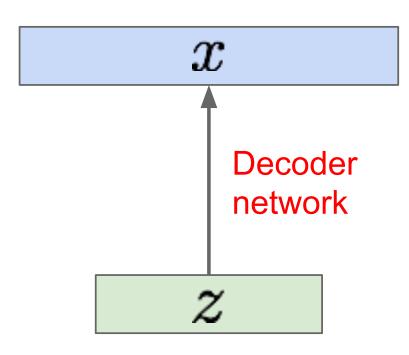
How should we represent this model?

Choose prior p(z) to be simple, e.g. Gaussian. Reasonable for latent attributes, e.g. pose, how much smile.

Sample from true conditional

$$p_{\theta^*}(x \mid z^{(i)})$$

Sample from true prior $p_{\theta^*}(z)$



We want to estimate the true parameters θ^* of this generative model.

How should we represent this model?

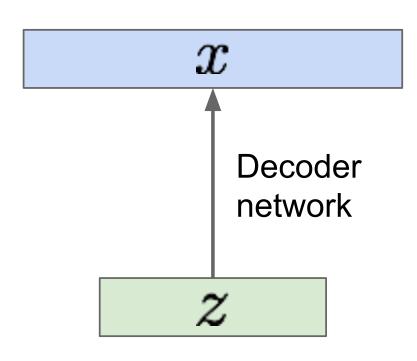
Choose prior p(z) to be simple, e.g. Gaussian.

Conditional p(x|z) is complex (generates image) => represent with neural network

Sample from true conditional

$$p_{\theta^*}(x \mid z^{(i)})$$

Sample from true prior $p_{\theta^*}(z)$



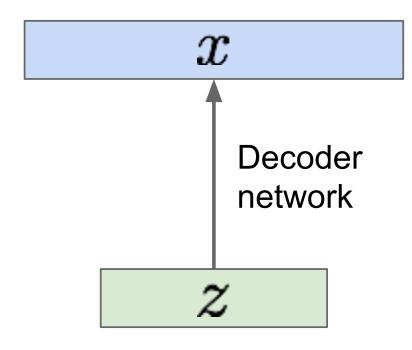
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How to train the model?

Sample from true conditional

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We want to estimate the true parameters θ^* of this generative model.

How to train the model?

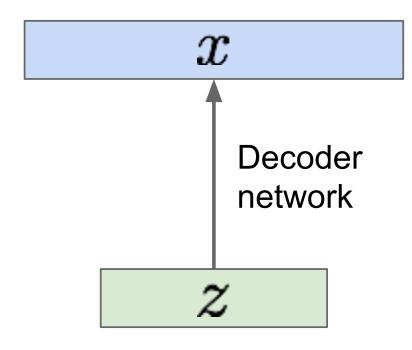
Remember strategy for training generative models from FVBNs. Learn model parameters to maximize likelihood of training data

$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Sample from true conditional

$$p_{\theta^*}(x \mid z^{(i)})$$

Sample from true prior $p_{\theta^*}(z)$



We want to estimate the true parameters θ^* of this generative model.

How to train the model?

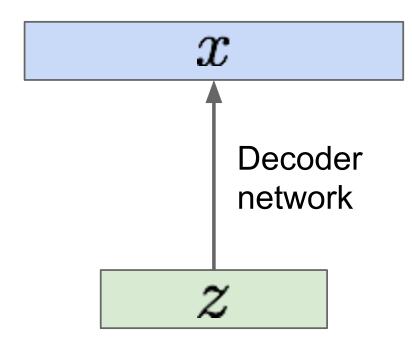
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$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$

Sample from true conditional

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We want to estimate the true parameters θ^* of this generative model.

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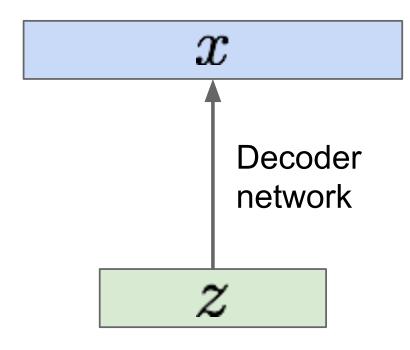
$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Q: What is the problem with this?

Sample from true conditional

$$p_{\theta^*}(x \mid z^{(i)})$$

Sample from true prior $p_{\theta^*}(z)$



We want to estimate the true parameters θ^* of this generative model.

How to train the model?

Remember strategy for training generative models from FVBNs. Learn model parameters to maximize likelihood of training data

$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Q: What is the problem with this?

Intractable!

Data likelihood: $p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$

Data likelihood:
$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$
 Simple Gaussian prior

Decoder neural network

Data likelihood:
$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$

Data likelihood:
$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Intractible to compute p(x|z) for every z!

Data likelihood: $p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$

Posterior density also intractable: $p_{\theta}(z|x) = p_{\theta}(x|z)p_{\theta}(z)/p_{\theta}(x)$

Data likelihood:
$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$

Posterior density also intractable: $p_{ heta}(z|x) = p_{ heta}(x|z)p_{ heta}(z)/p_{ heta}(x)$

Intractable data likelihood

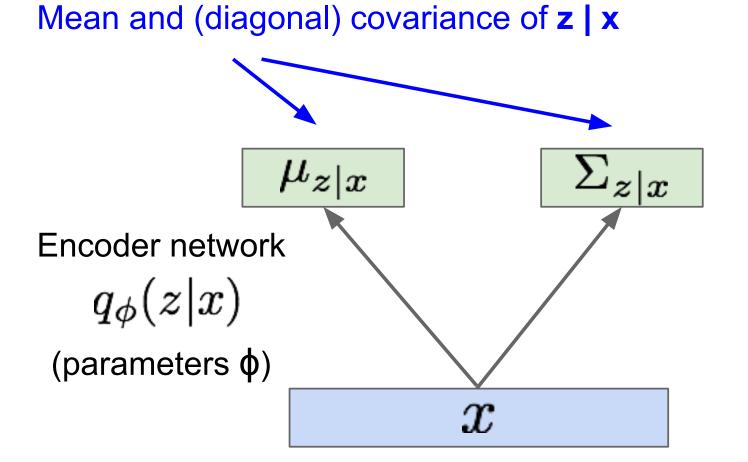
Data likelihood:
$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$

Posterior density also intractable: $p_{ heta}(z|x) = p_{ heta}(x|z)p_{ heta}(z)/p_{ heta}(x)$

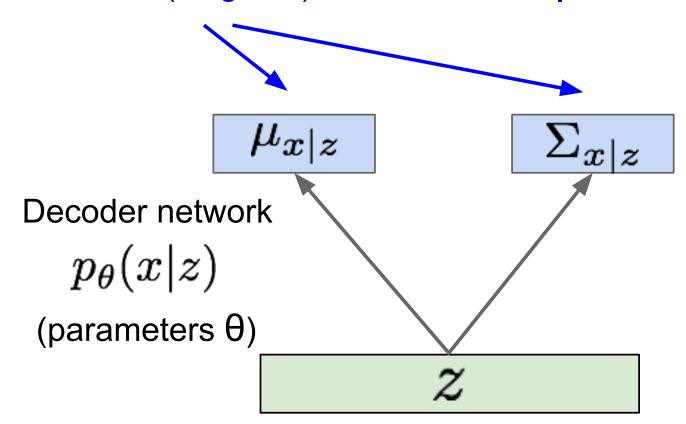
Solution: In addition to decoder network modeling $p_{\theta}(x|z)$, define additional encoder network $q_{\theta}(z|x)$ that approximates $p_{\theta}(z|x)$

Will see that this allows us to derive a lower bound on the data likelihood that is tractable, which we can optimize

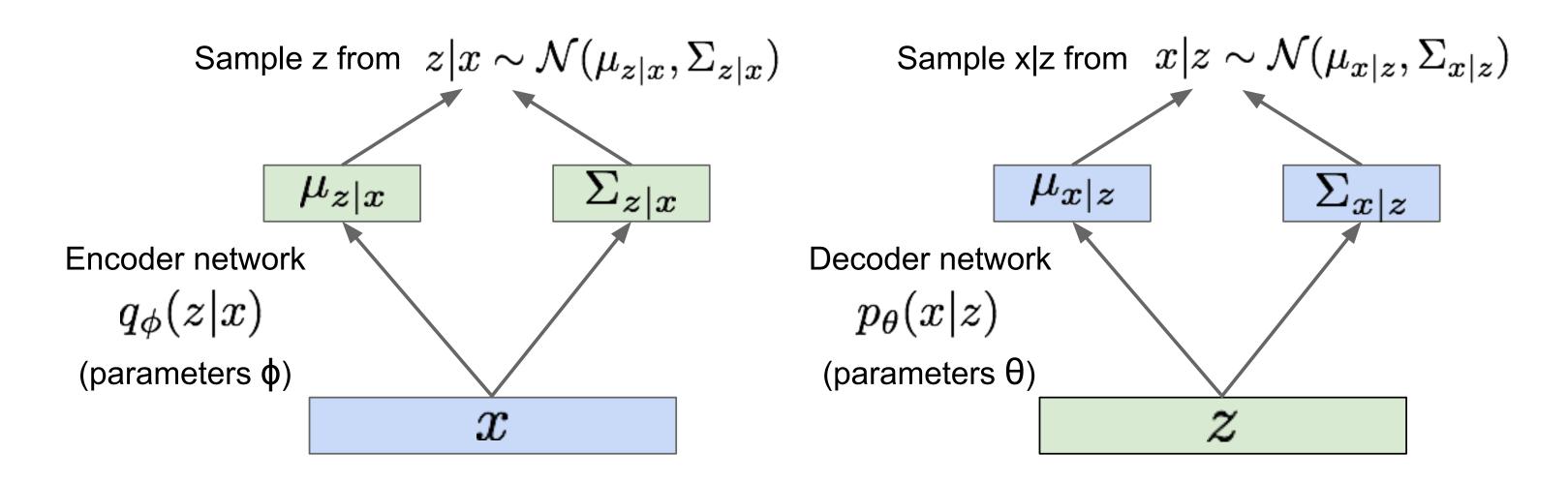
Since we're modeling probabilistic generation of data, encoder and decoder networks are probabilistic



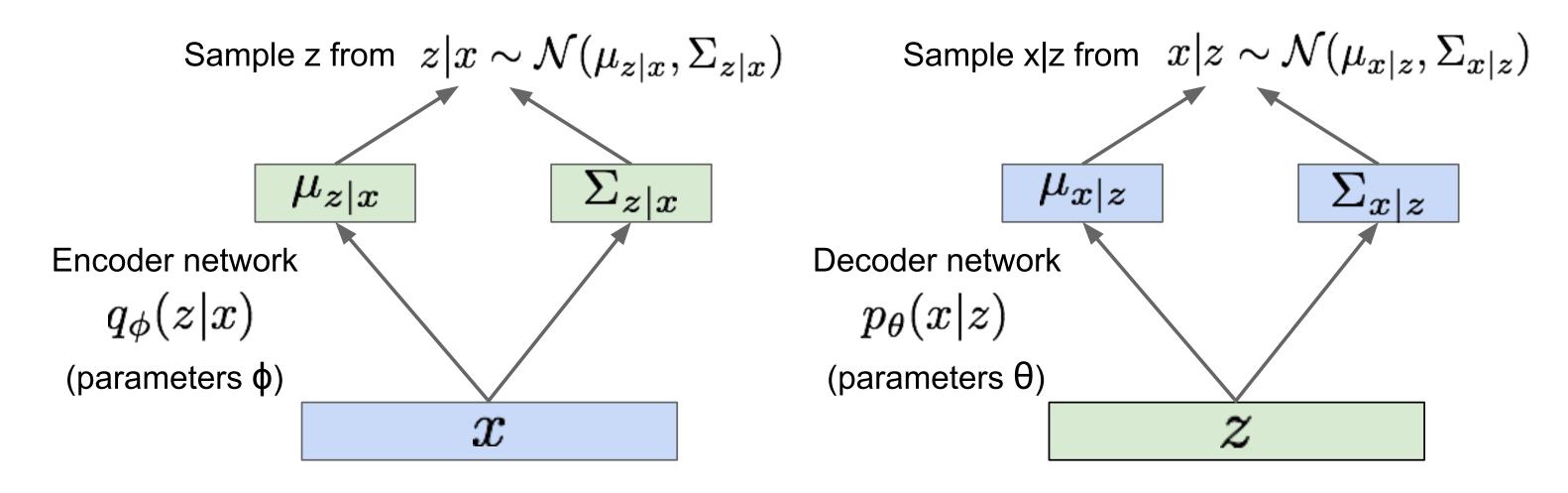
Mean and (diagonal) covariance of x | z



Since we're modeling probabilistic generation of data, encoder and decoder networks are probabilistic



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Encoder and decoder networks also called "recognition"/"inference" and "generation" networks

Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)}) \right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$

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Taking expectation wrt. z (using encoder network) will come in handy later

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The expectation wrt. z (using encoder network) let us write nice KL terms

Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

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Decoder network gives $p_{\theta}(x|z)$, can compute estimate of this term through sampling. (Sampling differentiable through reparam. trick, see paper.)

This KL term (between Gaussians for encoder and z prior) has nice closed-form solution!

 $p_{\theta}(z|x)$ intractable (saw earlier), can't compute this KL term :(But we know KL divergence always >= 0.

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Tractable lower bound which we can take gradient of and optimize! ($p_{\theta}(x|z)$ differentiable, KL term differentiable)

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$$\underbrace{\mathcal{L}(x^{(i)}, \theta, \phi)}_{\theta, \phi} = \arg \max_{\theta, \phi} \sum_{i=1}^{N} \mathcal{L}(x^{(i)}, \theta, \phi)$$

$$\log p_{\theta}(x^{(i)}) \ge \mathcal{L}(x^{(i)}, \theta, \phi)$$

Variational lower bound ("ELBO")

$$\theta^*, \phi^* = \arg\max_{\theta, \phi} \sum_{i=1}^{N} \mathcal{L}(x^{(i)}, \theta, \phi)$$

Training: Maximize lower bound

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$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)}|z)p_{\theta}(z)}{p_{\theta}(z|x^{(i)})}\right] \quad (\text{Bayes' Rule}) \qquad \text{Make approximate}$$

$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)}|z)p_{\theta}(z)}{p_{\theta}(z|x^{(i)})} \frac{q_{\phi}(z|x^{(i)})}{q_{\phi}(z|x^{(i)})}\right] \quad (\text{Multiply by constant}) \quad \text{close to prior}$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)}|z)\right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z|x^{(i)})}{p_{\theta}(z)}\right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z|x^{(i)})}{p_{\theta}(z|x^{(i)})}\right] \quad (\text{Logarithms})$$

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Putting it all together: maximizing the likelihood lower bound

$$\underbrace{\mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid\mid p_{\theta}(z))}_{\mathcal{L}(x^{(i)}, \theta, \phi)}$$

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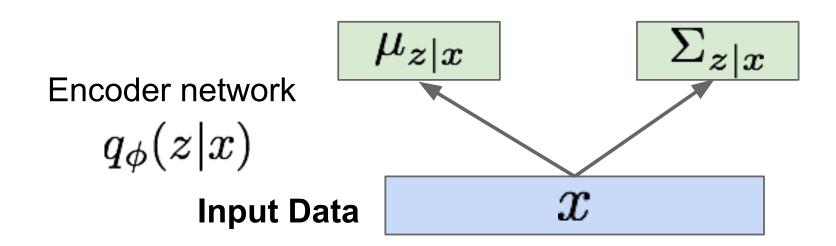
Let's look at computing the bound (forward pass) for a given minibatch of input data

Input Data

x

Putting it all together: maximizing the likelihood lower bound

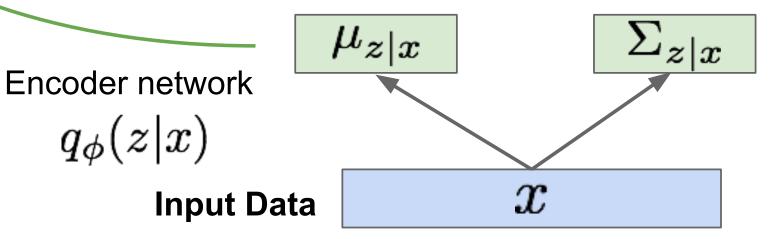
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Putting it all together: maximizing the likelihood lower bound

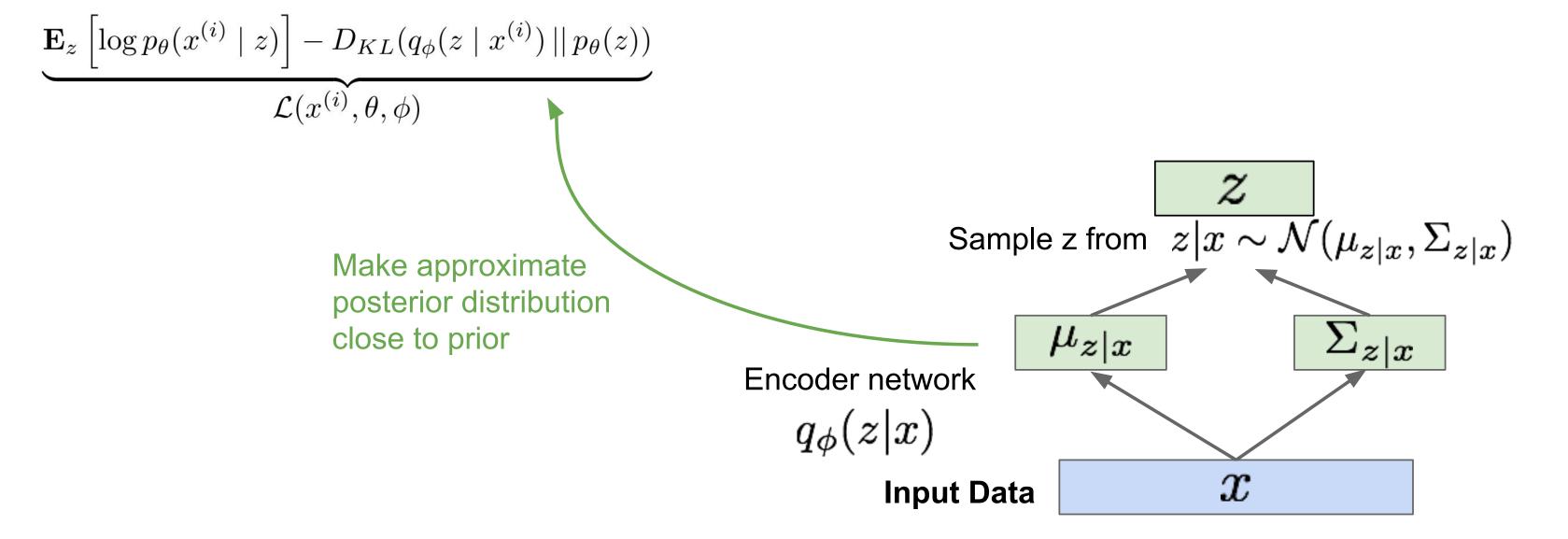
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Make approximate posterior distribution close to prior

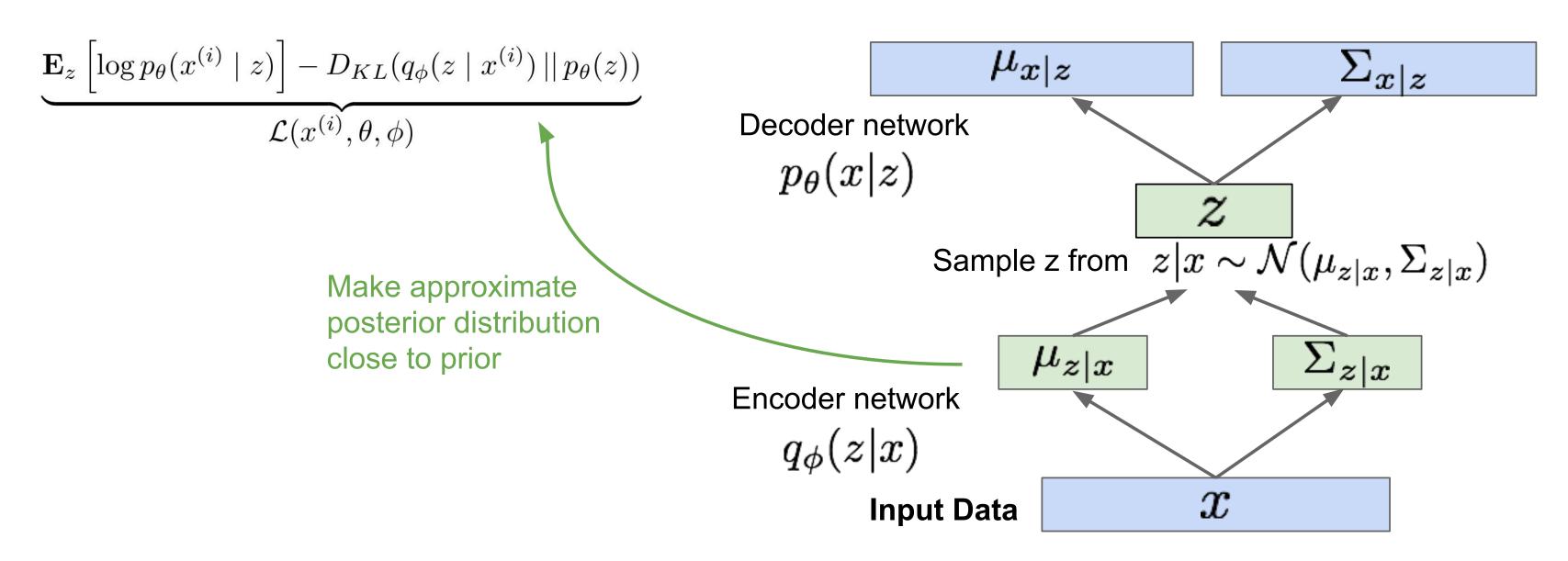


 $q_{\phi}(z|x)$

Putting it all together: maximizing the likelihood lower bound



Putting it all together: maximizing the likelihood lower bound



Putting it all together: maximizing the likelihood lower bound

$$\mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid\mid p_{\theta}(z))$$

 $\mathcal{L}(x^{(i)}, \theta, \phi)$

Make approximate posterior distribution close to prior

Maximize likelihood of original input being reconstructed

 \hat{x} Sample x|z from $x|z \sim \mathcal{N}(\mu_{x|z}, \Sigma_{x|z})$ $\mu_{x|z}$

 $\Sigma_{x|z}$

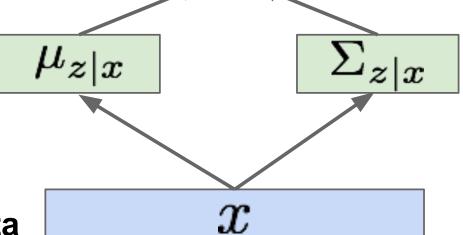
Decoder network

$$p_{\theta}(x|z)$$

Encoder network

 $q_{\phi}(z|x)$

Sample z from $z|x \sim \mathcal{N}(\mu_{z|x}, \Sigma_{z|x})$



Input Data

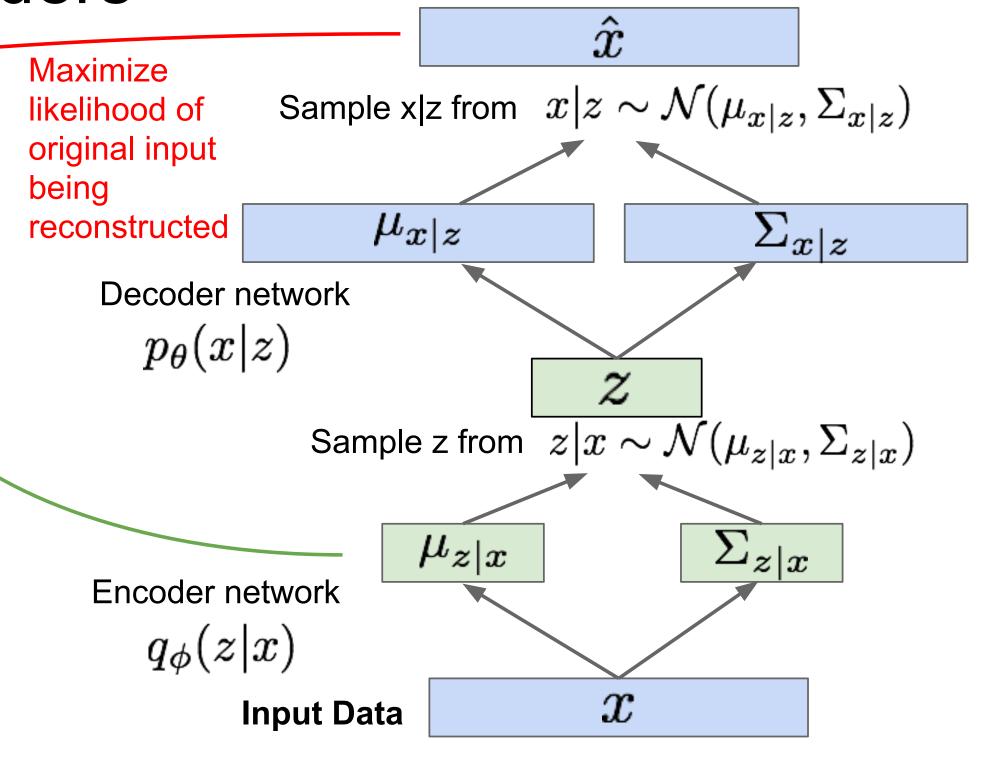
Putting it all together: maximizing the likelihood lower bound

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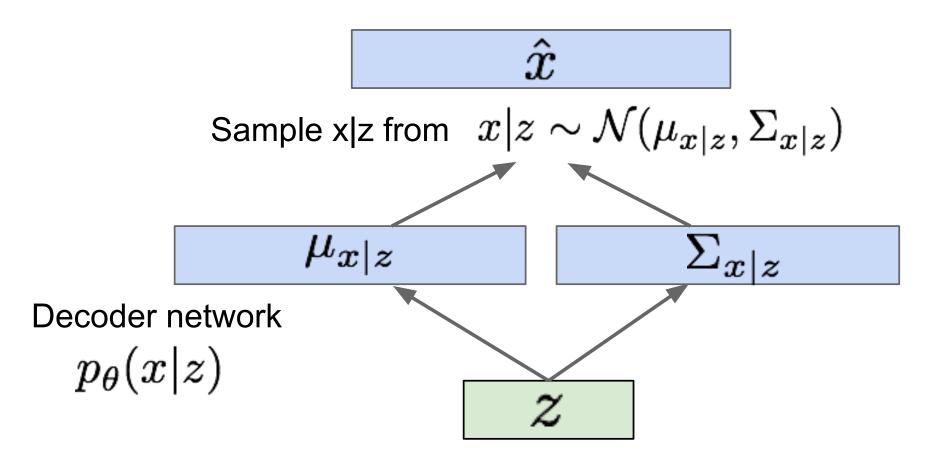
 $\mathcal{L}(x^{(i)}, \theta, \phi)$

Make approximate posterior distribution close to prior

For every minibatch of input data: compute this forward pass, and then backprop!



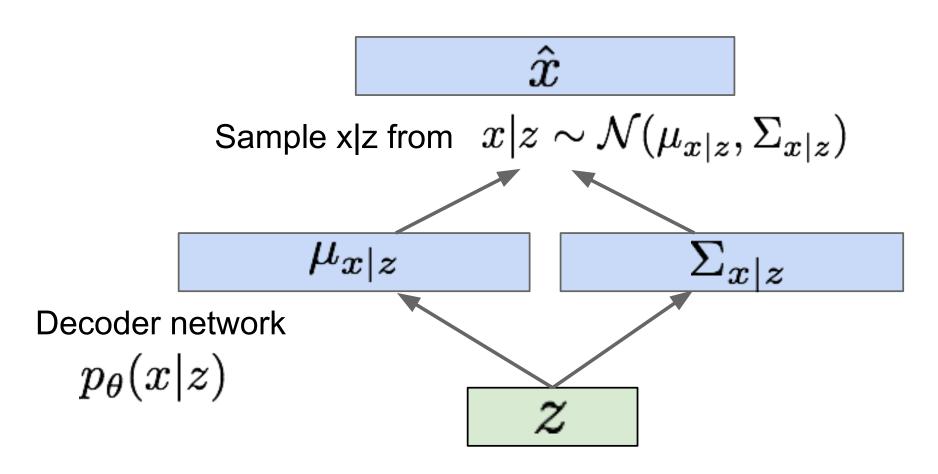
Use decoder network. Now sample z from prior!



Sample z from $z \sim \mathcal{N}(0, I)$

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

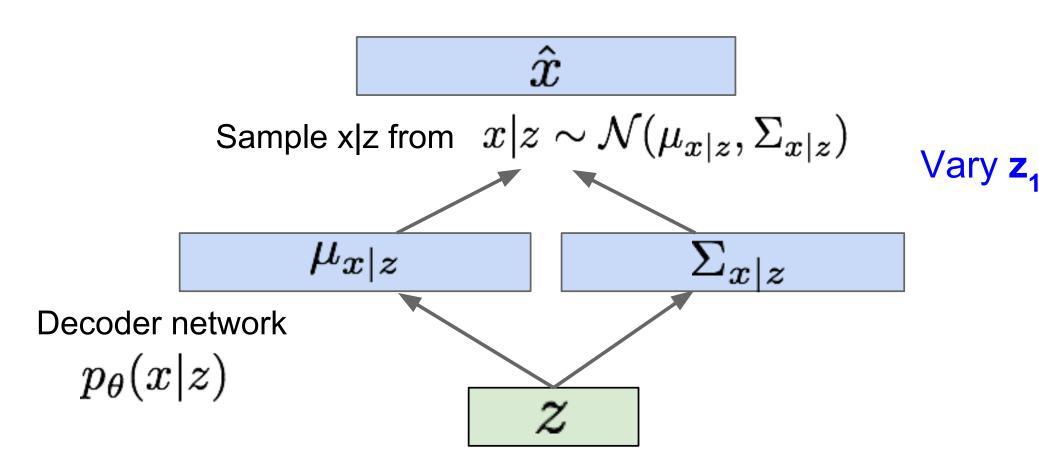
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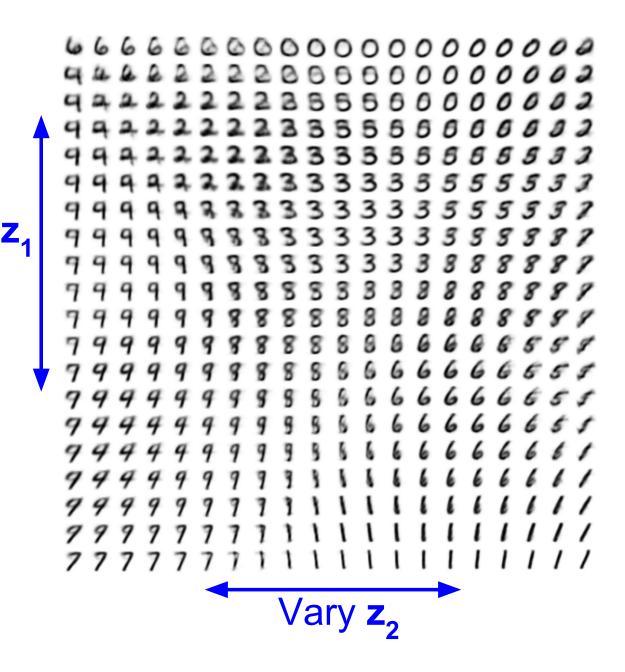
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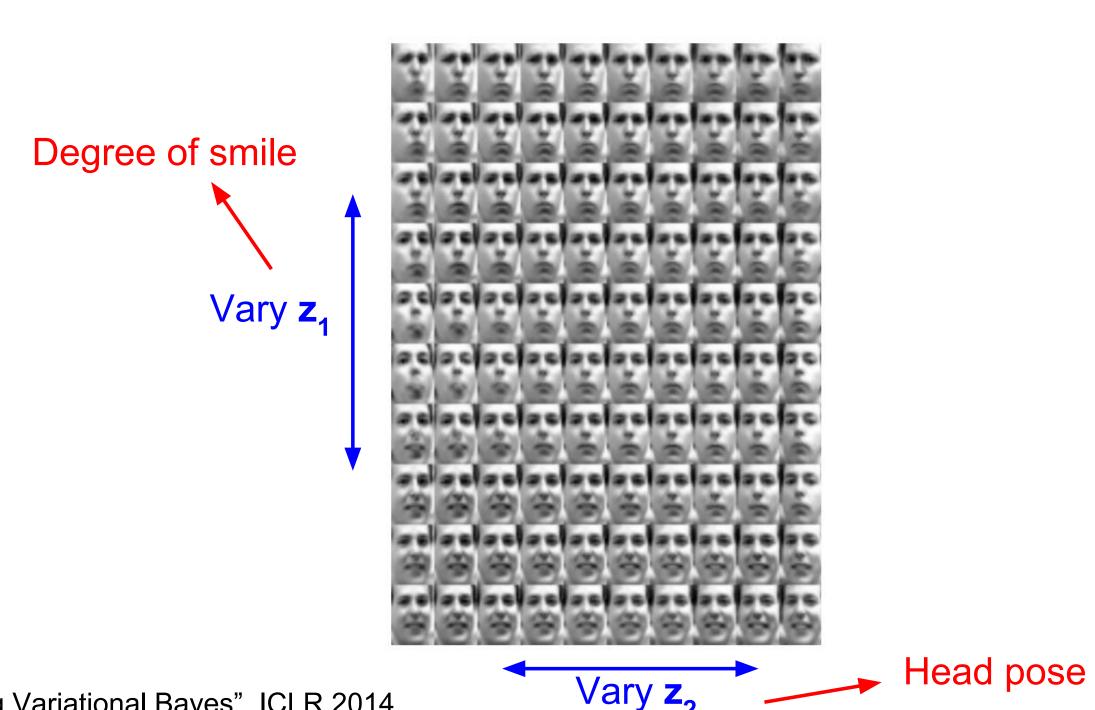
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Data manifold for 2-d z



Diagonal prior on **z** => independent latent variables

Different dimensions of **z** encode interpretable factors of variation



Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

Diagonal prior on **z** => independent latent variables

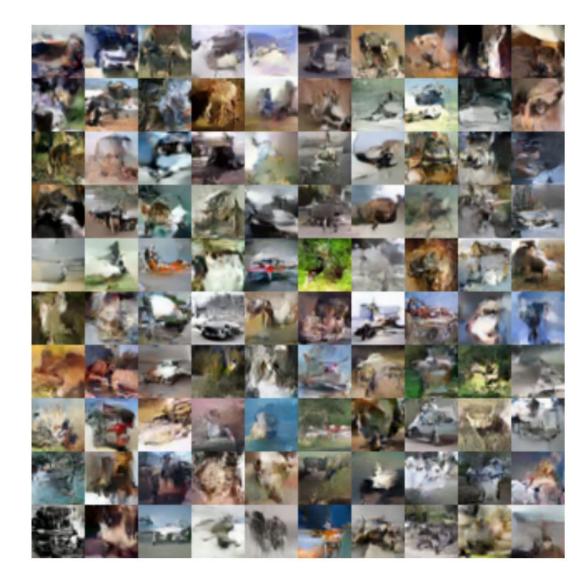
Different dimensions of **z** encode interpretable factors of variation

Also good feature representation that can be computed using $q_{\omega}(z|x)!$

Degree of smile Vary z₁ Head pose

Vary **z**₂

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014



32x32 CIFAR-10



Labeled Faces in the Wild

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Probabilistic spin to traditional autoencoders => allows generating data

Defines an intractable density => derive and optimize a (variational) lower bound

Pros:

- Principled approach to generative models
- Allows inference of q(z|x), can be useful feature representation for other tasks

Cons:

- Maximizes lower bound of likelihood: okay, but not as good evaluation as PixelRNN/PixelCNN
- Samples blurrier and lower quality compared to state-of-the-art (GANs)

Active areas of research:

- More flexible approximations, e.g. richer approximate posterior instead of diagonal Gaussian
- Incorporating structure in latent variables

Generative Adversarial Networks (GAN)

So far...

PixelCNNs define tractable density function, optimize likelihood of training data:

$$p_{\theta}(x) = \prod_{i=1}^{n} p_{\theta}(x_i|x_1, ..., x_{i-1})$$

VAEs define intractable density function with latent **z**:

$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$

Cannot optimize directly, derive and optimize lower bound on likelihood instead

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What if we give up on explicitly modeling density, and just want ability to sample?

GANs: don't work with any explicit density function! Instead, take game-theoretic approach: learn to generate from training distribution through 2-player game

Generative Adversarial Networks

Problem: Want to sample from complex, high-dimensional training distribution. No direct way to do this!

Solution: Sample from a simple distribution, e.g. random noise. Learn transformation to training distribution.

Q: What can we use to represent this complex transformation?

Generative Adversarial Networks

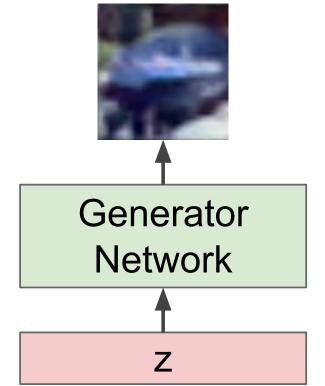
Problem: Want to sample from complex, high-dimensional training distribution. No direct way to do this!

Solution: Sample from a simple distribution, e.g. random noise. Learn transformation to training distribution.

Q: What can we use to represent this complex transformation?

A: A neural network!

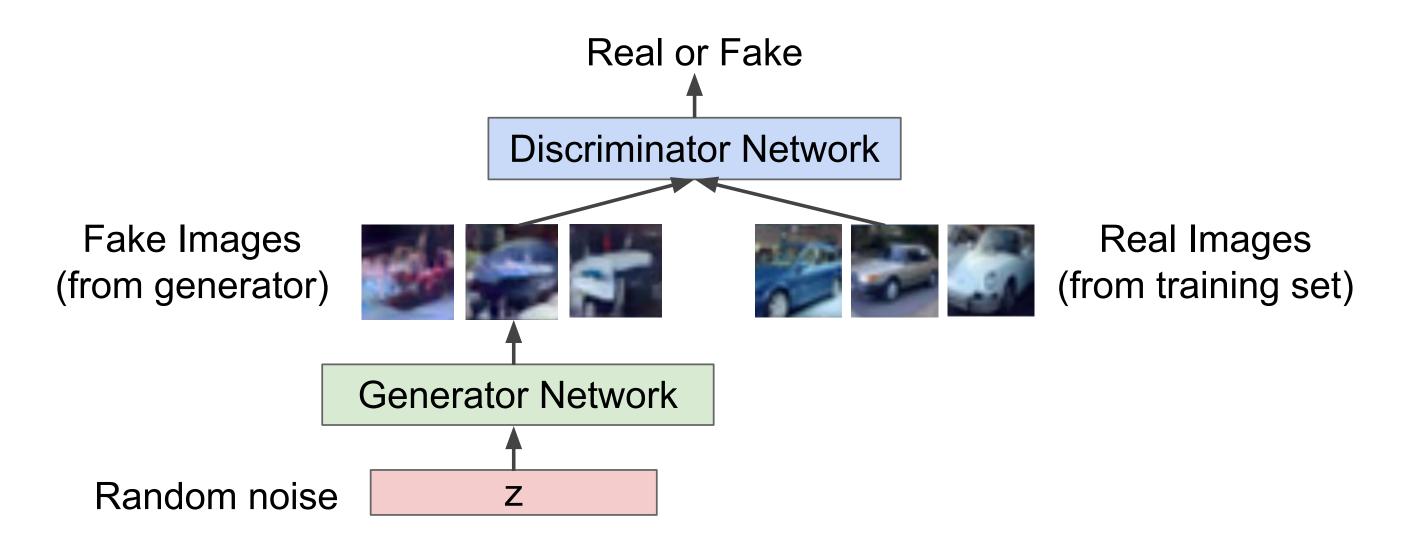
Output: Sample from training distribution



Input: Random noise

Generator network: try to fool the discriminator by generating real-looking images Discriminator network: try to distinguish between real and fake images

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Train jointly in minimax game

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Generator network: try to fool the discriminator by generating real-looking images Discriminator network: try to distinguish between real and fake images

Train jointly in **minimax game**

Discriminator outputs likelihood in (0,1) of real image

Minimax objective function:

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 Discriminator output for for real data x generated fake data G(z)

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Train jointly in minimax game

Discriminator outputs likelihood in (0,1) of real image

Minimax objective function:

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 Discriminator output for for real data x generated fake data G(z)

- Discriminator (θ_d) wants to **maximize objective** such that D(x) is close to 1 (real) and D(G(z)) is close to 0 (fake)
- Generator (θ_g) wants to **minimize objective** such that D(G(z)) is close to 1 (discriminator is fooled into thinking generated G(z) is real)

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Alternate between:

1. Gradient ascent on discriminator

$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

2. Gradient descent on generator

$$\min_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z)))$$

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

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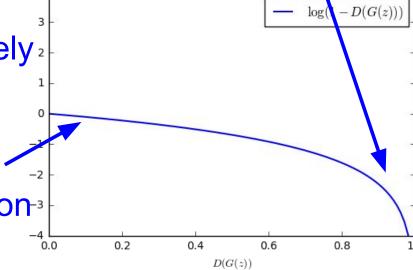
2. Gradient descent on generator

$$\min_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z)))$$

In practice, optimizing this generator objective does not work well!

Gradient signal dominated by region where sample is already good





Minimax objective function:

$$\min_{\theta_a} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Alternate between:

1. Gradient ascent on discriminator

$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

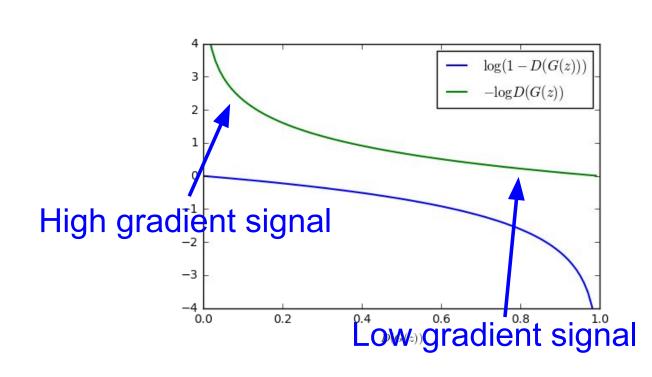
2. Instead: Gradient ascent on generator, different

objective

$$\max_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(D_{\theta_d}(G_{\theta_g}(z)))$$

Instead of minimizing likelihood of discriminator being correct, now maximize likelihood of discriminator being wrong.

Same objective of fooling discriminator, but now higher gradient signal for bad samples => works much better! Standard in practice.



Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Alternate between:

1. Gradient ascent on discriminator

$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right] \text{landscapes helps training,}$$
 is an active area of

2. Instead: Gradient ascent on generator, different

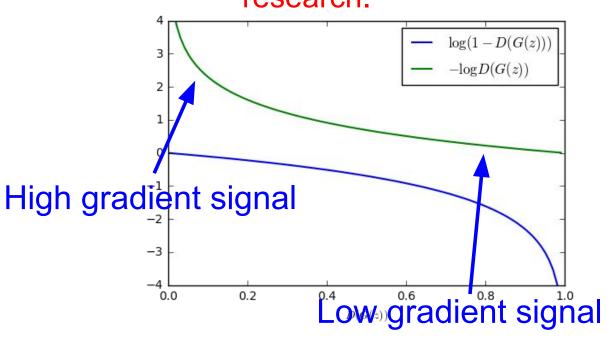
objective

$$\max_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(D_{\theta_d}(G_{\theta_g}(z)))$$

Instead of minimizing likelihood of discriminator being correct, now maximize likelihood of discriminator being wrong.

Same objective of fooling discriminator, but now higher gradient signal for bad samples => works much better! Standard in practice.

Aside: Jointly training two networks is challenging, can be unstable. Choosing objectives with better loss landscapes helps training, is an active area of research.



Putting it together: GAN training algorithm

for number of training iterations do

for k steps do

- Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_g(z)$.
- Sample minibatch of m examples $\{x^{(1)}, \ldots, x^{(m)}\}$ from data generating distribution $p_{\text{data}}(x)$.
- Update the discriminator by ascending its stochastic gradient:

$$\nabla_{\theta_d} \frac{1}{m} \sum_{i=1}^{m} \left[\log D_{\theta_d}(x^{(i)}) + \log(1 - D_{\theta_d}(G_{\theta_g}(z^{(i)}))) \right]$$

end for

- Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_q(z)$.
- Update the generator by ascending its stochastic gradient (improved objective):

$$\nabla_{\theta_g} \frac{1}{m} \sum_{i=1}^m \log(D_{\theta_d}(G_{\theta_g}(z^{(i)})))$$

end for

Putting it together: GAN training algorithm

for number of training iterations do for k steps do

- Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_q(z)$.
- Sample minibatch of m examples $\{x^{(1)}, \dots, x^{(m)}\}$ from data generating distribution $p_{\text{data}}(\boldsymbol{x})$.
- Update the discriminator by ascending its stochastic gradient:

$$\nabla_{\theta_d} \frac{1}{m} \sum_{i=1}^m \left[\log D_{\theta_d}(x^{(i)}) + \log(1 - D_{\theta_d}(G_{\theta_g}(z^{(i)}))) \right]$$

more stable, others use k > 1, no best rule.

Some find k=1

Recent work (e.g. Wasserstein GAN) alleviates this problem, better stability!

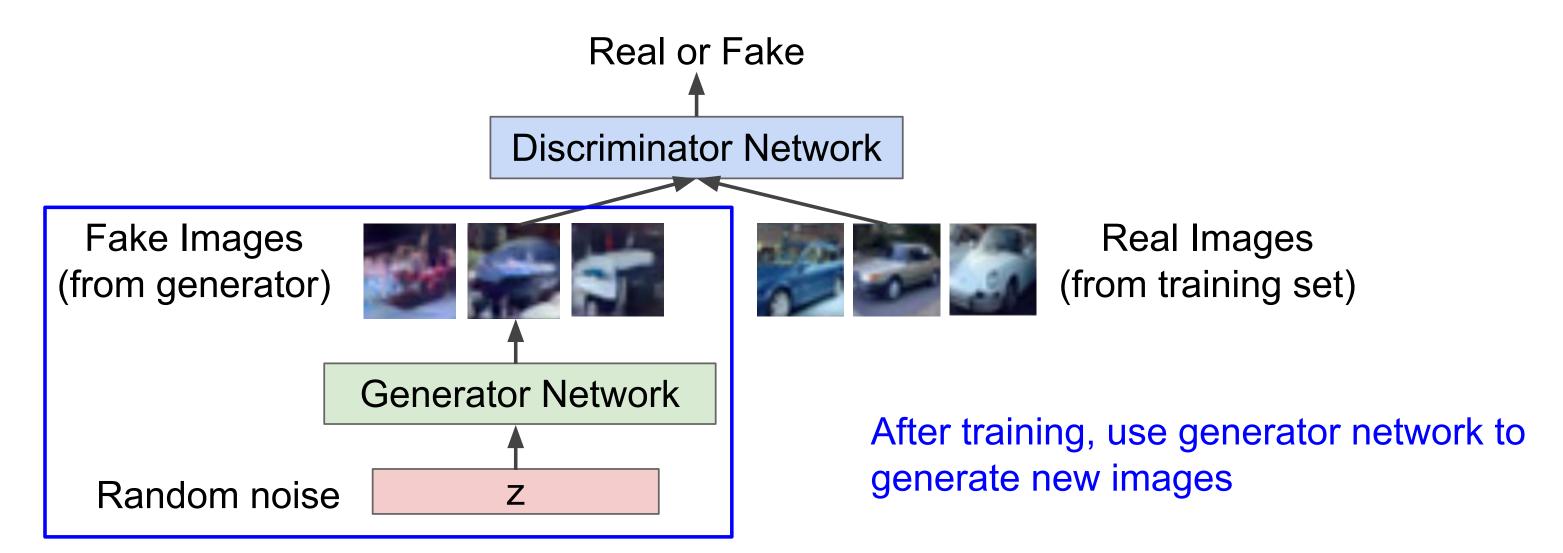
end for

- Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_q(z)$.
- Update the generator by ascending its stochastic gradient (improved objective):

$$\nabla_{\theta_g} \frac{1}{m} \sum_{i=1}^m \log(D_{\theta_d}(G_{\theta_g}(z^{(i)})))$$

end for

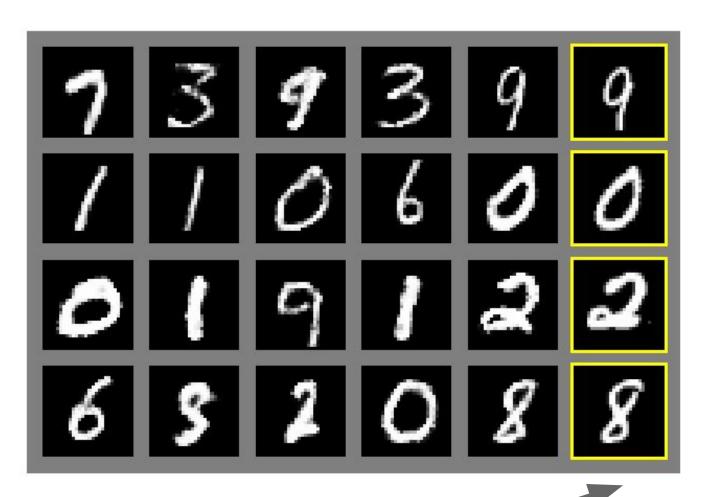
Generator network: try to fool the discriminator by generating real-looking images Discriminator network: try to distinguish between real and fake images

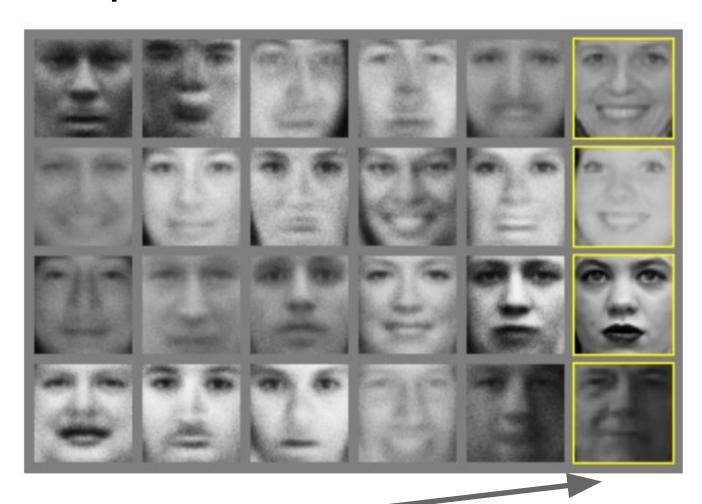


Fake and real images copyright Emily Denton et al. 2015. Reproduced with permission.

Generative Adversarial Nets

Generated samples





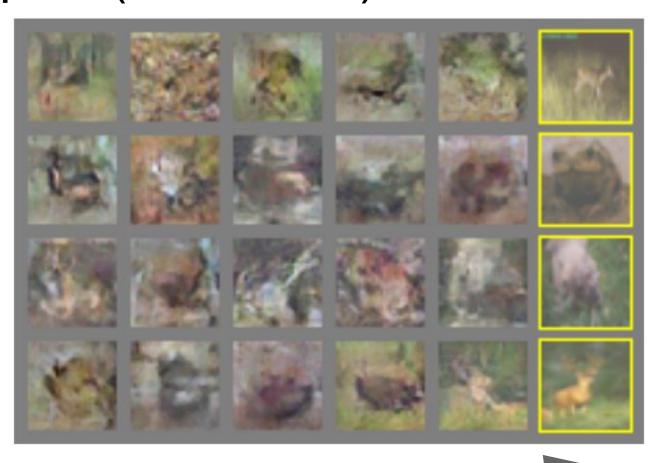
Nearest neighbor from training set

Figures copyright Ian Goodfellow et al., 2014. Reproduced with permission.

Generative Adversarial Nets

Generated samples (CIFAR-10)





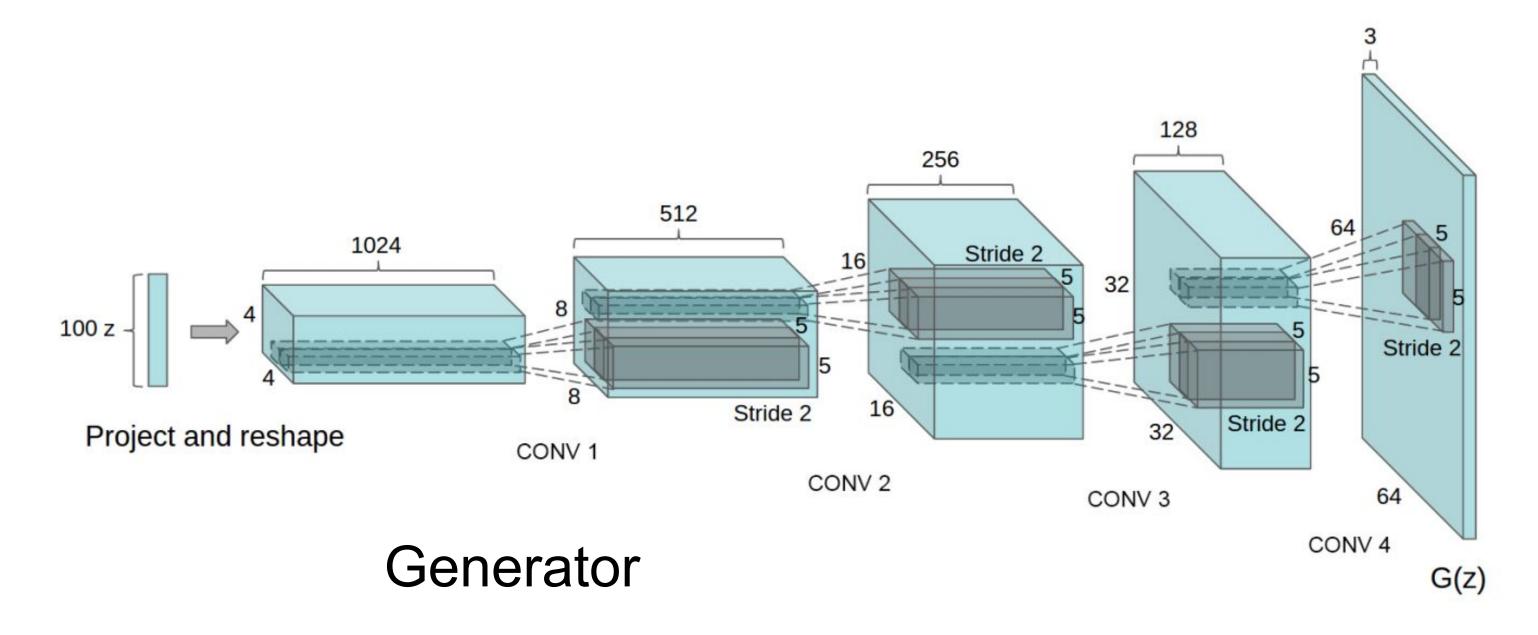
Nearest neighbor from training set

Generator is an upsampling network with fractionally-strided convolutions Discriminator is a convolutional network

Architecture guidelines for stable Deep Convolutional GANs

- Replace any pooling layers with strided convolutions (discriminator) and fractional-strided convolutions (generator).
- Use batchnorm in both the generator and the discriminator.
- Remove fully connected hidden layers for deeper architectures.
- Use ReLU activation in generator for all layers except for the output, which uses Tanh.
- Use LeakyReLU activation in the discriminator for all layers.

Radford et al, "Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks", ICLR 2016



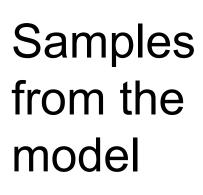
Radford et al, "Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks", ICLR 2016

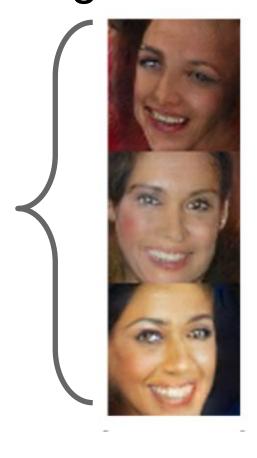
Samples from the model look much better!

Interpolating between random points in laten space

Smiling woman Neutral woman

Neutral man









Neutral man Smiling woman Neutral woman Samples from the model Average Z vectors, do arithmetic

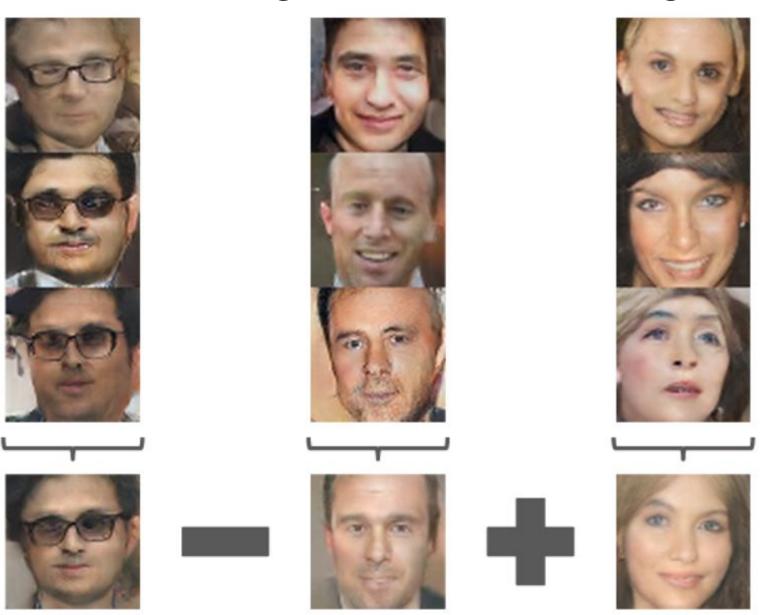
Neutral man Smiling woman Neutral woman Samples from the model Average Z vectors, do arithmetic

Radford et al, ICLR 2016

Smiling Man



Glasses man No glasses woman



Glasses man

No glasses man

No glasses woman







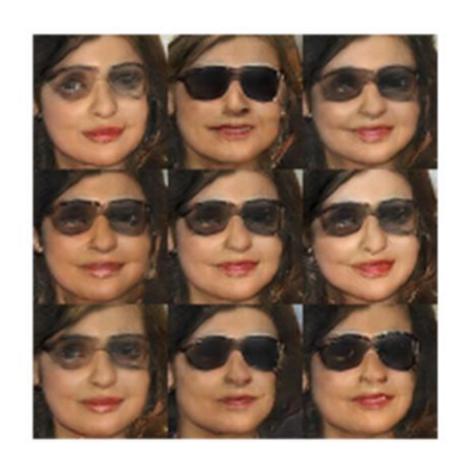












2017: Explosion of GANs

"The GAN Zoo"

- GAN Generative Adversarial Networks
- 3D-GAN Learning a Probabilistic Latent Space of Object Shapes via 3D Generative-Adversarial Modeling
- acGAN Face Aging With Conditional Generative Adversarial Networks
- AC-GAN Conditional Image Synthesis With Auxiliary Classifier GANs
- AdaGAN AdaGAN: Boosting Generative Models
- AEGAN Learning Inverse Mapping by Autoencoder based Generative Adversarial Nets
- AffGAN Amortised MAP Inference for Image Super-resolution
- AL-CGAN Learning to Generate Images of Outdoor Scenes from Attributes and Semantic Layouts
- ALI Adversarially Learned Inference
- AM-GAN Generative Adversarial Nets with Labeled Data by Activation Maximization
- AnoGAN Unsupervised Anomaly Detection with Generative Adversarial Networks to Guide Marker Discovery
- · ArtGAN ArtGAN: Artwork Synthesis with Conditional Categorial GANs
- b-GAN b-GAN: Unified Framework of Generative Adversarial Networks
- · Bayesian GAN Deep and Hierarchical Implicit Models
- BEGAN BEGAN: Boundary Equilibrium Generative Adversarial Networks
- BiGAN Adversarial Feature Learning
- BS-GAN Boundary-Seeking Generative Adversarial Networks
- CGAN Conditional Generative Adversarial Nets
- CaloGAN CaloGAN: Simulating 3D High Energy Particle Showers in Multi-Layer Electromagnetic Calorimeters with Generative Adversarial Networks
- CCGAN Semi-Supervised Learning with Context-Conditional Generative Adversarial Networks
- CatGAN Unsupervised and Semi-supervised Learning with Categorical Generative Adversarial Networks
- CoGAN Coupled Generative Adversarial Networks

- Context-RNN-GAN Contextual RNN-GANs for Abstract Reasoning Diagram Generation
- C-RNN-GAN C-RNN-GAN: Continuous recurrent neural networks with adversarial training
- CS-GAN Improving Neural Machine Translation with Conditional Sequence Generative Adversarial Nets
- CVAE-GAN CVAE-GAN: Fine-Grained Image Generation through Asymmetric Training
- CycleGAN Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks
- DTN Unsupervised Cross-Domain Image Generation
- DCGAN Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks
- DiscoGAN Learning to Discover Cross-Domain Relations with Generative Adversarial Networks
- DR-GAN Disentangled Representation Learning GAN for Pose-Invariant Face Recognition
- DualGAN DualGAN: Unsupervised Dual Learning for Image-to-Image Translation
- EBGAN Energy-based Generative Adversarial Network
- f-GAN f-GAN: Training Generative Neural Samplers using Variational Divergence Minimization
- FF-GAN Towards Large-Pose Face Frontalization in the Wild
- GAWWN Learning What and Where to Draw
- GeneGAN GeneGAN: Learning Object Transfiguration and Attribute Subspace from Unpaired Data
- Geometric GAN Geometric GAN
- GoGAN Gang of GANs: Generative Adversarial Networks with Maximum Margin Ranking
- GP-GAN GP-GAN: Towards Realistic High-Resolution Image Blending
- IAN Neural Photo Editing with Introspective Adversarial Networks
- iGAN Generative Visual Manipulation on the Natural Image Manifold
- IcGAN Invertible Conditional GANs for image editing
- ID-CGAN Image De-raining Using a Conditional Generative Adversarial Network
- Improved GAN Improved Techniques for Training GANs
- InfoGAN InfoGAN: Interpretable Representation Learning by Information Maximizing Generative Adversarial Nets
- LAGAN Learning Particle Physics by Example: Location-Aware Generative Adversarial Networks for Physics Synthesis
- LAPGAN Deep Generative Image Models using a Laplacian Pyramid of Adversarial Networks

https://github.com/hindupuravinash/the-gan-zoo

2017: Explosion of GANs See also: https://github.com/soumith/ganhacks for tips and tricks for trainings GANs

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2017: Explosion of GANs

Source->Target domain transfer



CycleGAN. Zhu et al. 2017.

Text -> Image Synthesis

this small bird has a pink breast and crown, and black almost all black with a red primaries and secondaries.

this magnificent fellow is crest, and white cheek patch.





Reed et al. 2017.

Many GAN applications



Pix2pix. Isola 2017. Many examples at https://phillipi.github.io/pix2pix/

GANs

Don't work with an explicit density function

Take game-theoretic approach: learn to generate from training distribution through 2-player game

Pros:

Beautiful, state-of-the-art samples!

Cons:

- Trickier / more unstable to train
- Can't solve inference queries such as p(x), p(z|x)

Active areas of research:

- Better loss functions, more stable training (Wasserstein GAN, LSGAN, many others)
- Conditional GANs, GANs for all kinds of applications

Recap

Generative Models

- PixeIRNN and PixeICNN Explicit density model, optimizes exact likelihood, good samples. But inefficient sequential generation.
- Variational Autoencoders (VAE) Optimize variational lower bound on likelihood. Useful latent representation, inference queries. But current sample quality not the best.
- Generative Adversarial Networks (GANs) Game-theoretic approach, best samples!

 But can be tricky and unstable to train,
 no inference queries.