

# Lecture 7: Tricks + Word Embeddings

Alan Ritter

(many slides from Greg Durrett)

# Recall: Feedforward NNs

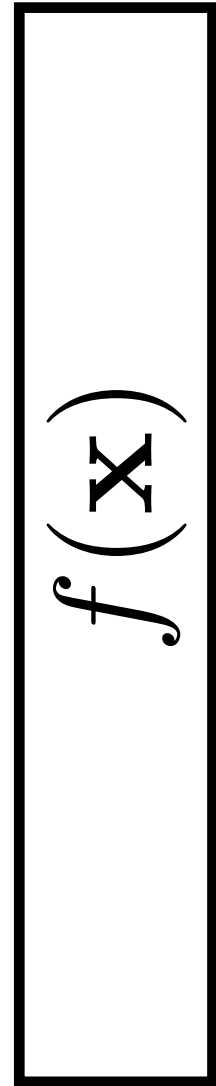
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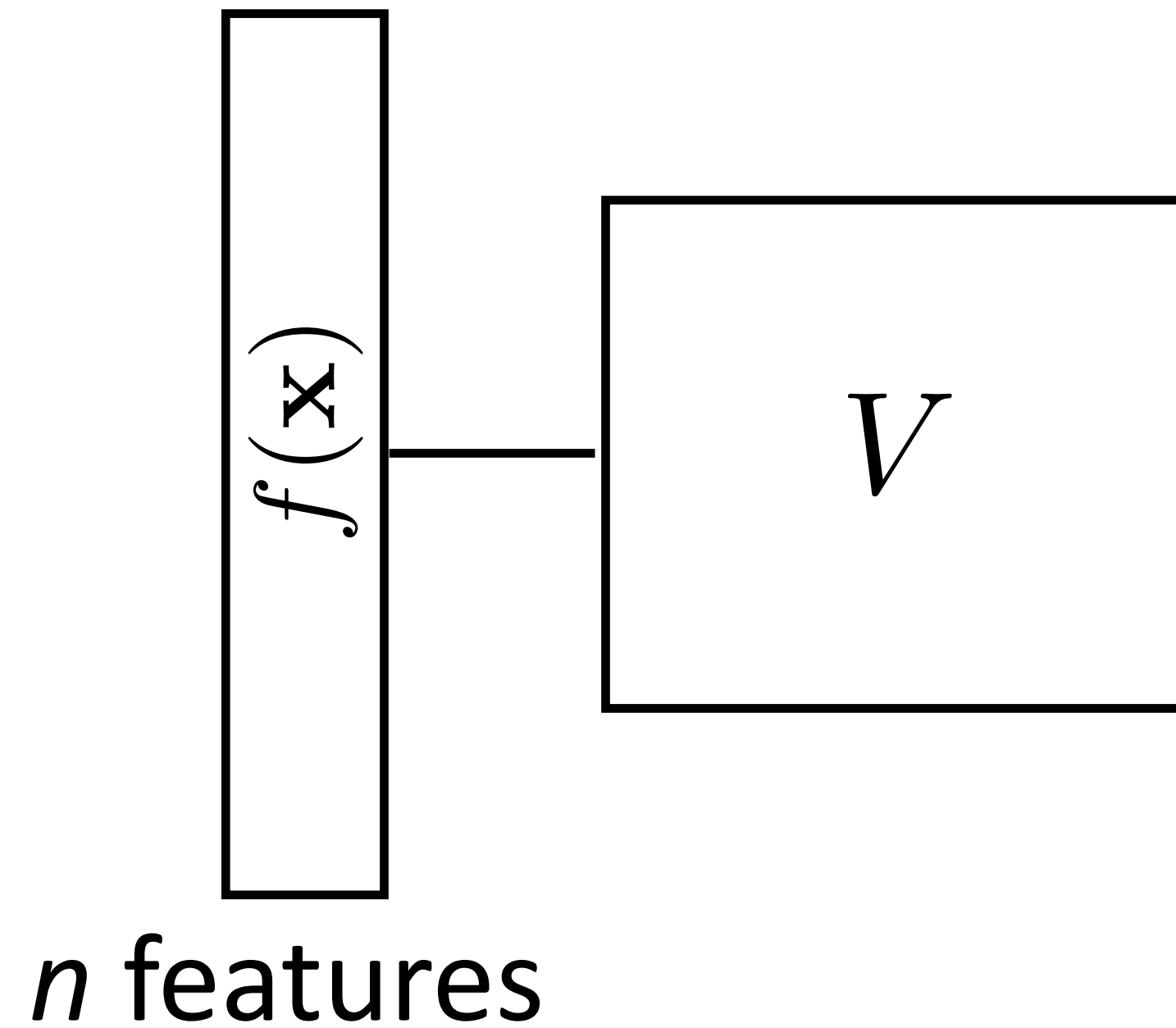


$n$  features

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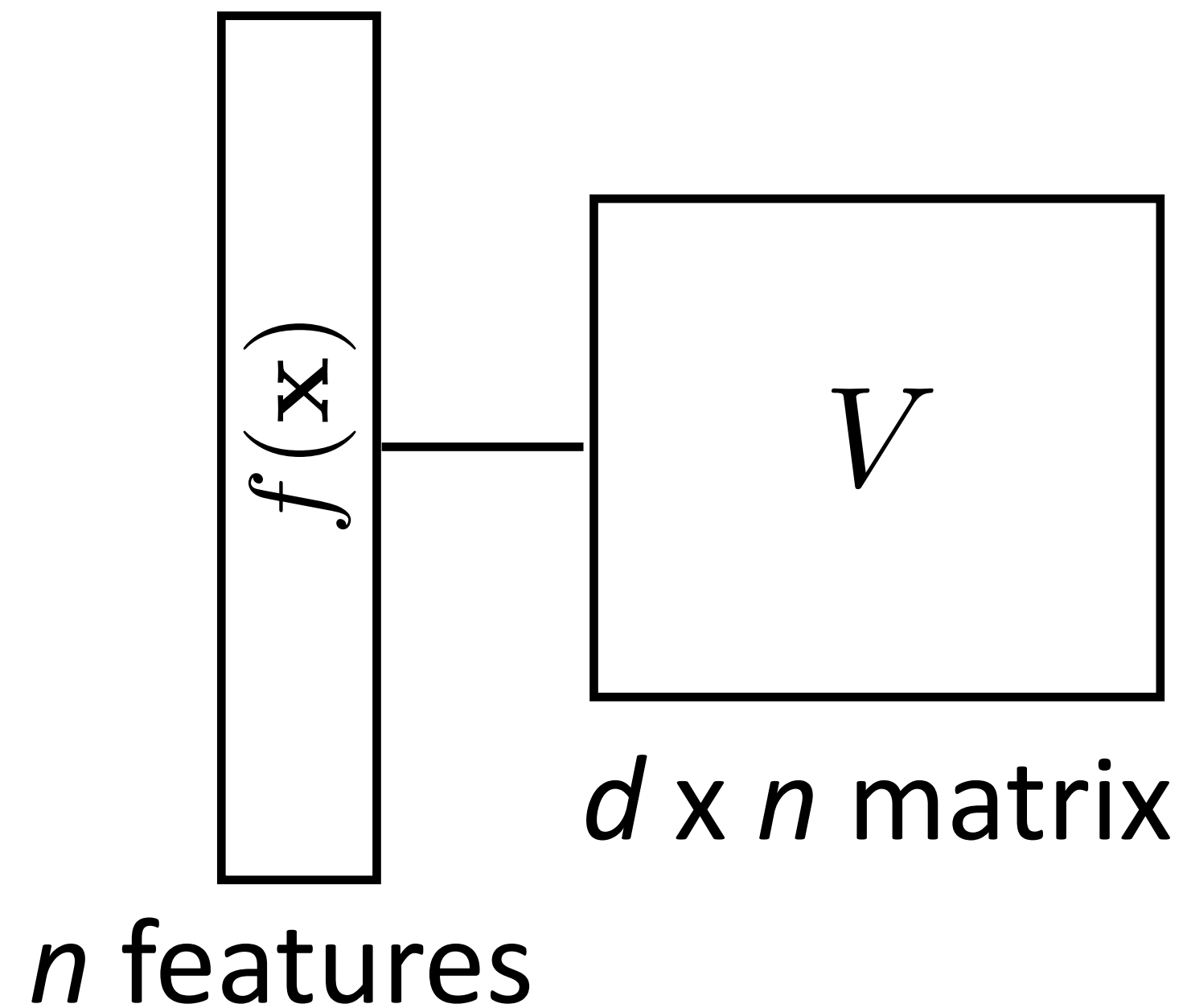
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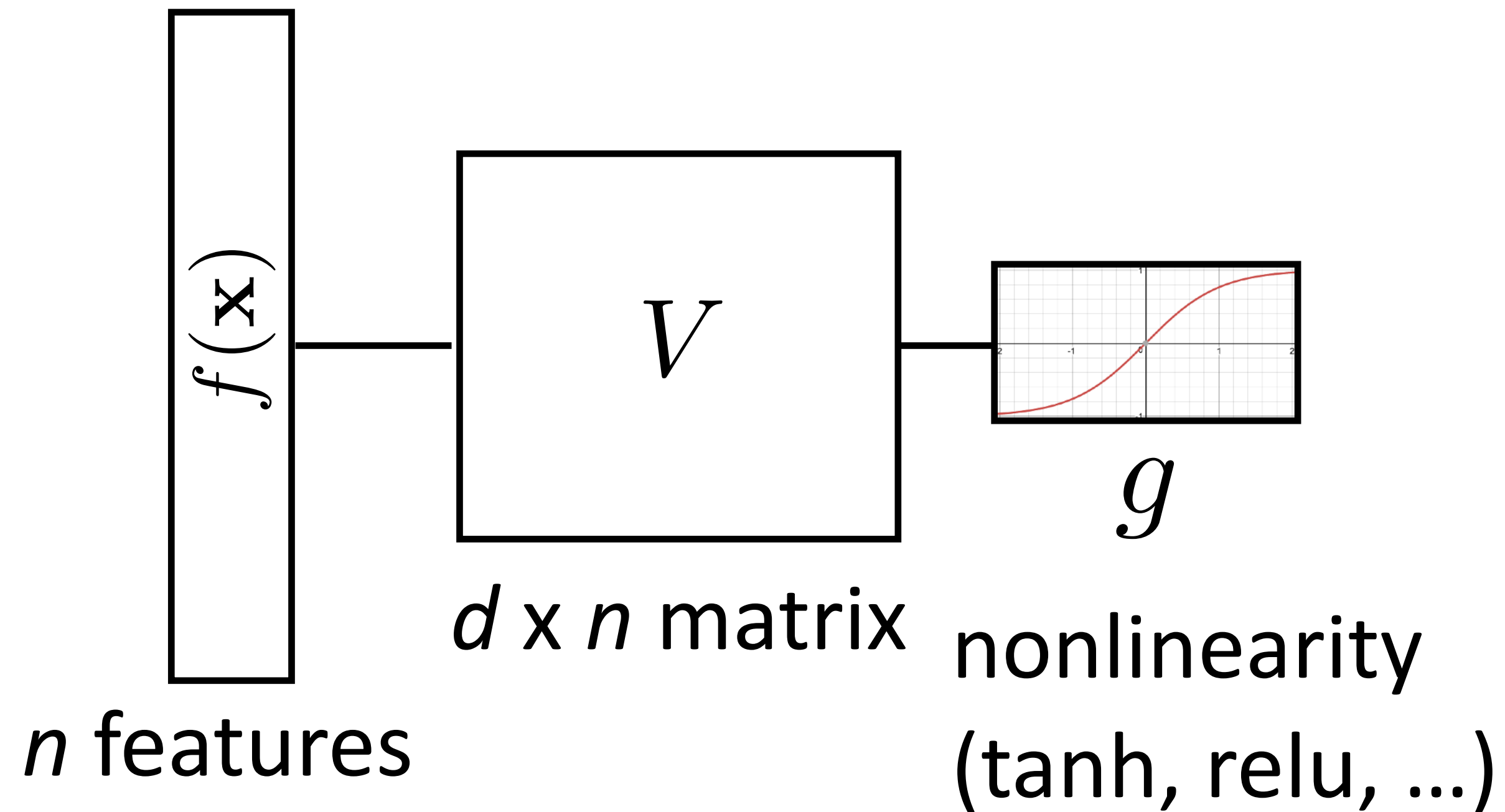
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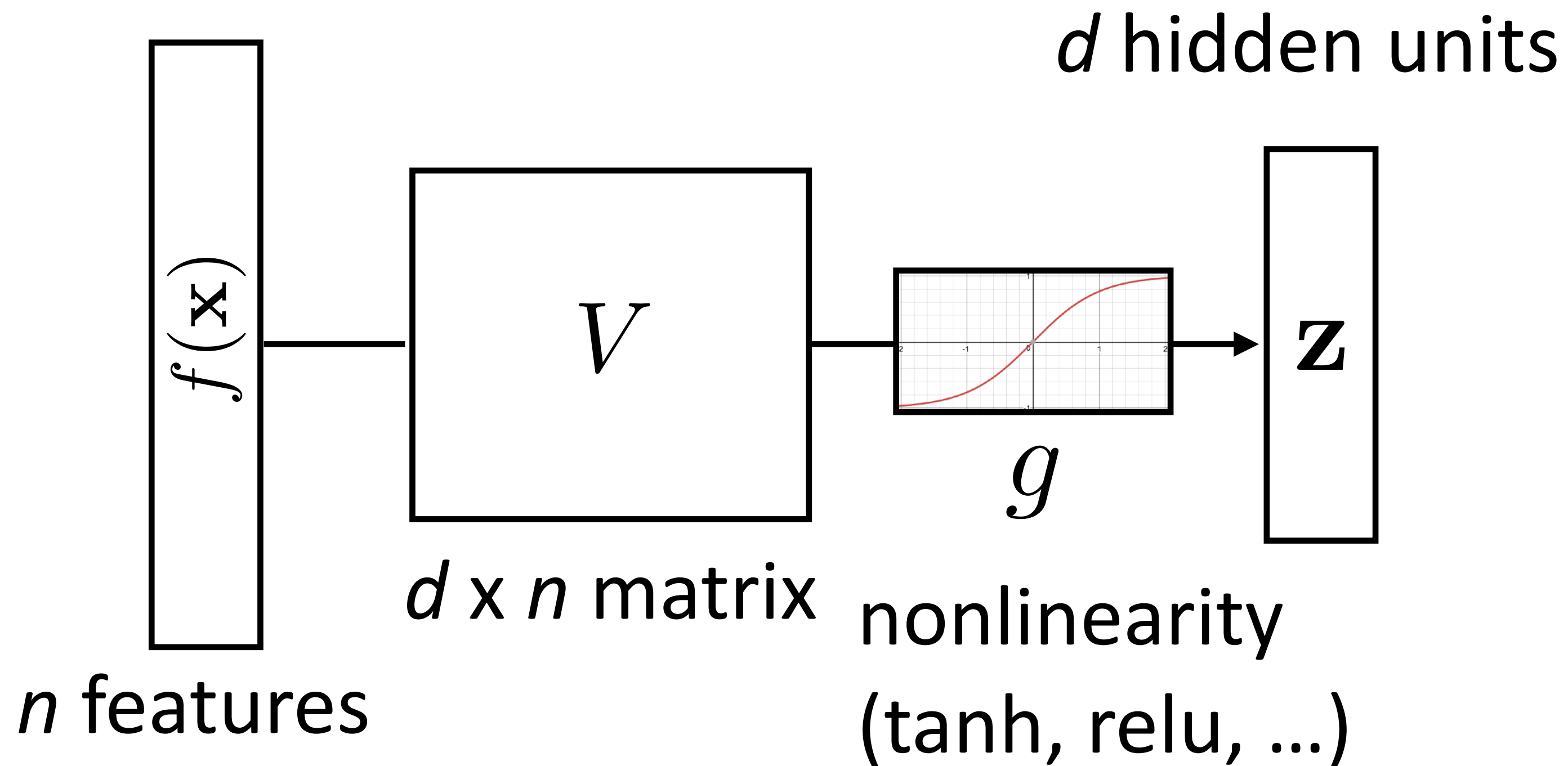
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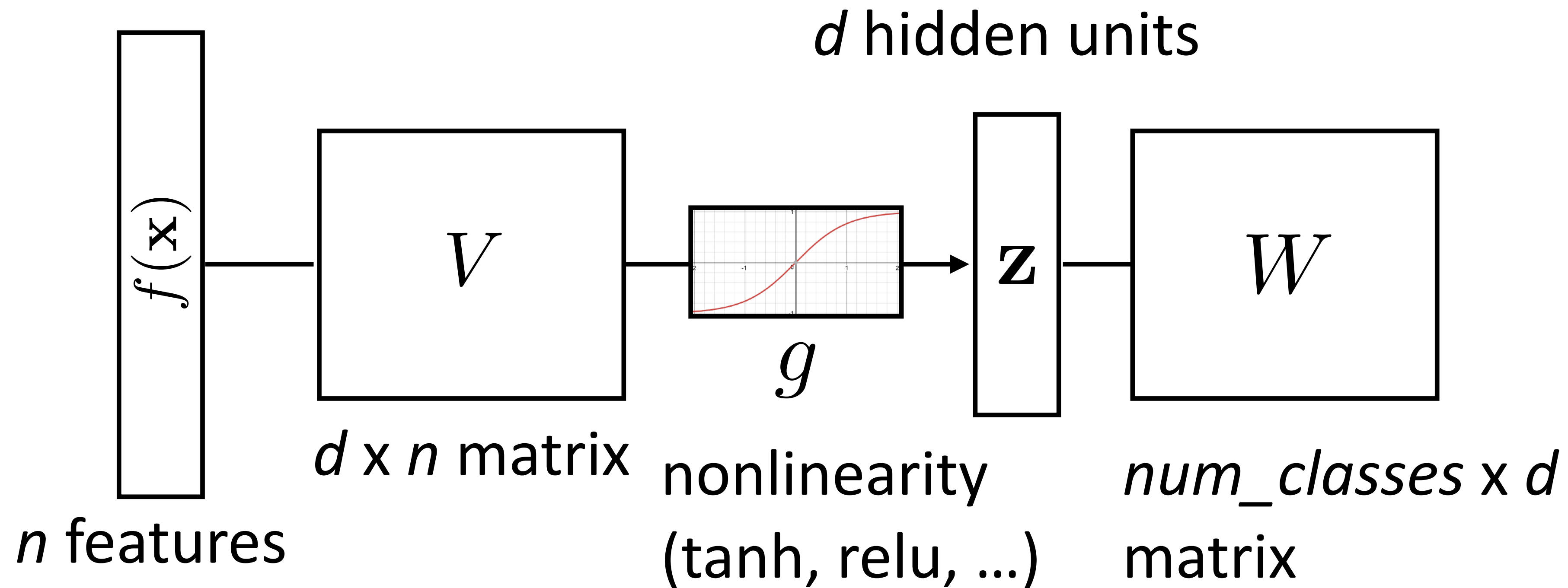
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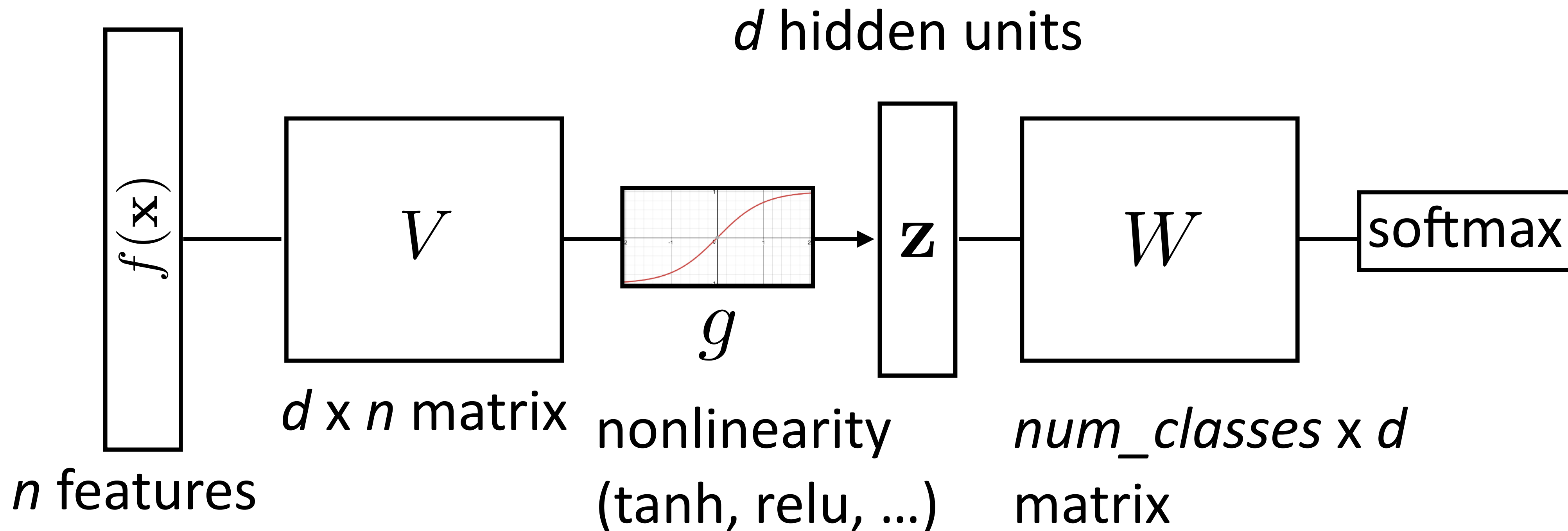




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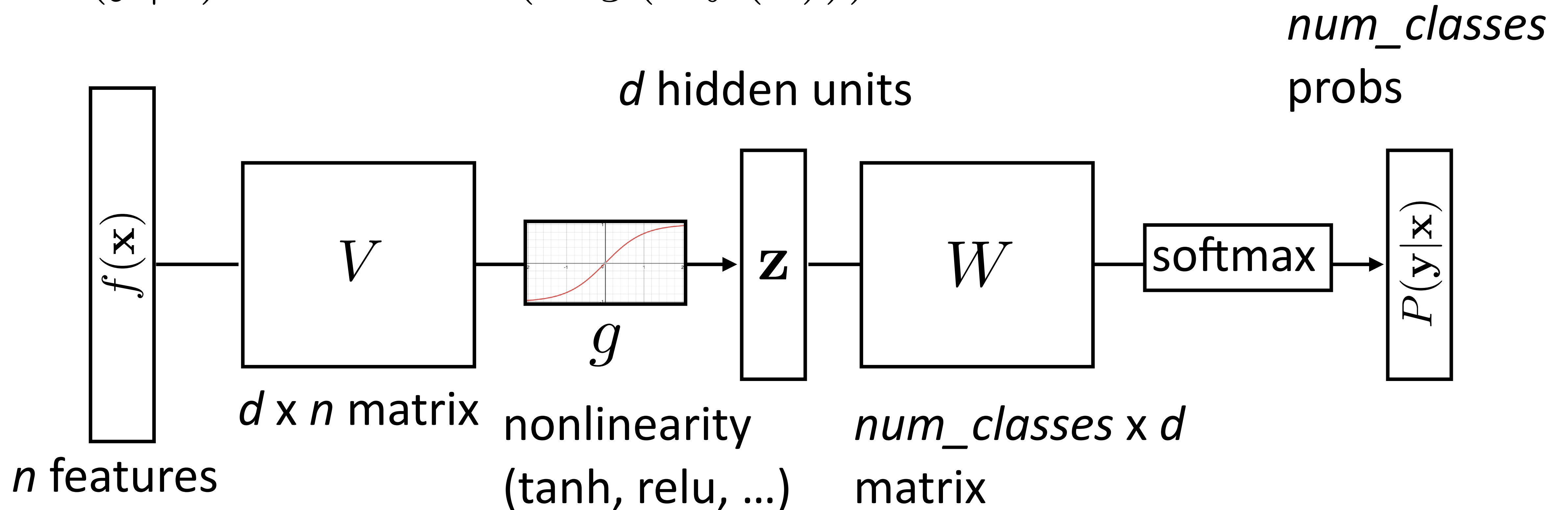
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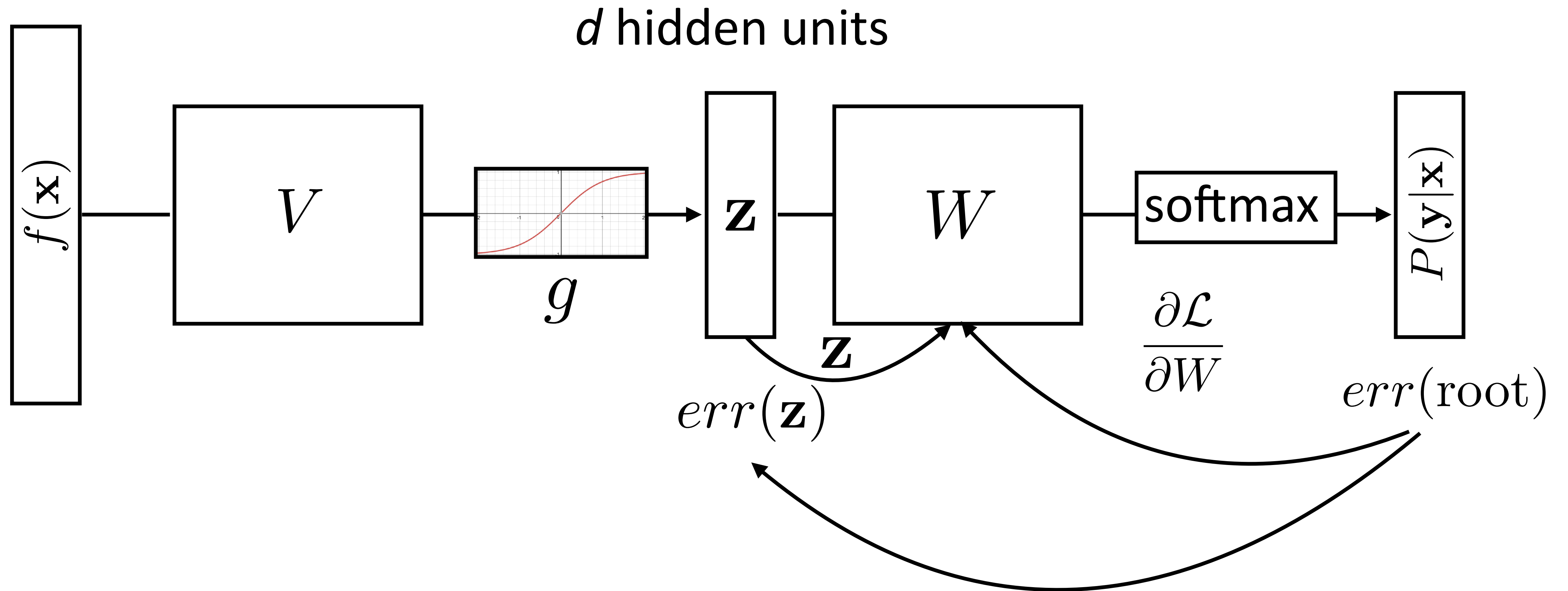
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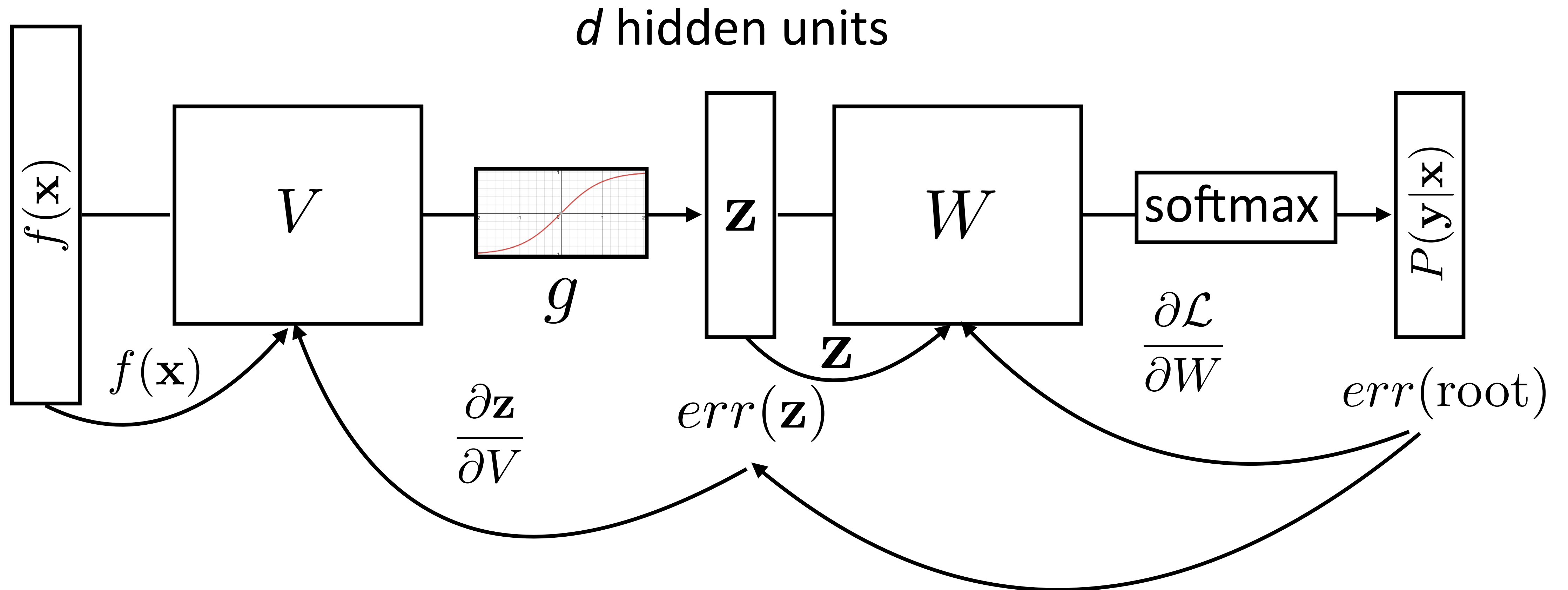
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# This Lecture

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- ▶ Training
- ▶ Word representations
- ▶ word2vec/GloVe
- ▶ Evaluating word embeddings

# Training Tips

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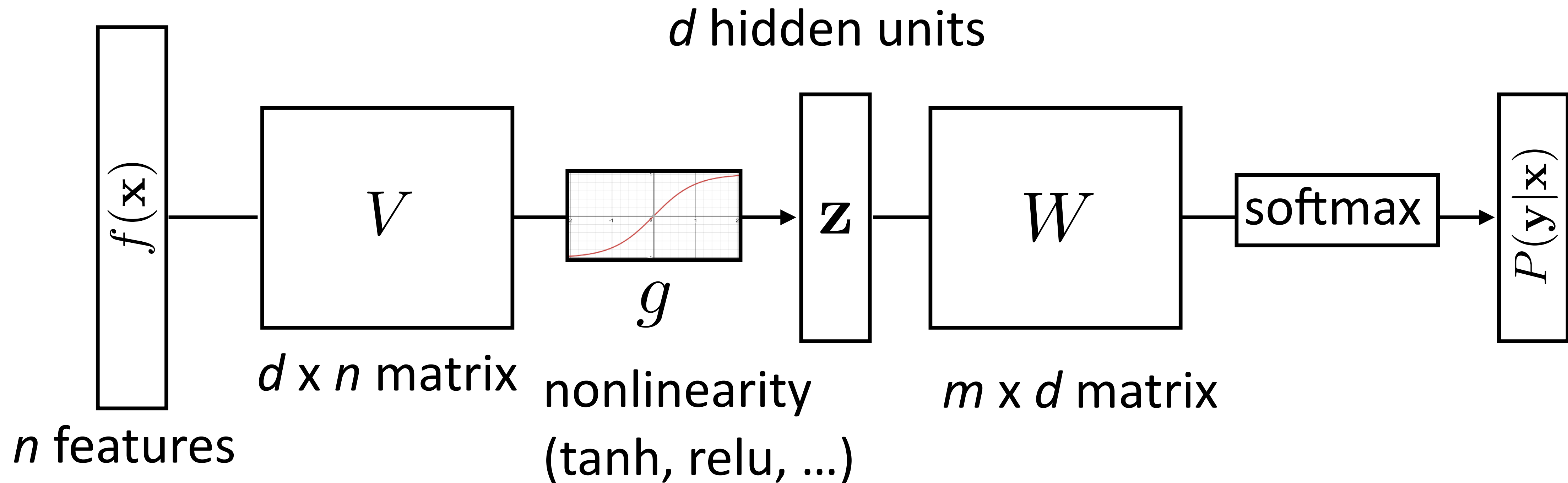
- ▶ Basic formula: compute gradients on batch, use first-order opt. method
- ▶ How to initialize? How to regularize? What optimizer to use?
- ▶ This lecture: some practical tricks. Take deep learning or optimization courses to understand this further



# How does initialization affect learning?

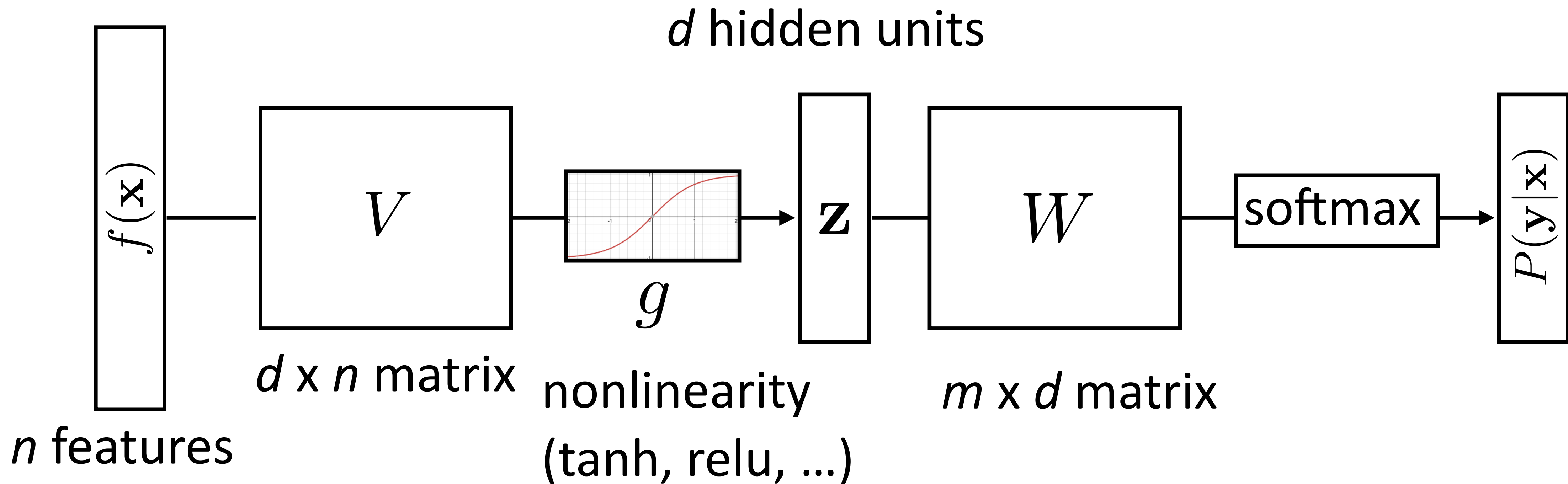
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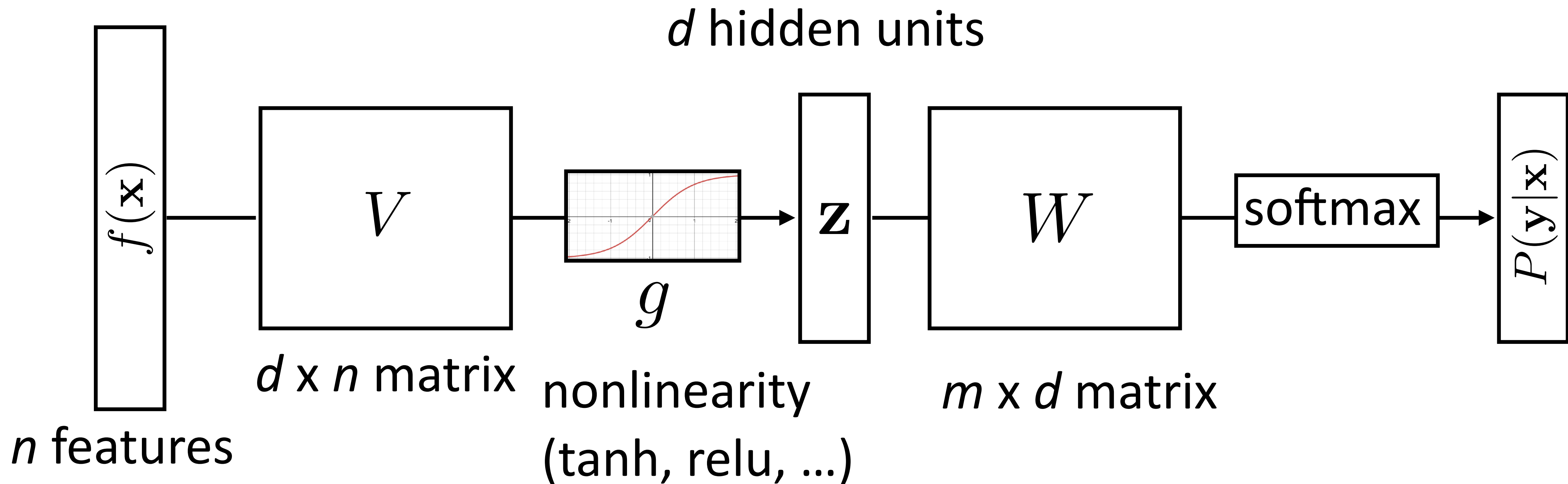
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- ▶ How do we initialize  $V$  and  $W$ ? What consequences does this have?
- ▶ *Nonconvex* problem, so initialization matters!

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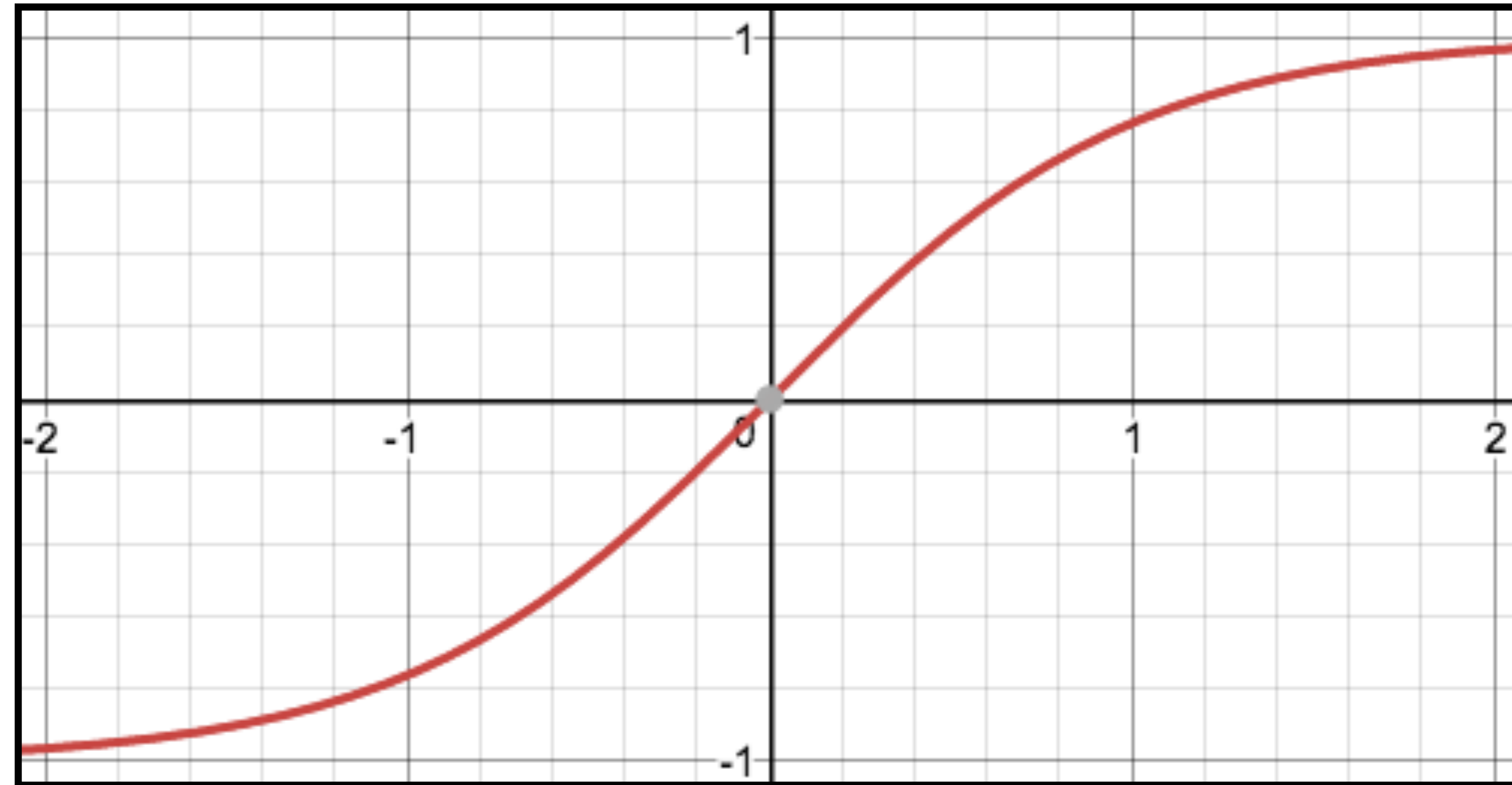
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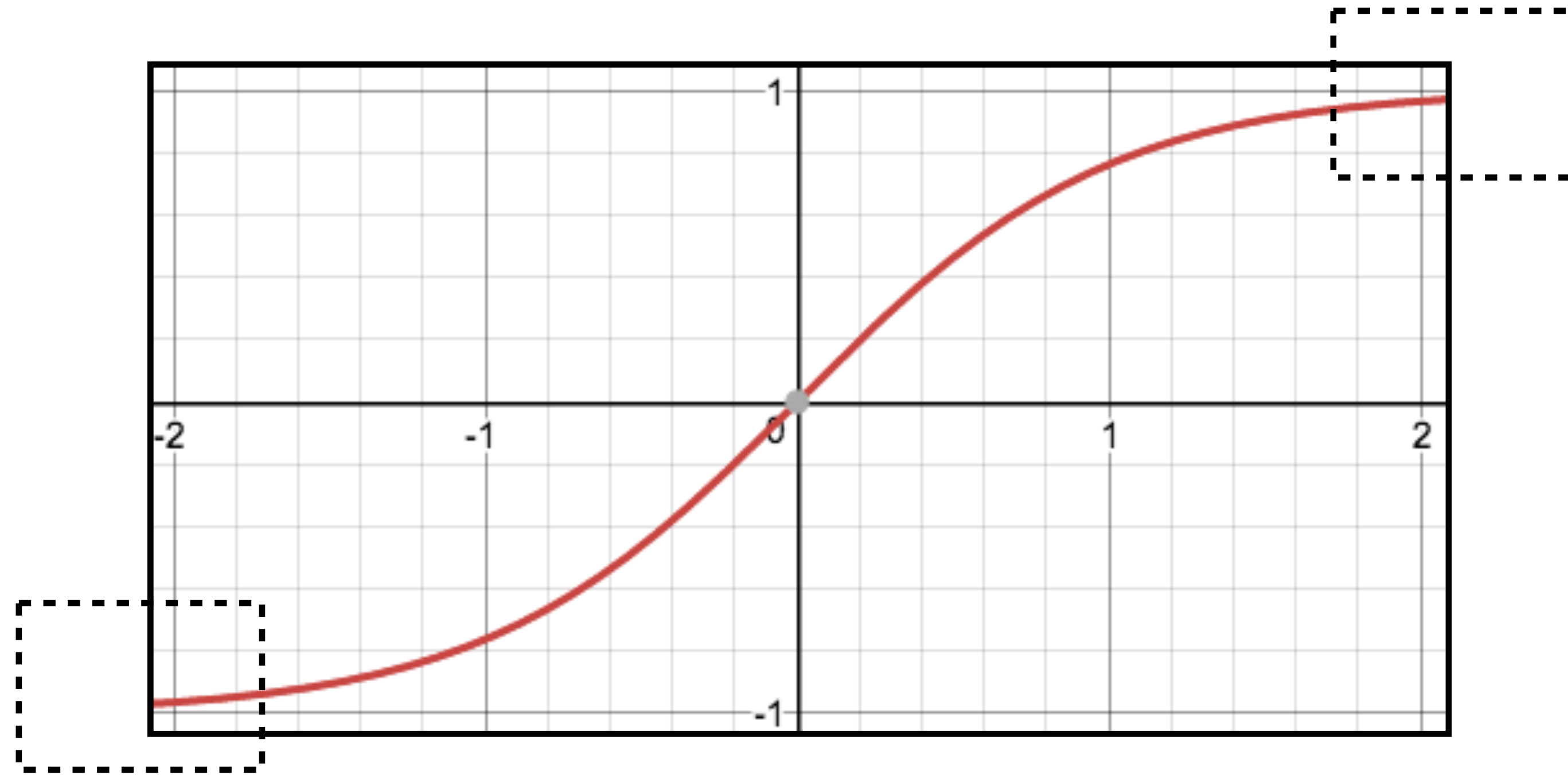
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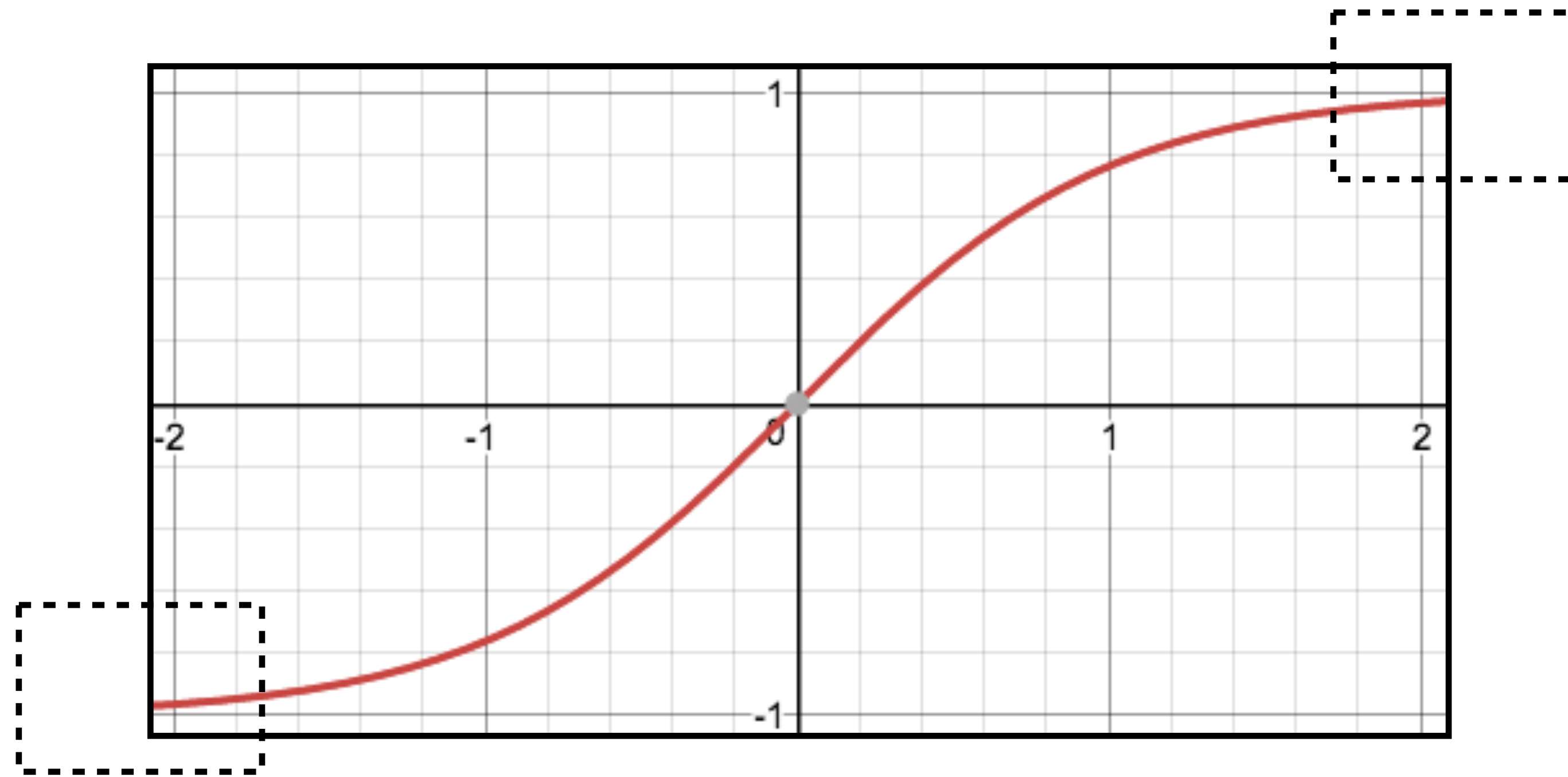




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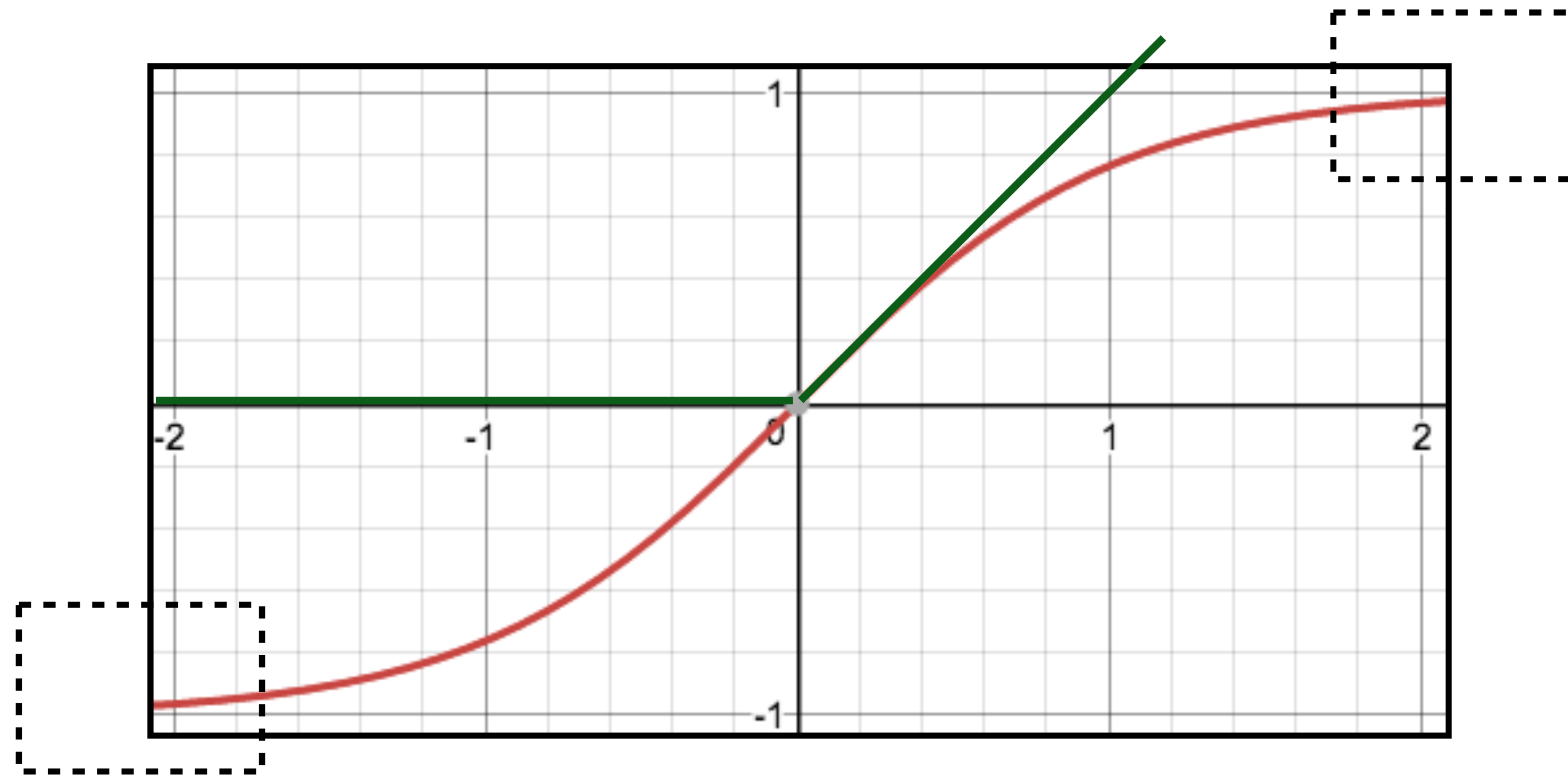
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- ▶ If cell activations are too large in absolute value, gradients are small
- ▶ **ReLU**: larger dynamic range (all positive numbers), but can produce big values, can break down if everything is too negative

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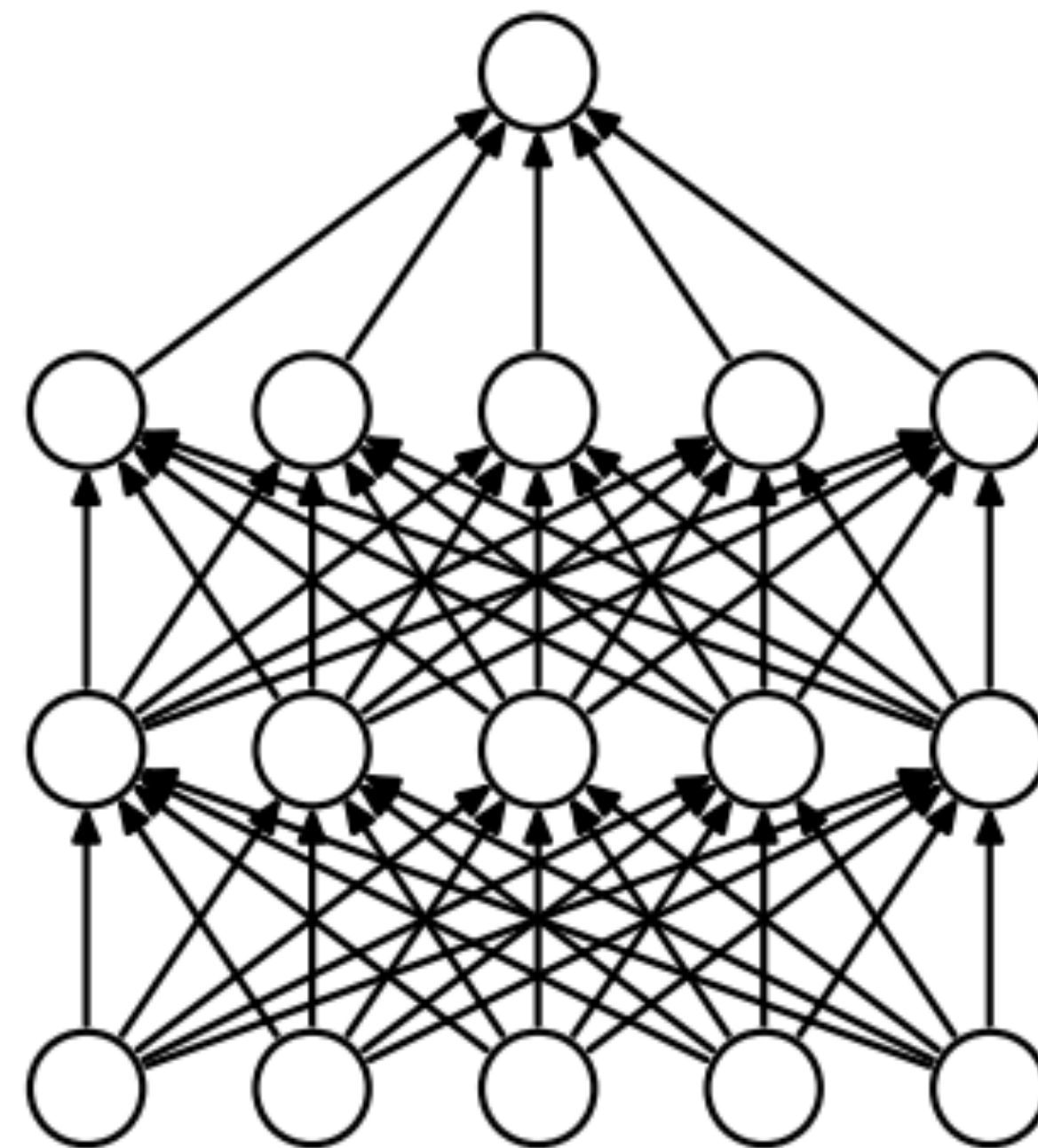
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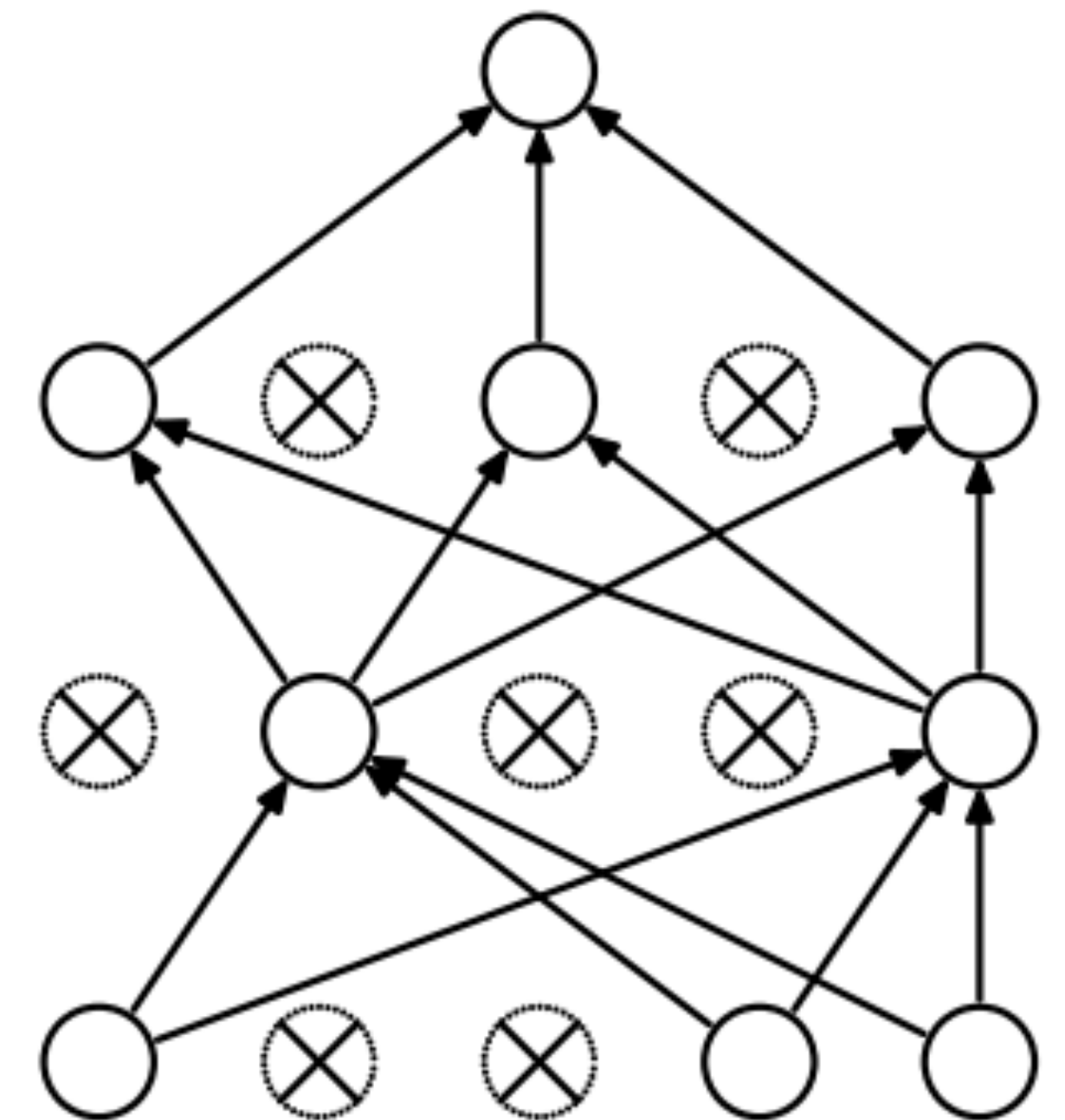
▶ Batch normalization (Ioffe and Szegedy, 2015): periodically shift+rescale each layer to have mean 0 and variance 1 over a batch (useful if net is deep)

# Dropout

- ▶ Probabilistically zero out parts of the network during training to prevent overfitting, use whole network at test time



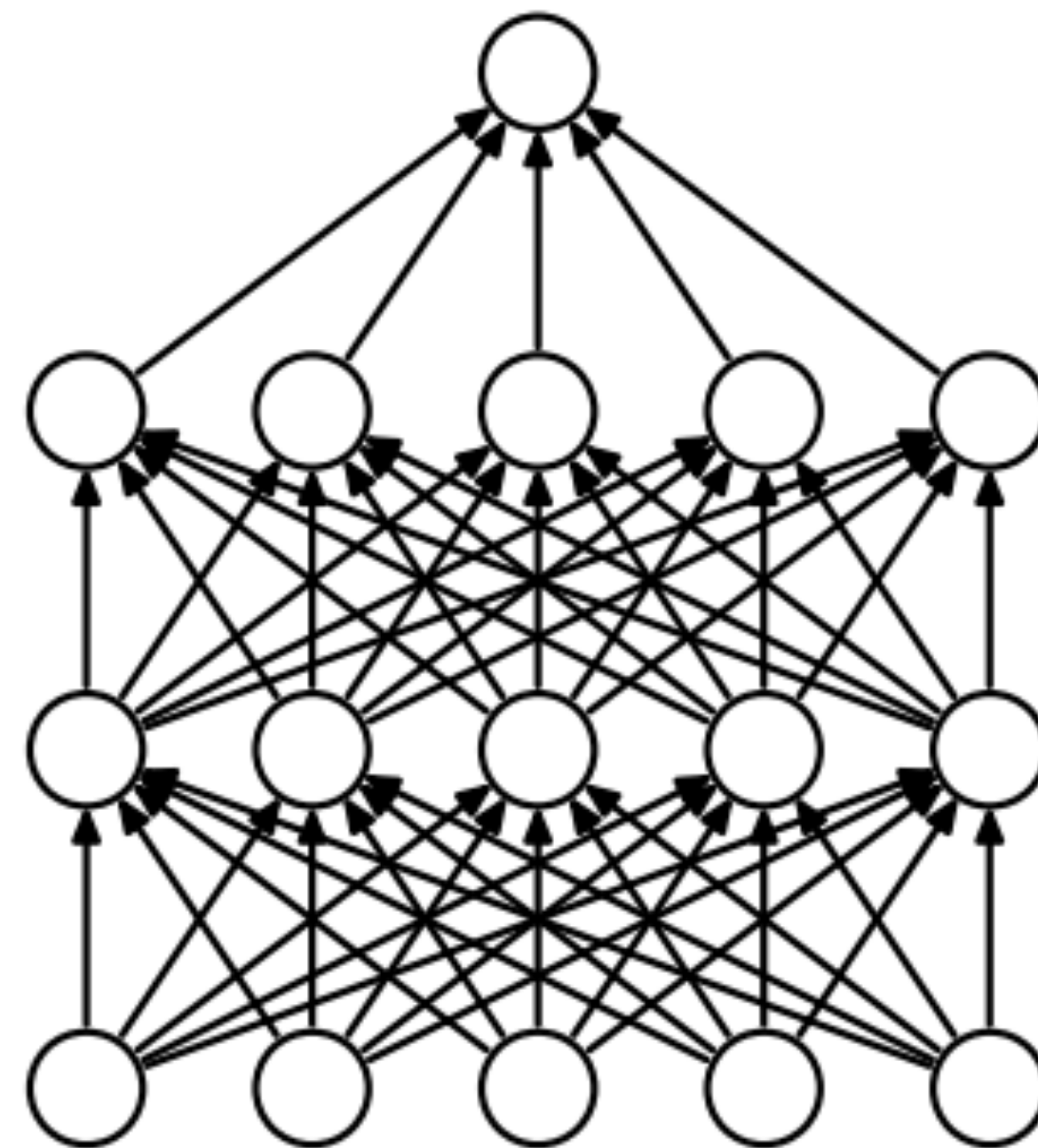
(a) Standard Neural Net



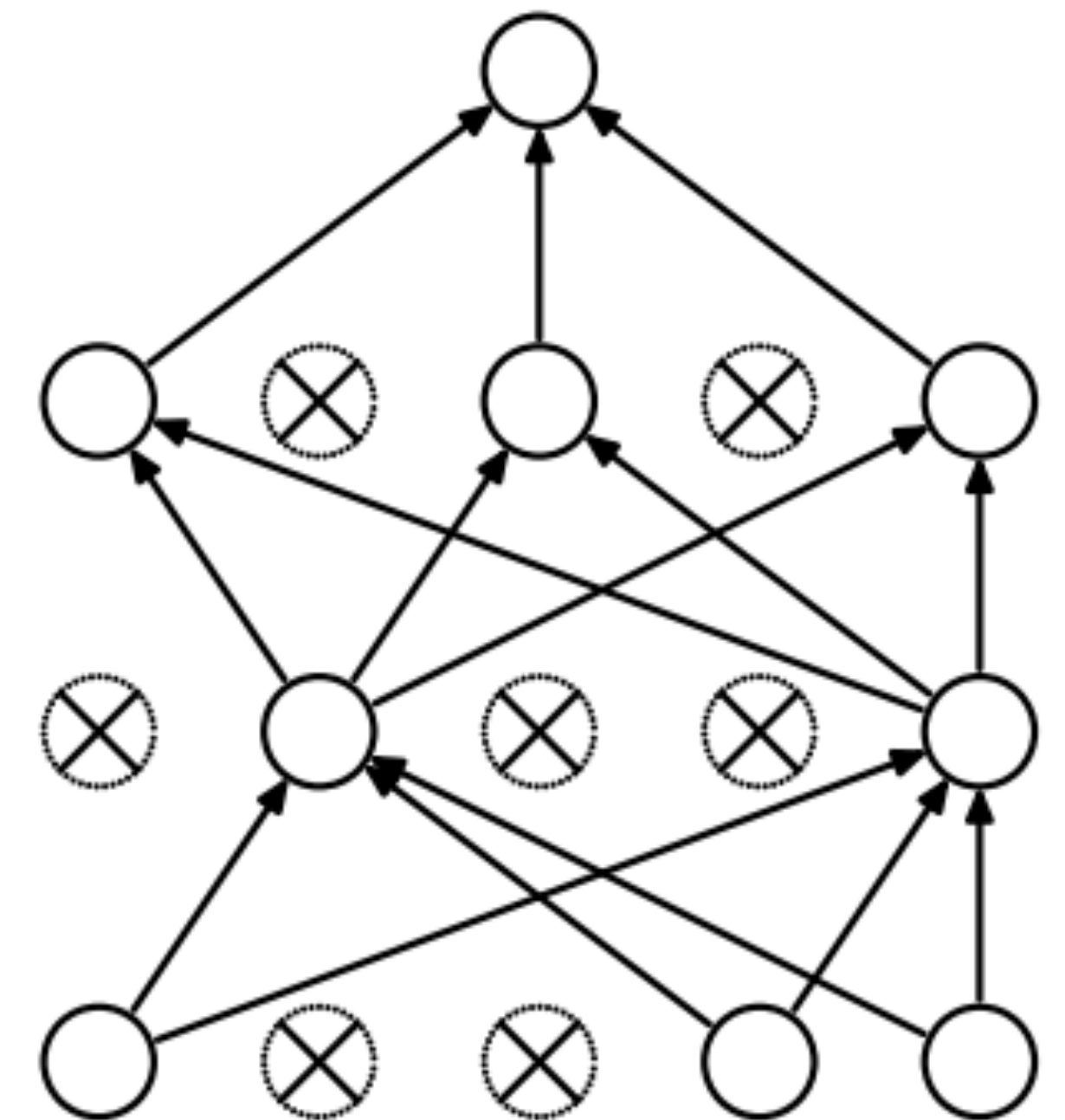
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- ▶ Probabilistically zero out parts of the network during training to prevent overfitting, use whole network at test time
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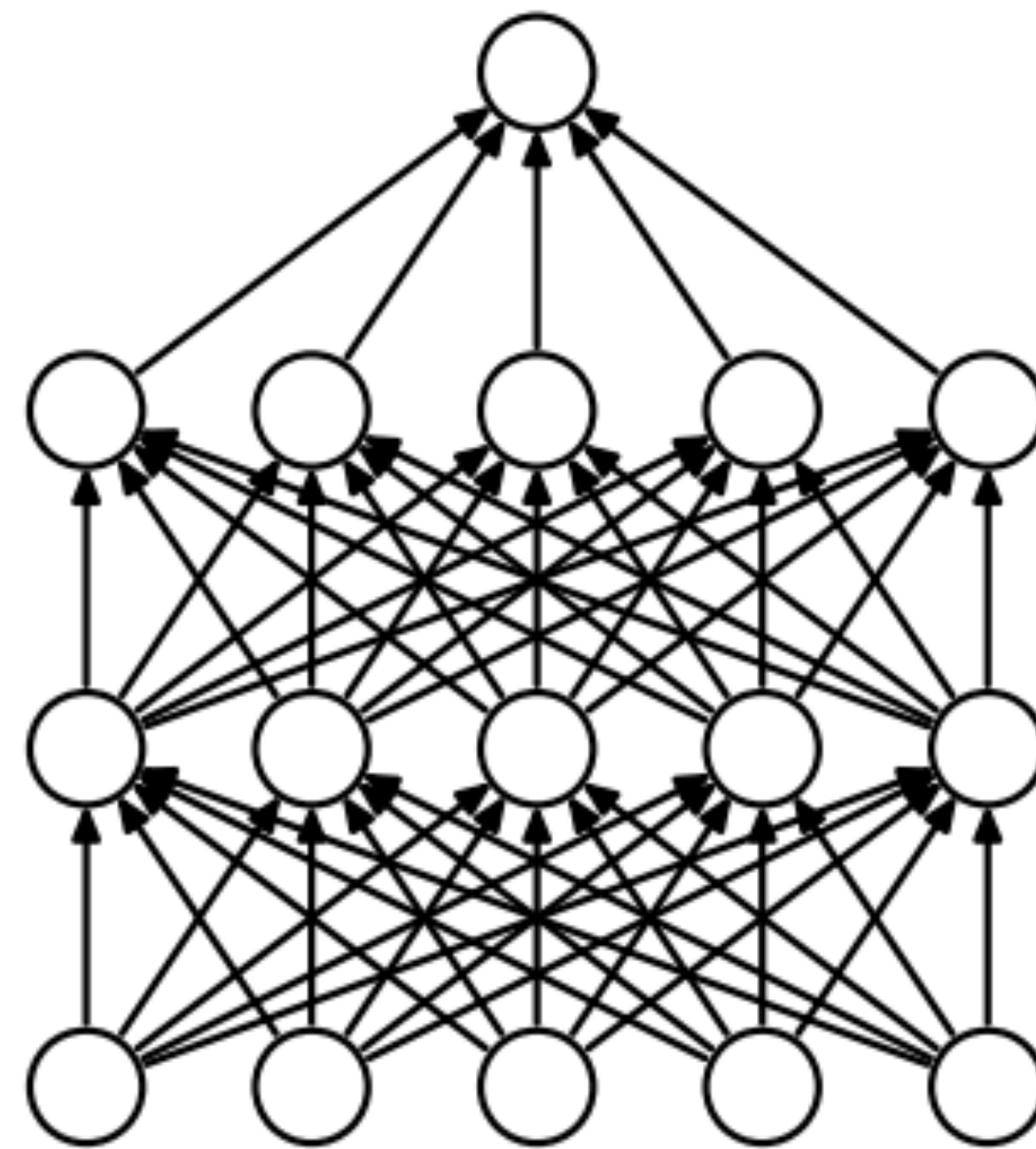
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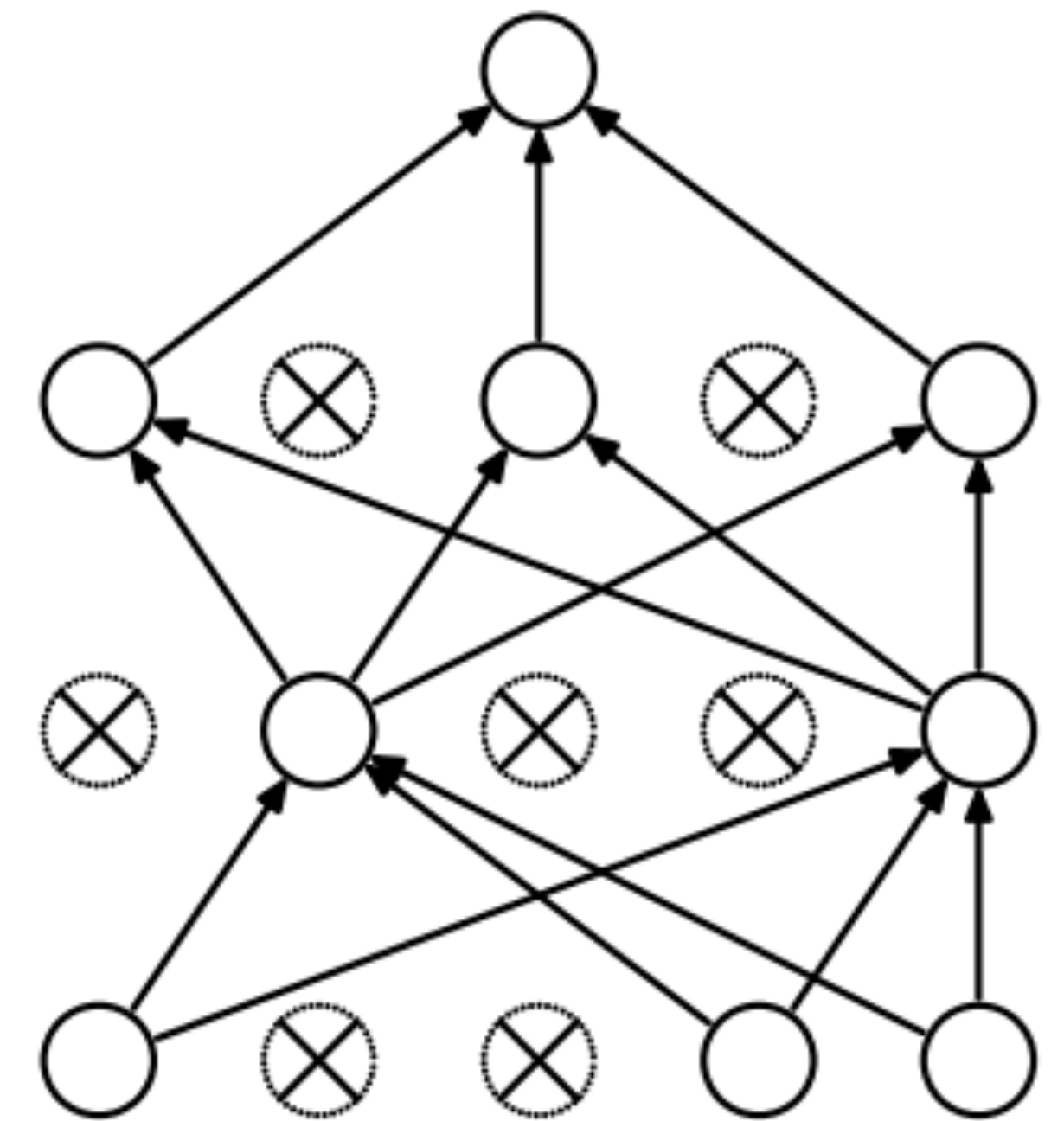
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- ▶ Probabilistically zero out parts of the network during training to prevent overfitting, use whole network at test time
- ▶ Form of stochastic regularization
- ▶ Similar to benefits of ensembling: network needs to be robust to missing signals, so it has redundancy



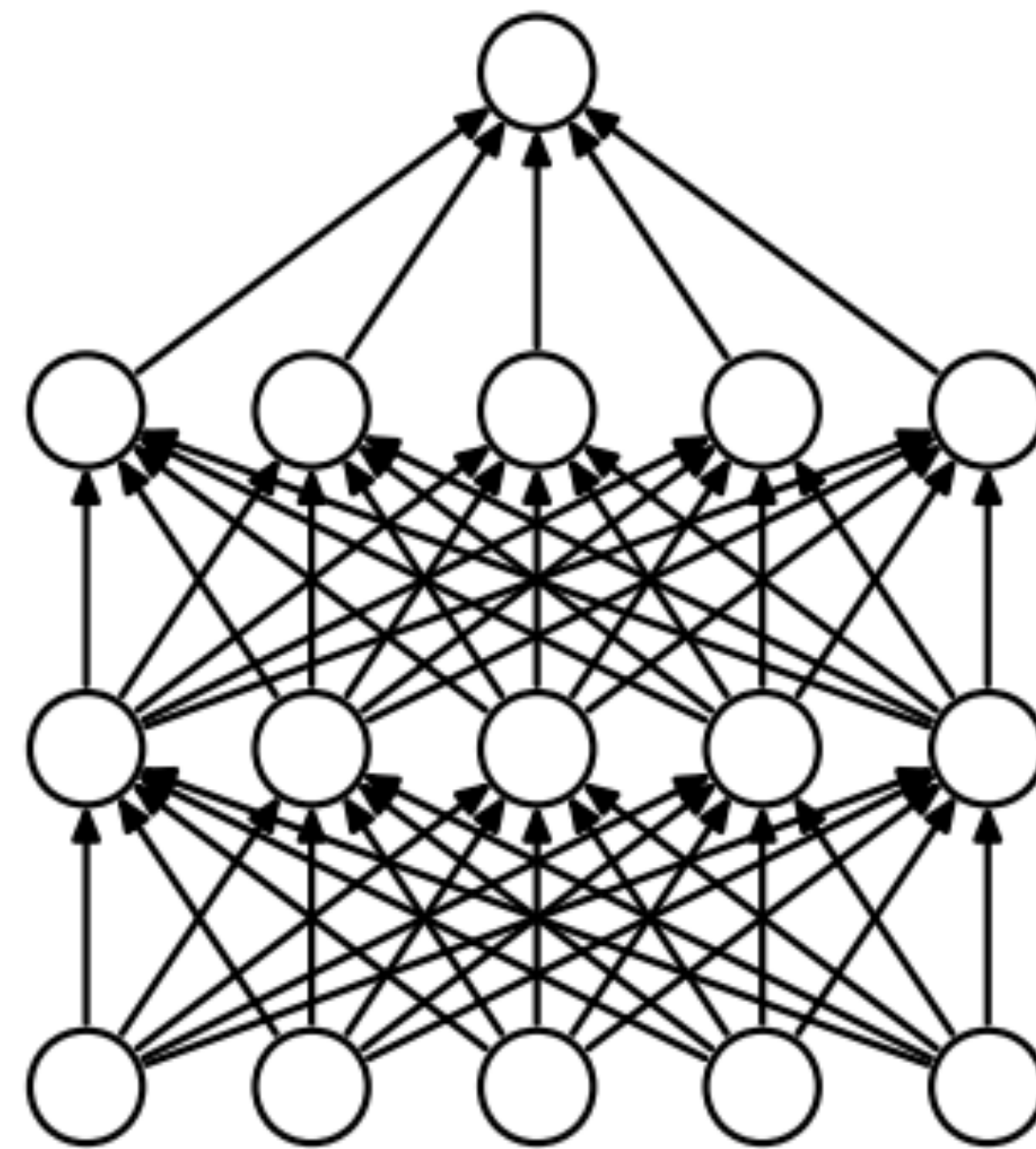
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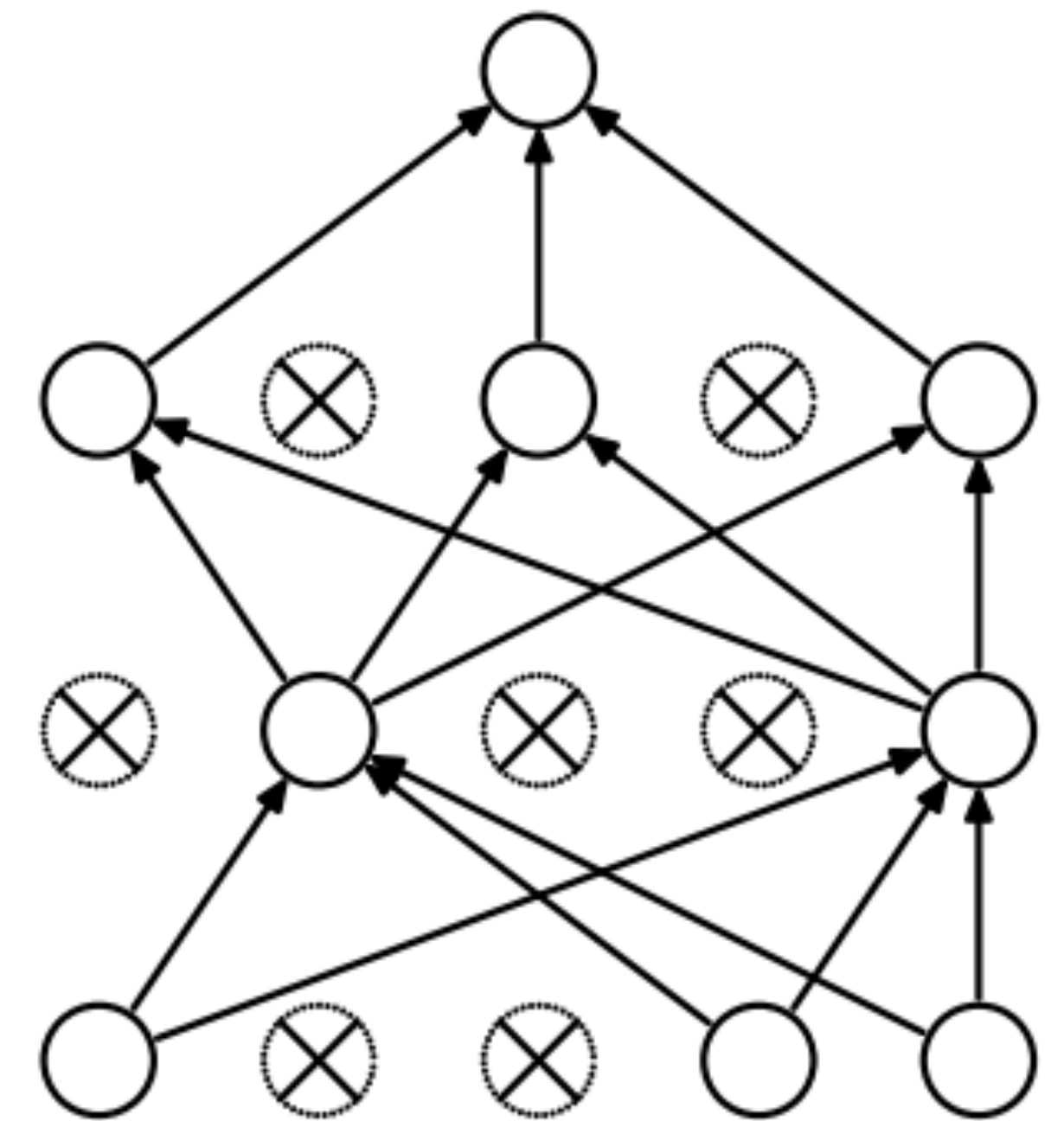
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- ▶ One line in Pytorch/Tensorflow



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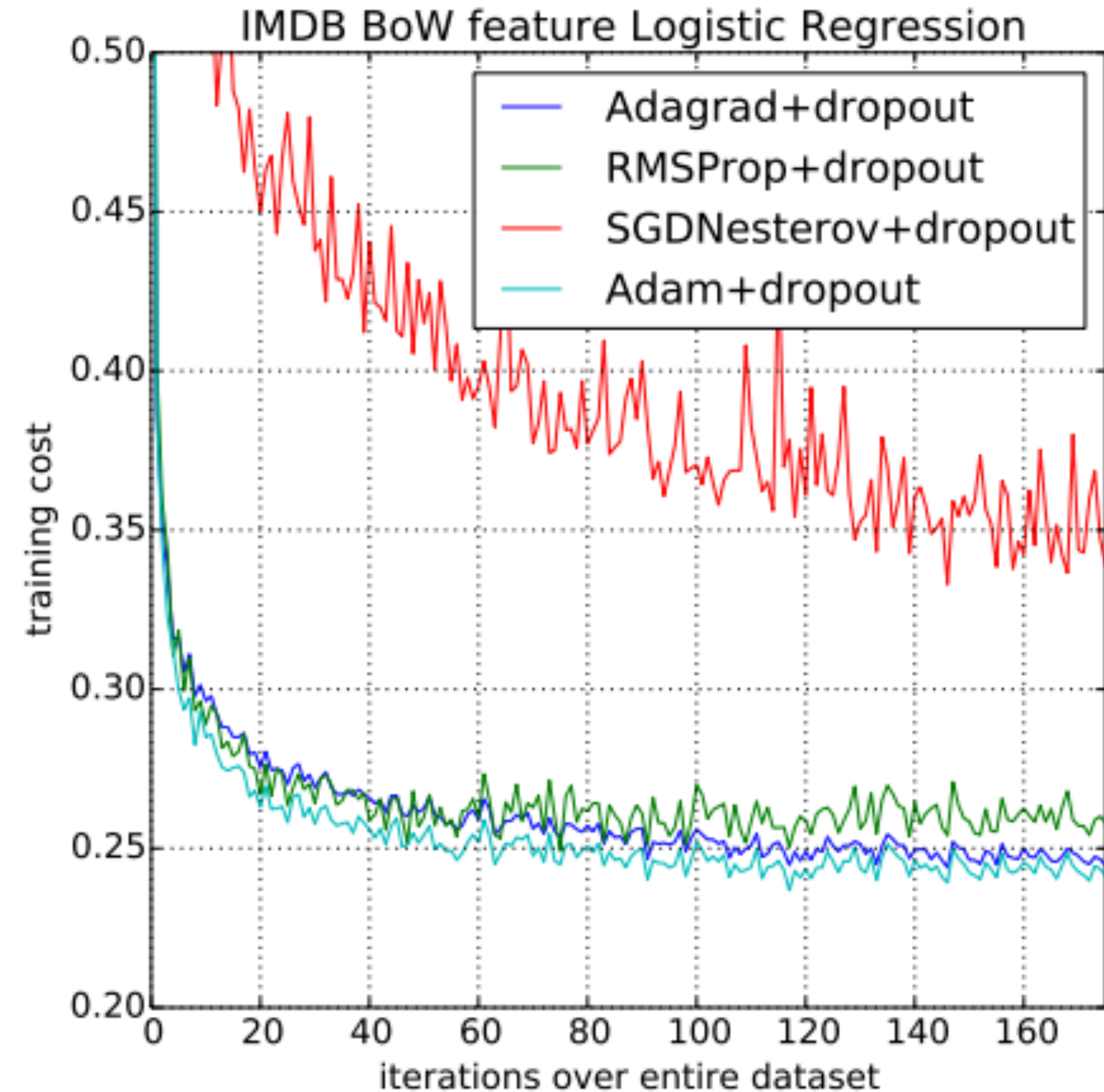
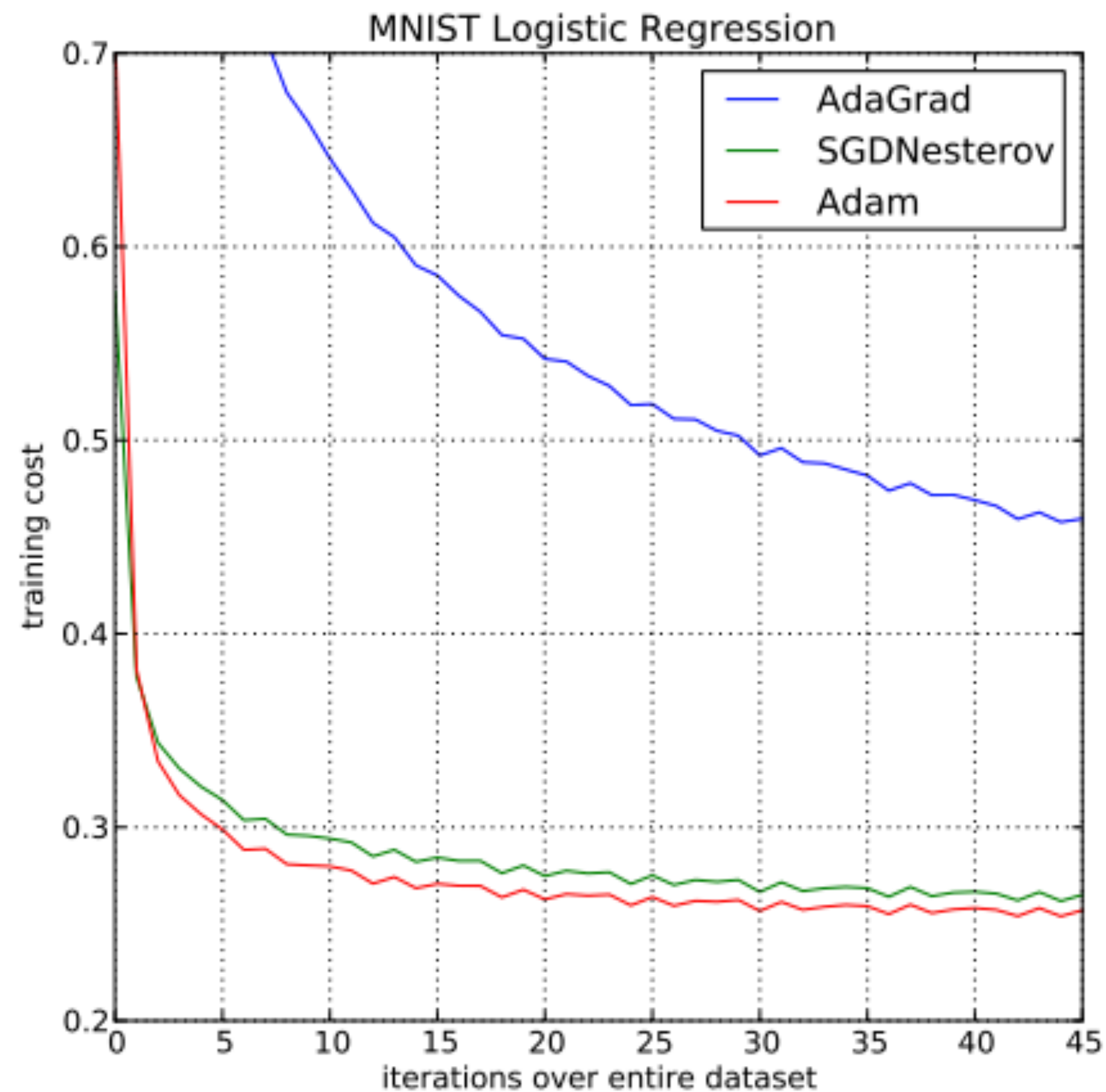
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- ▶ Adaptive step size like Adagrad, incorporates momentum

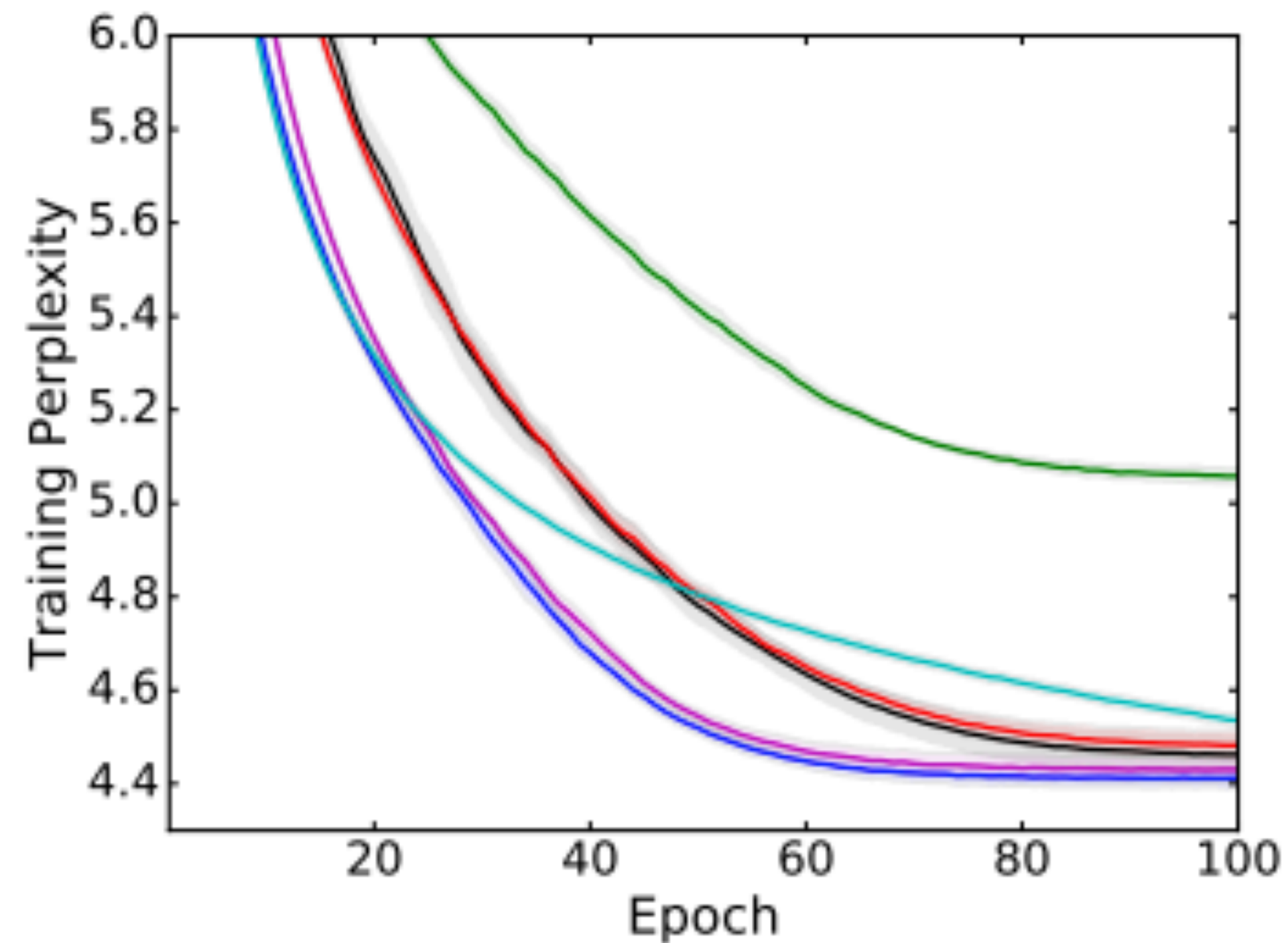
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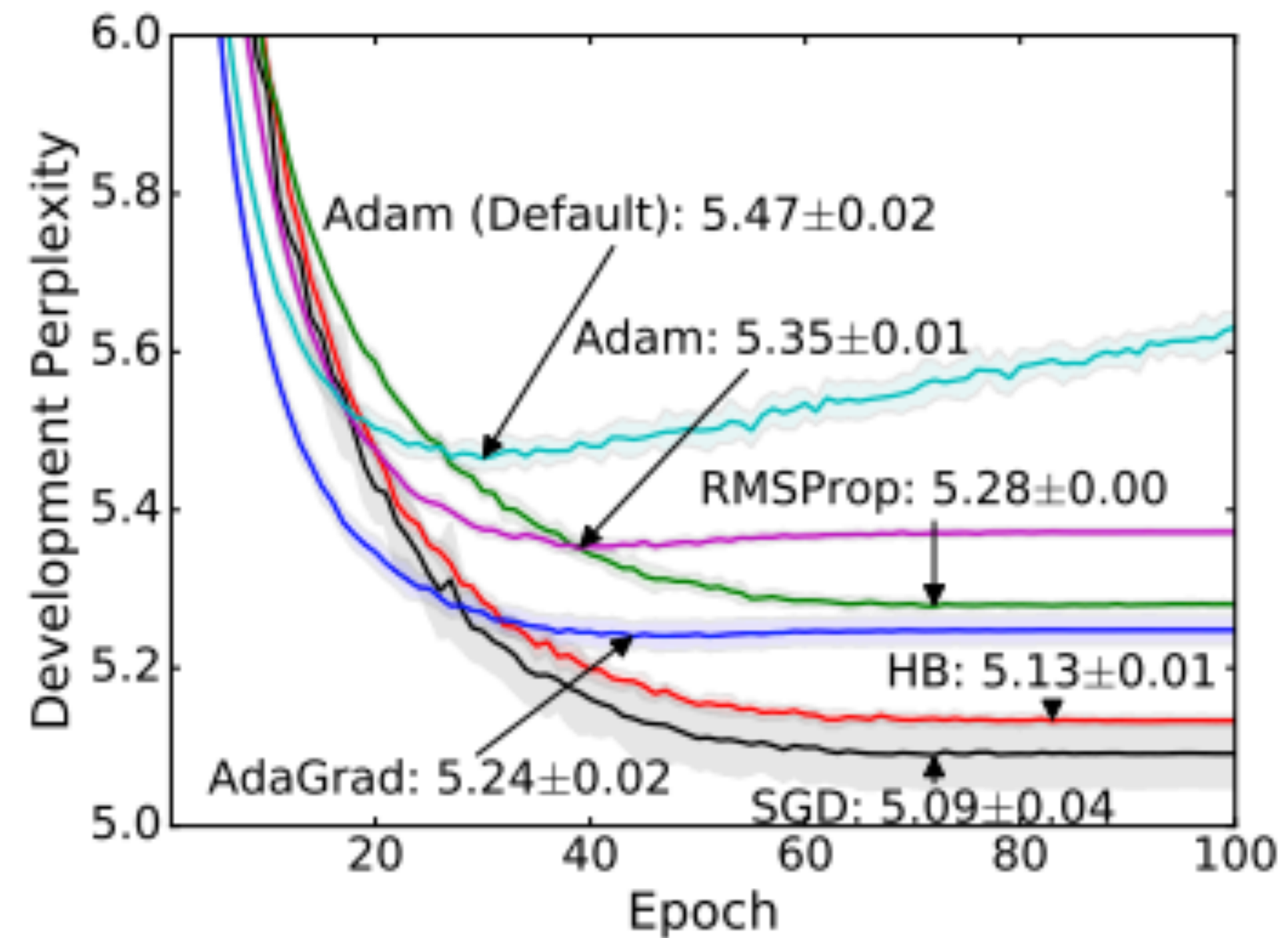


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- Wilson et al. NIPS 2017: adaptive methods can actually perform badly at test time (Adam is in pink, SGD in black)



(e) Generative Parsing (Training Set)

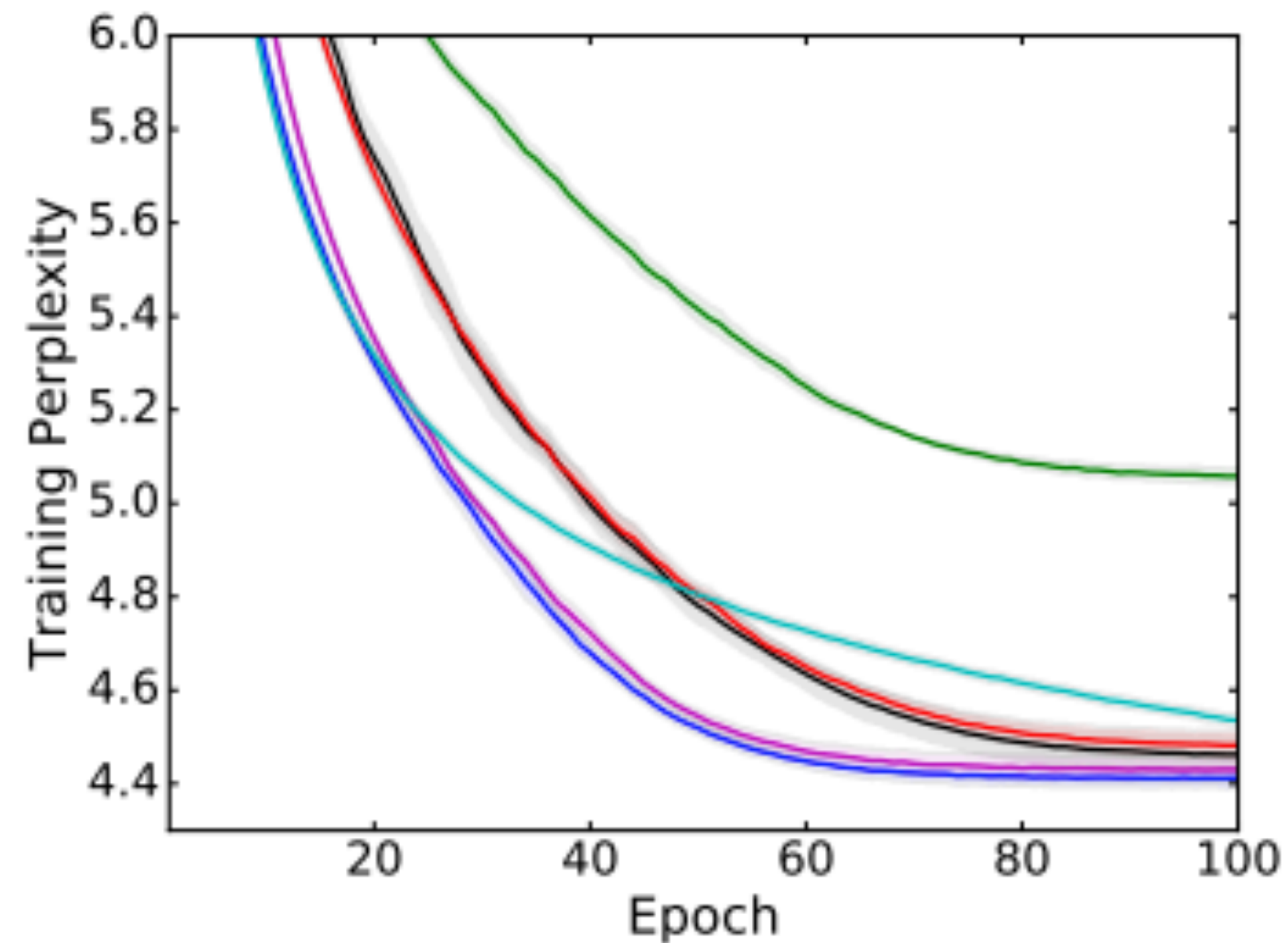


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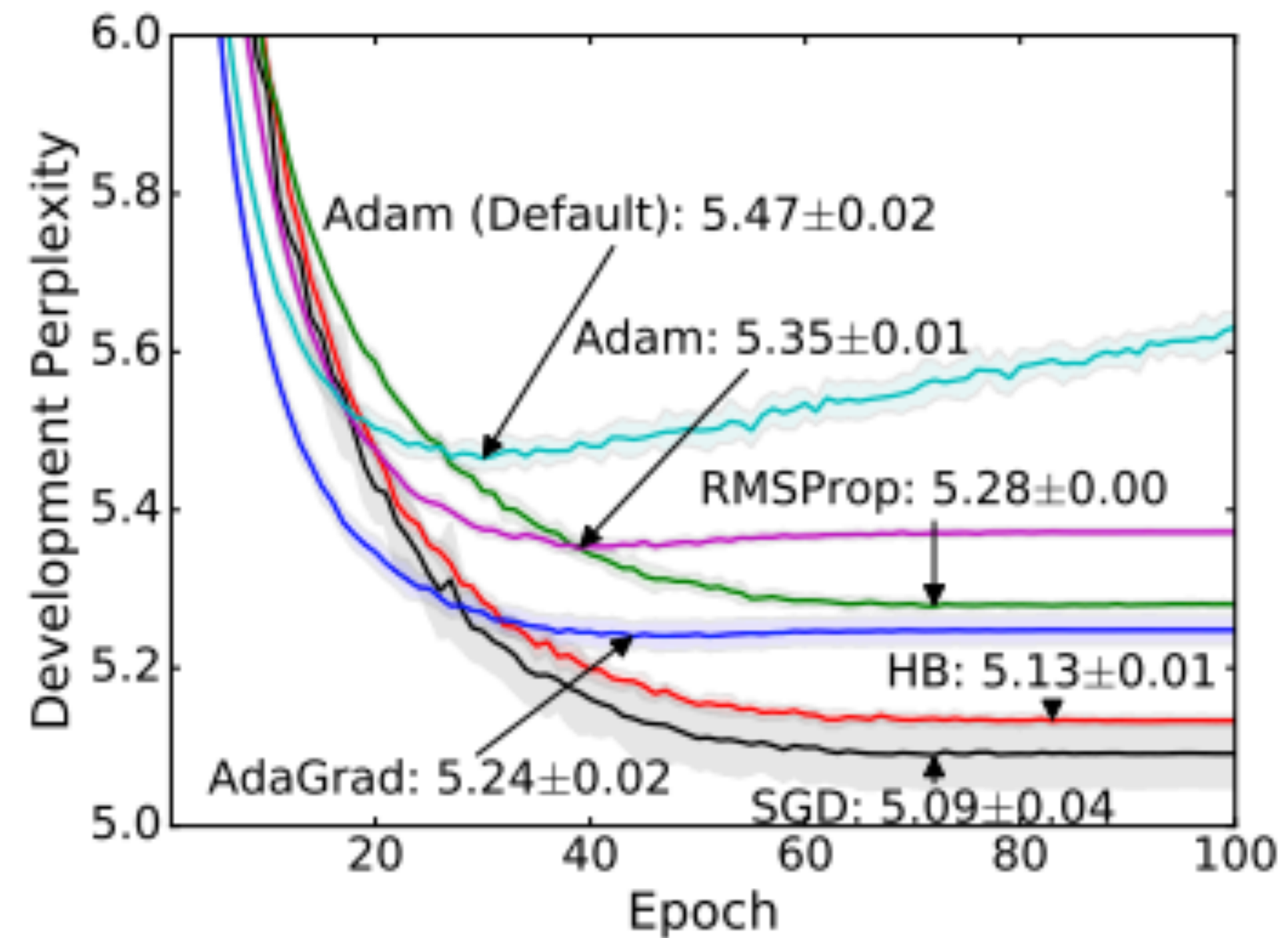


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- ▶ Wilson et al. NIPS 2017: adaptive methods can actually perform badly at test time (Adam is in pink, SGD in black)
- ▶ Check dev set periodically, decrease learning rate if not making progress



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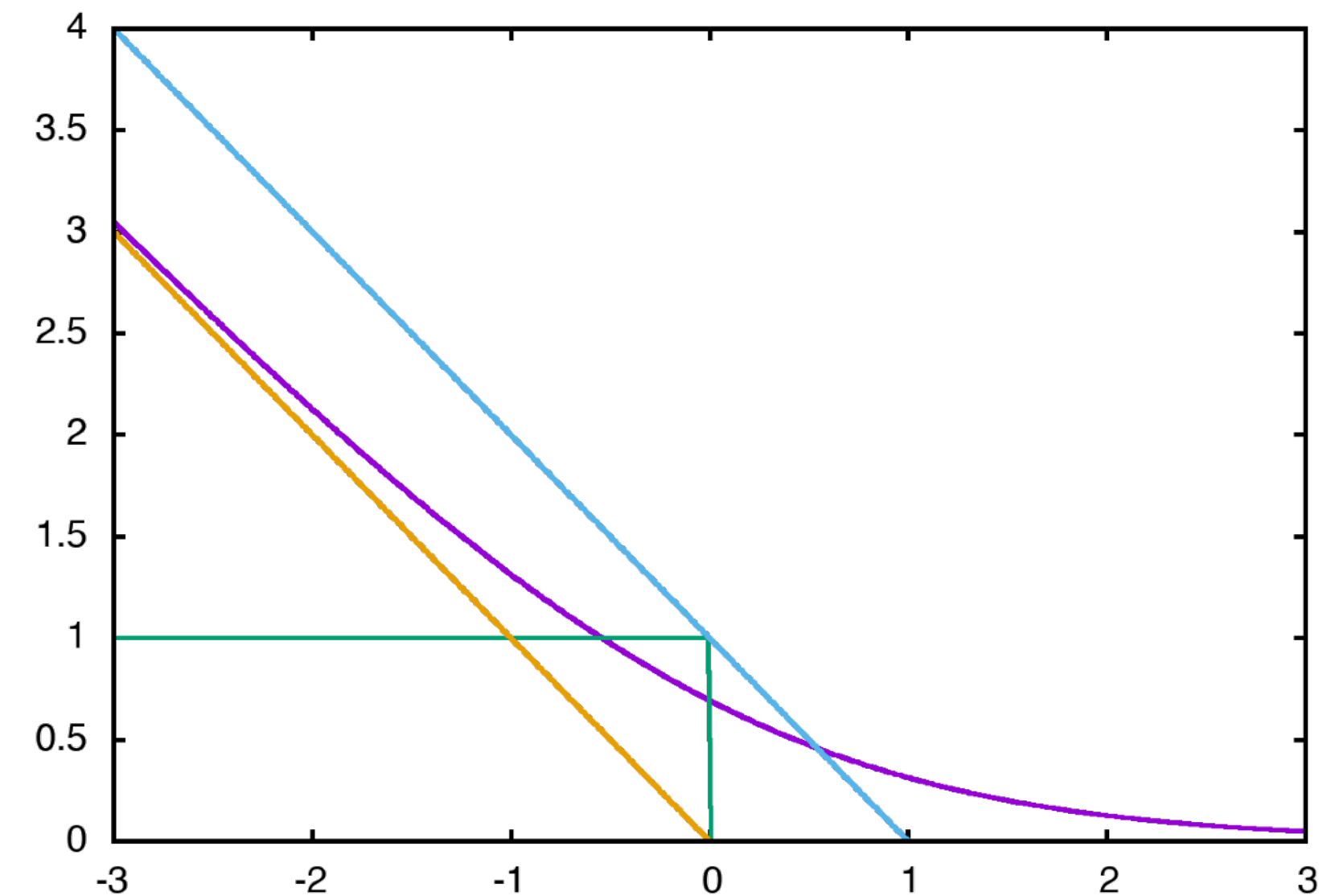
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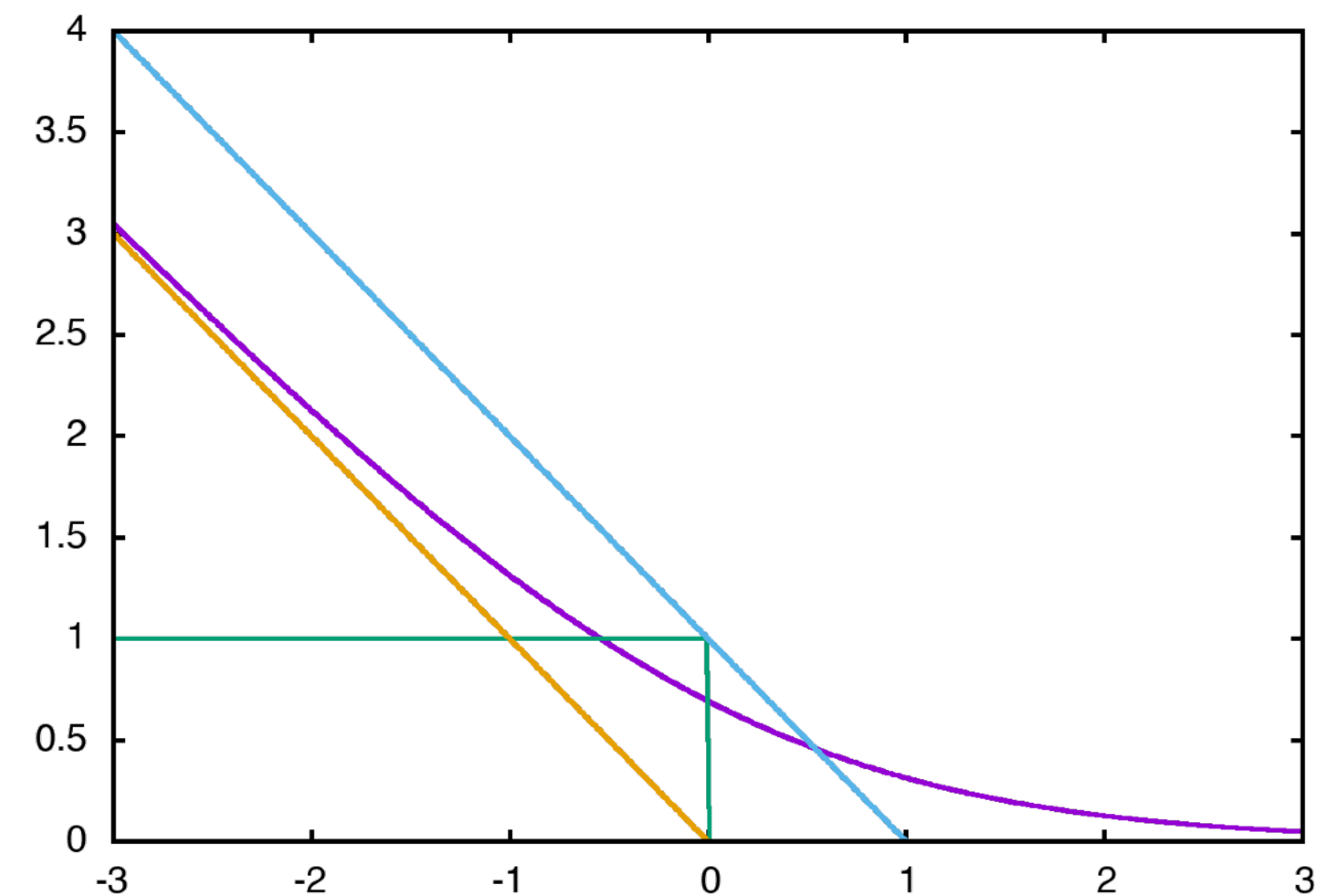
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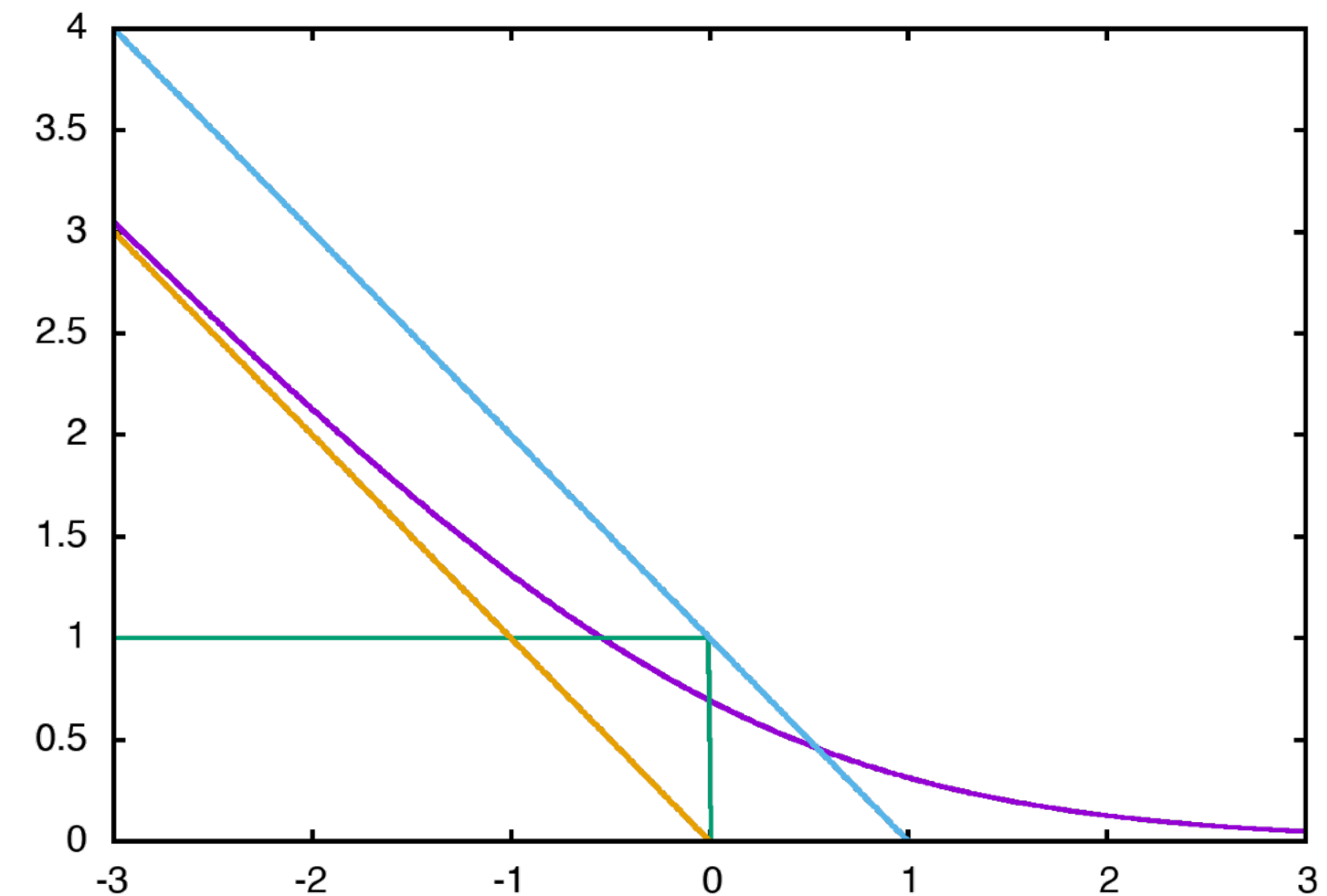
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- ▶ Inference: define the network, your library of choice takes care of it (mostly...)
- ▶ Training: lots of choices for optimization/hyperparameters



# Word Representations

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- ▶ Neural networks work very well at continuous data, but words are discrete



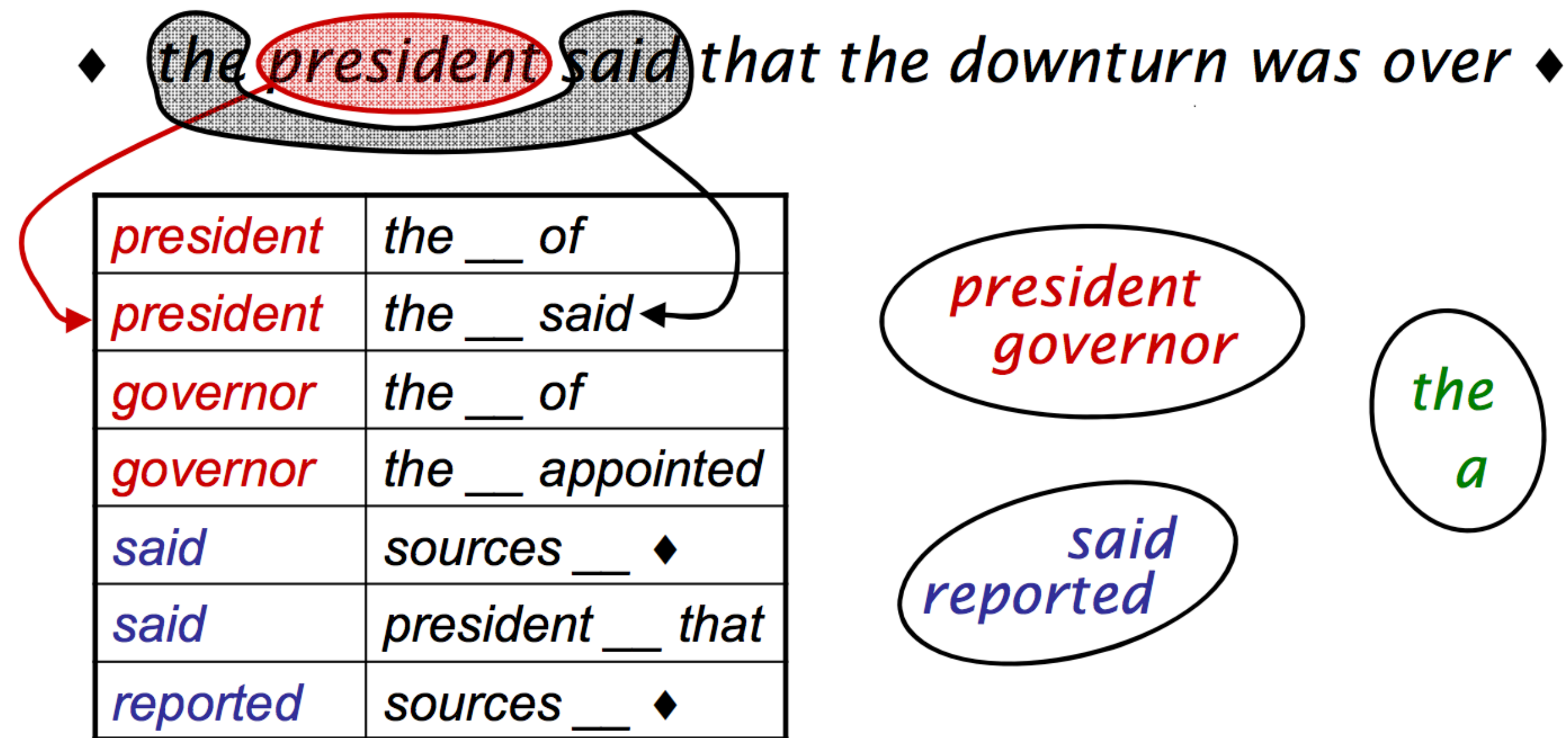
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- ▶ “You shall know a word by the company it keeps” Firth (1957)



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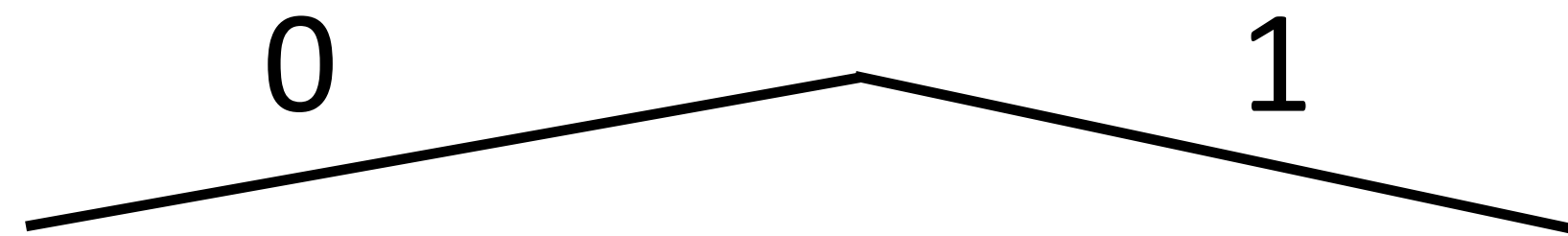
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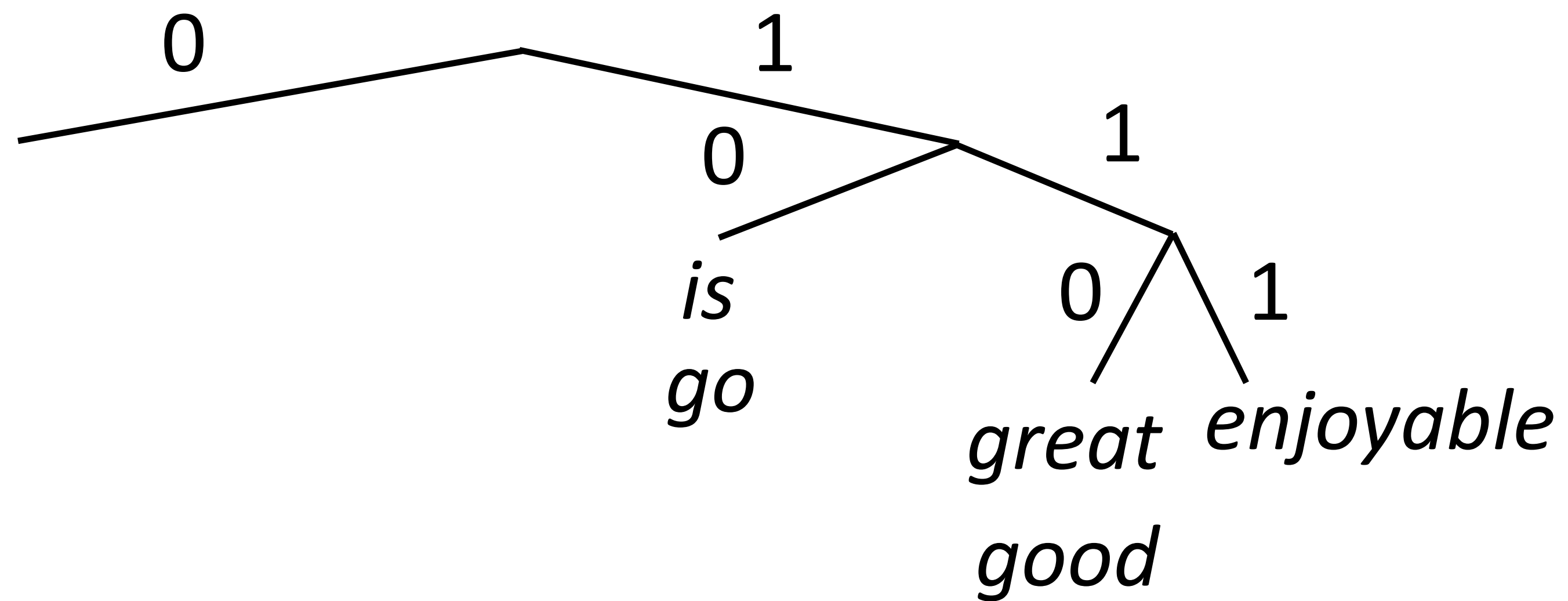
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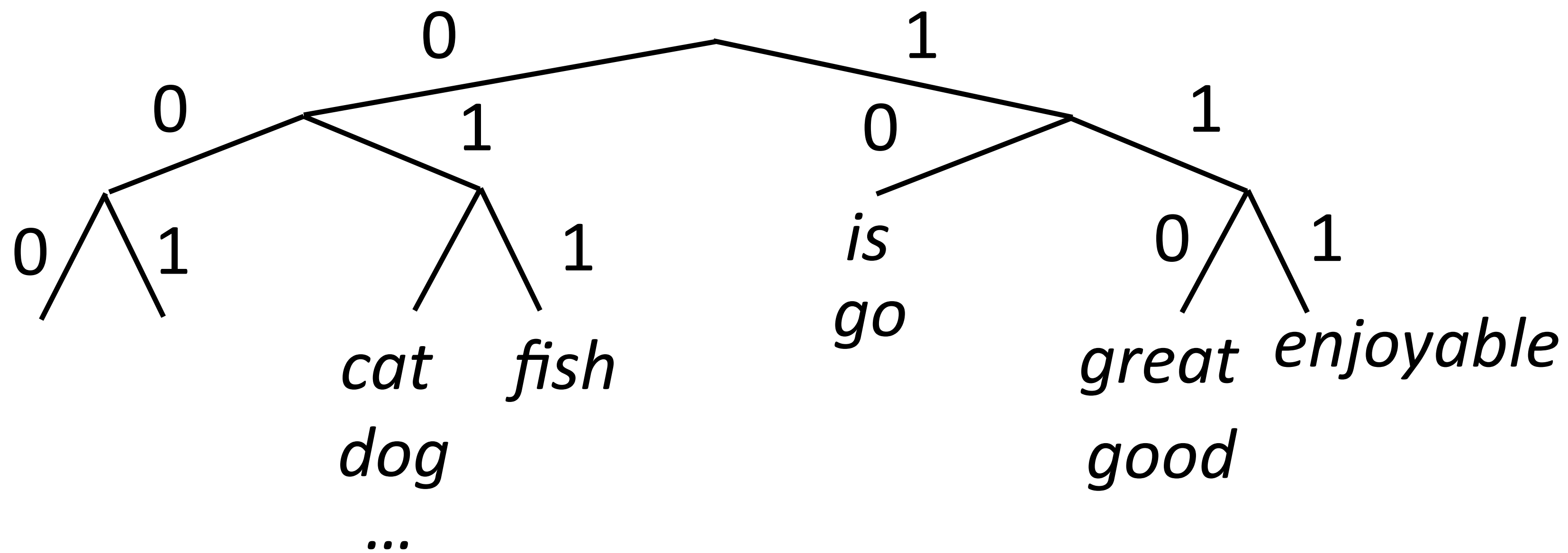
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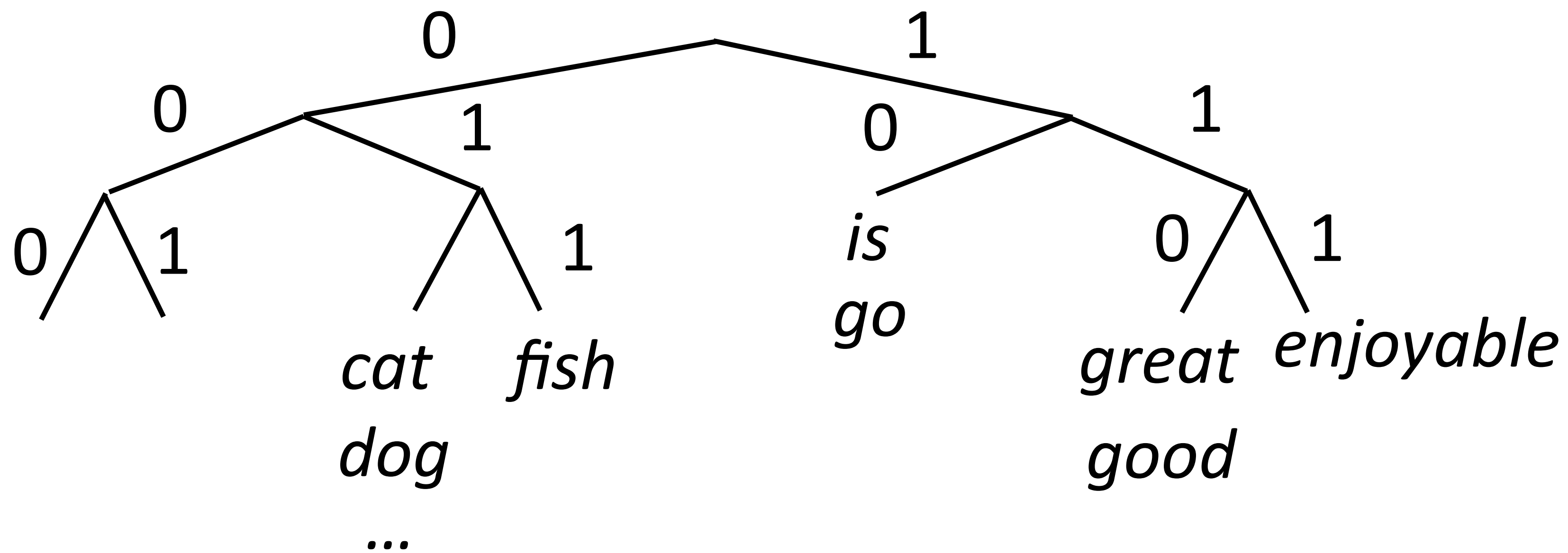
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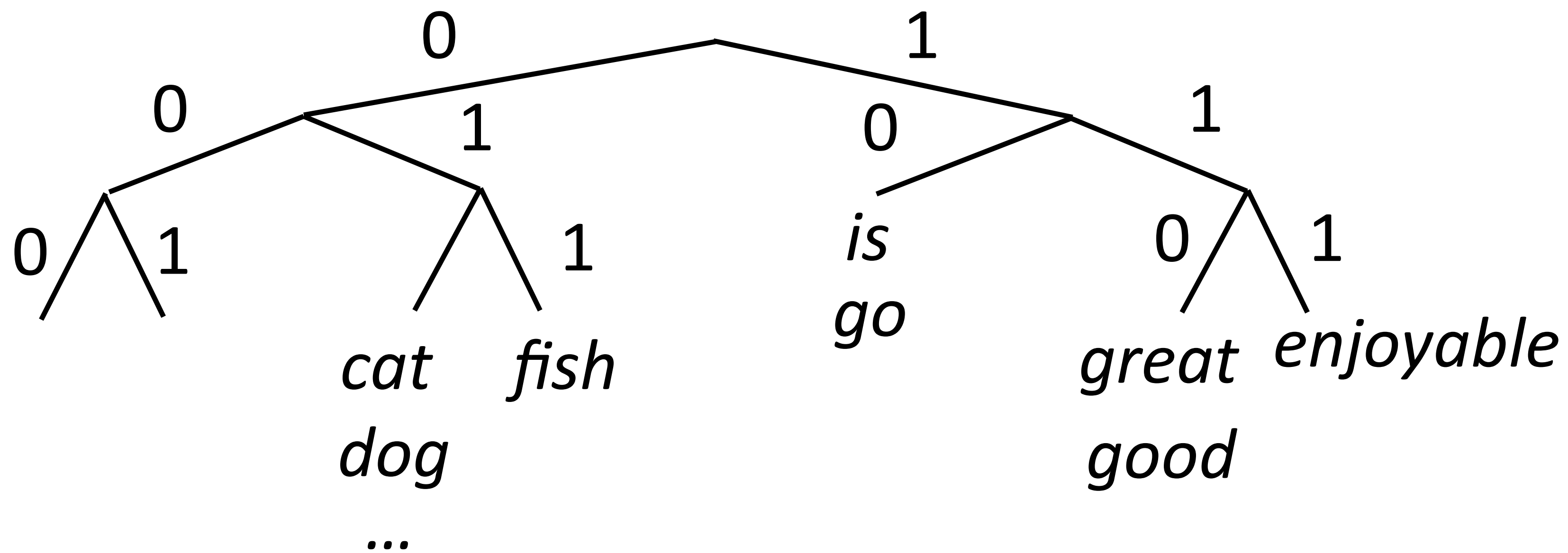


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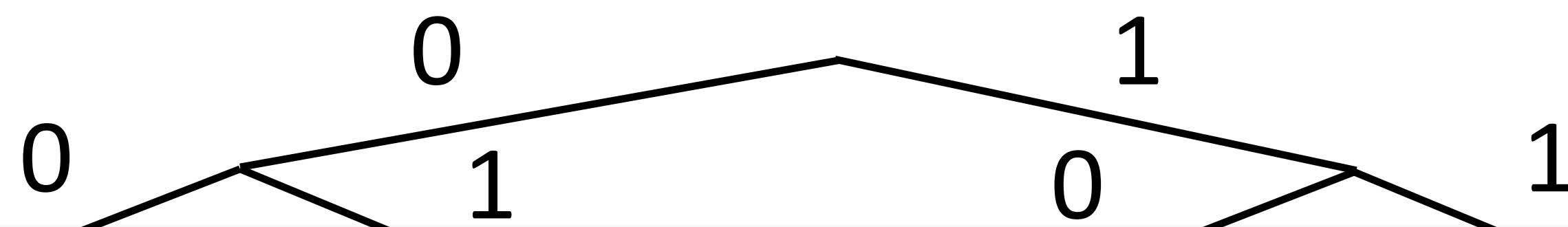
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- Brown et al. (1992)

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## Sample Brown Clusters:

- [https://raw.githubusercontent.com/aritter/5525\\_perceptron\\_tagger/master/60K\\_clusters.bits.txt](https://raw.githubusercontent.com/aritter/5525_perceptron_tagger/master/60K_clusters.bits.txt)

*cat fish*

*g*

*great enjoyable*

*dog*

*good*

...

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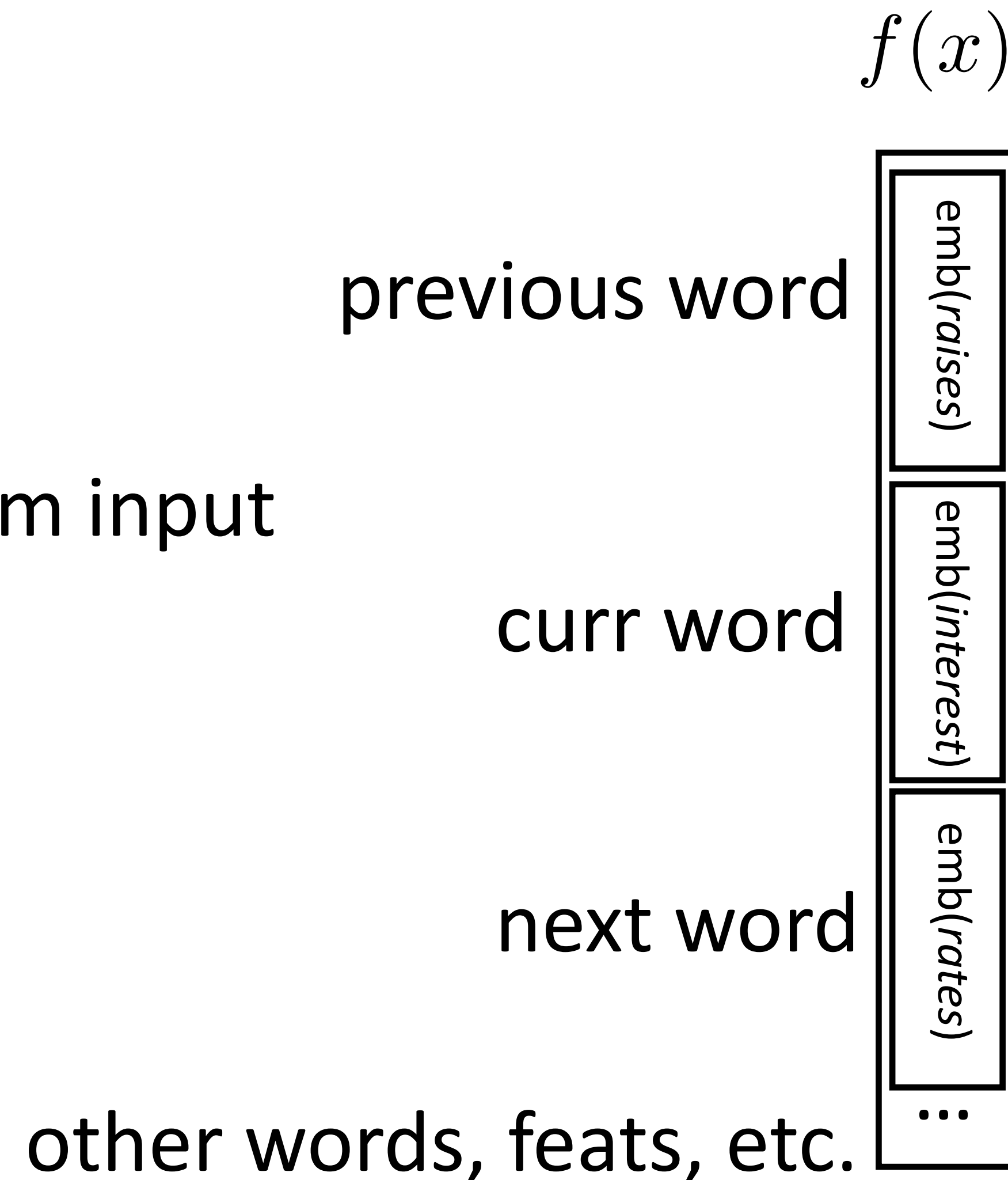
# Word Embeddings

- ▶ Part-of-speech tagging with FFNNs

??

*Fed raises interest rates in order to ...*

- ▶ Word embeddings for each word form input



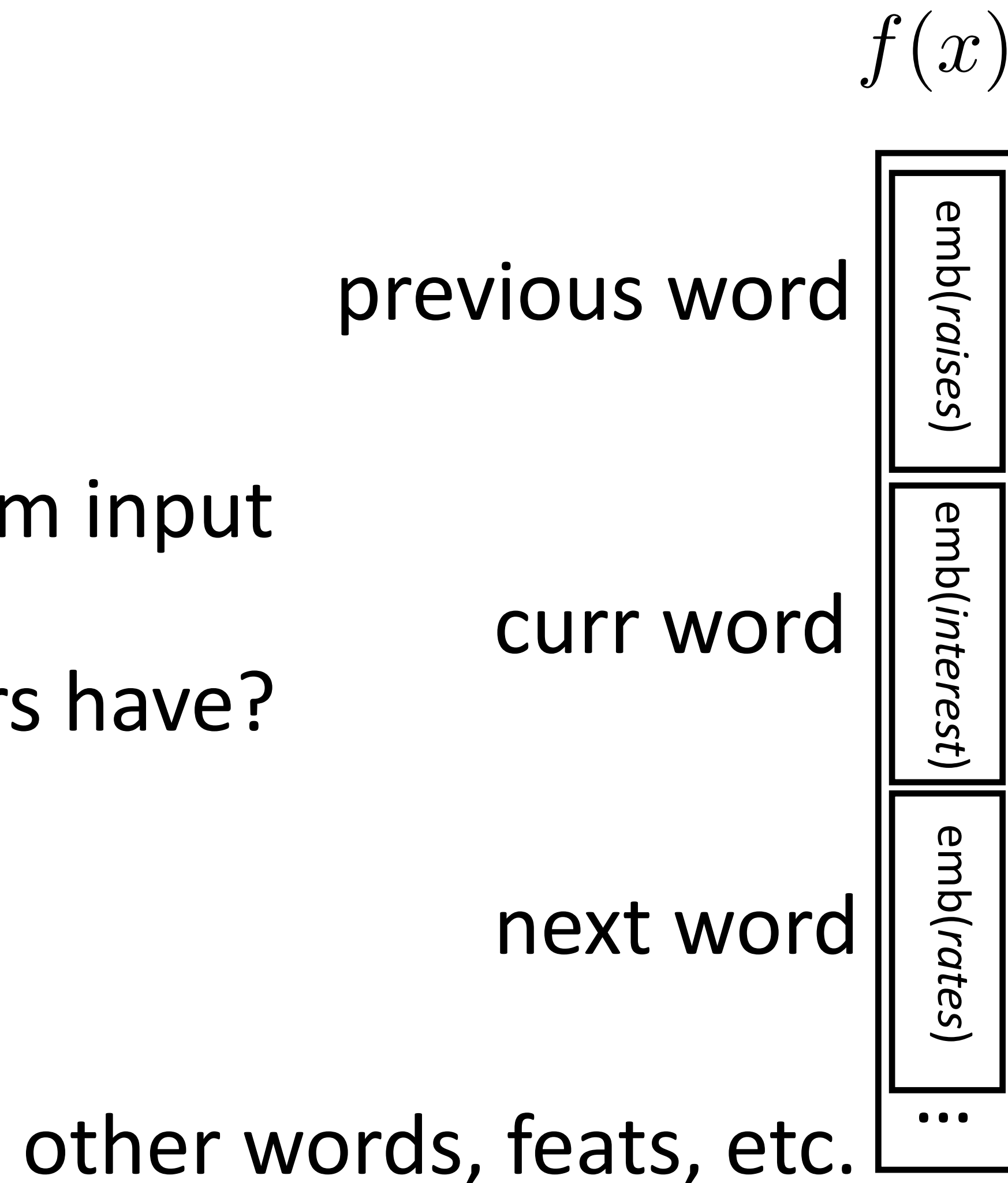
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*Fed raises **interest** rates in order to ...*

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- ▶ What properties should these vectors have?

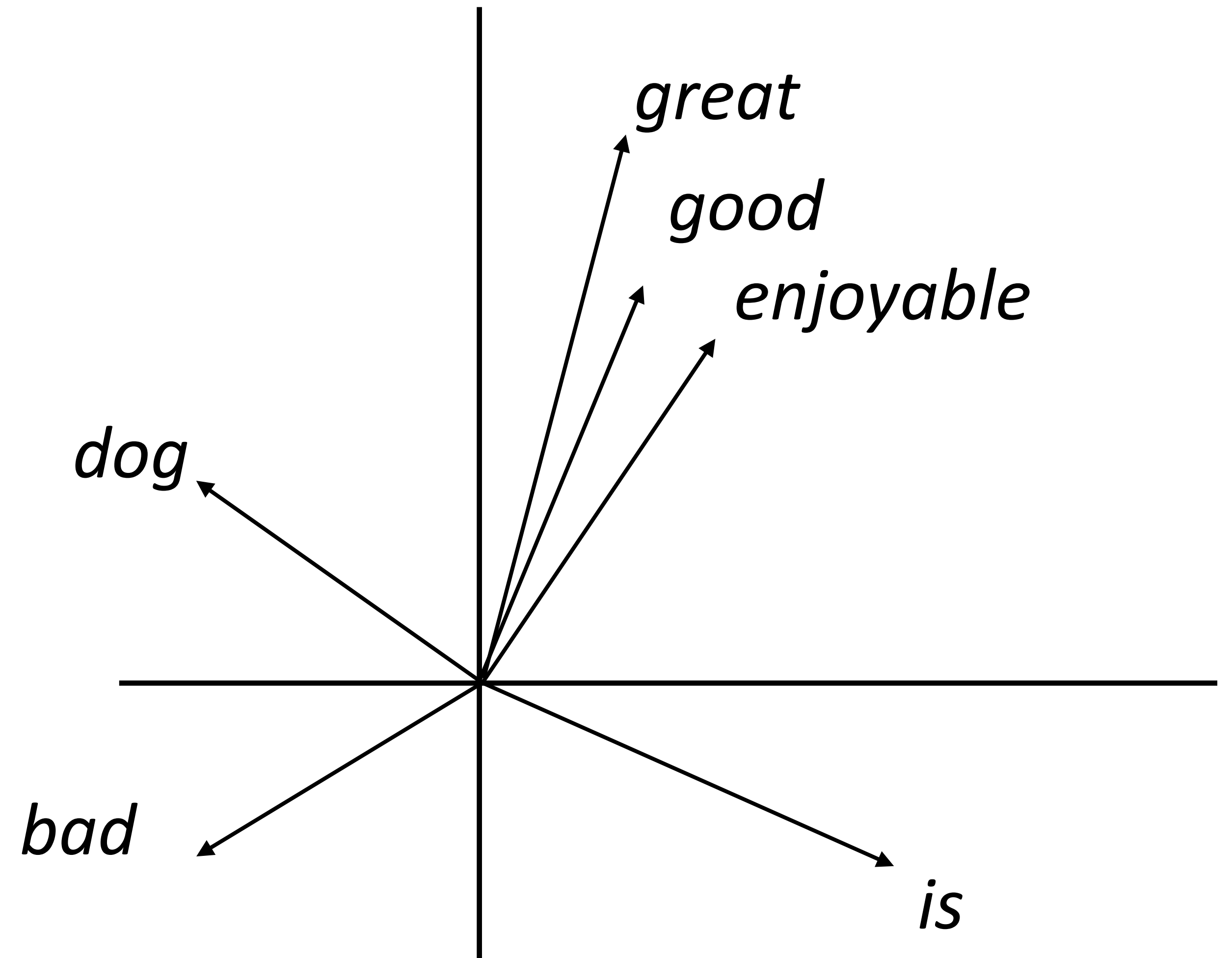


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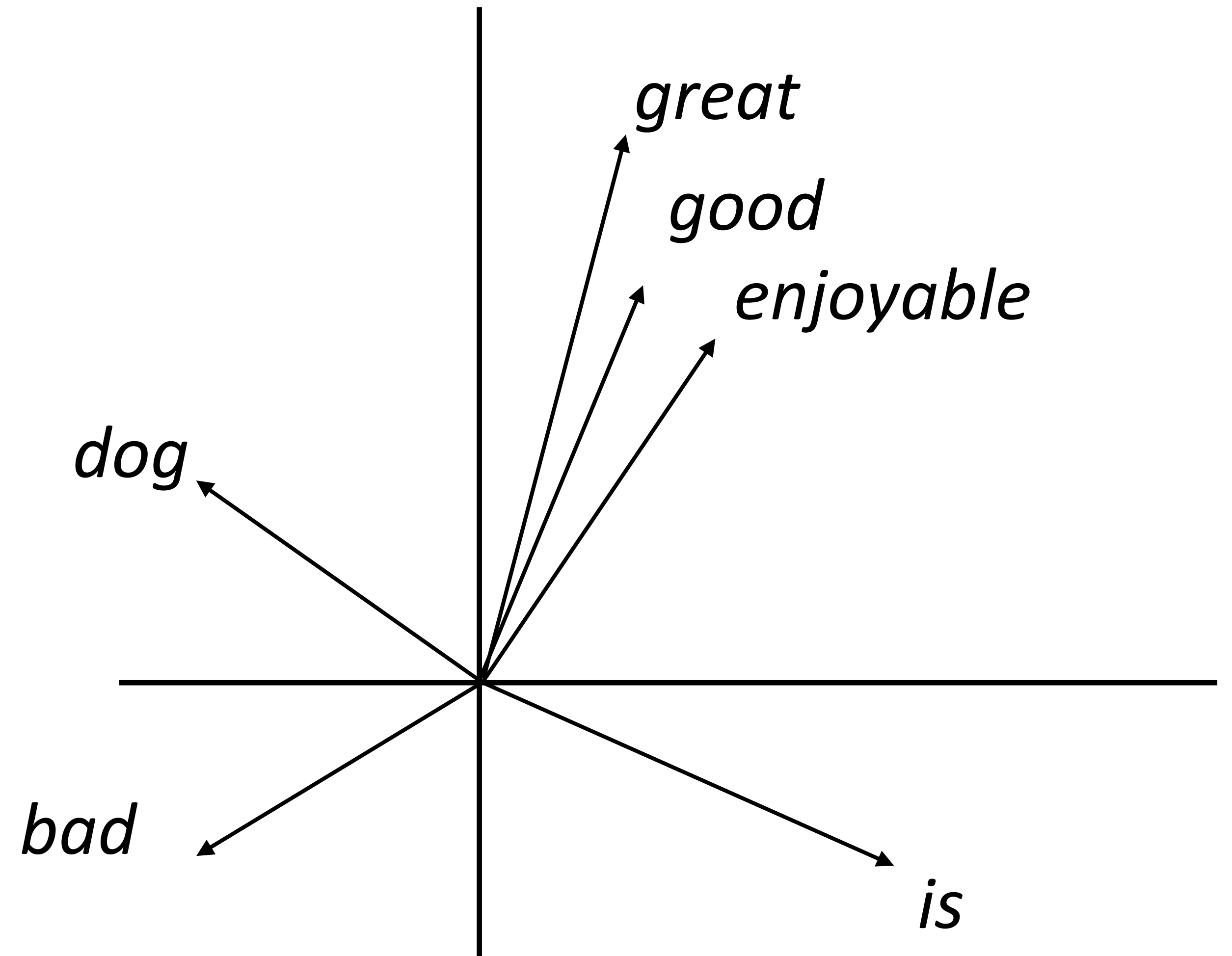
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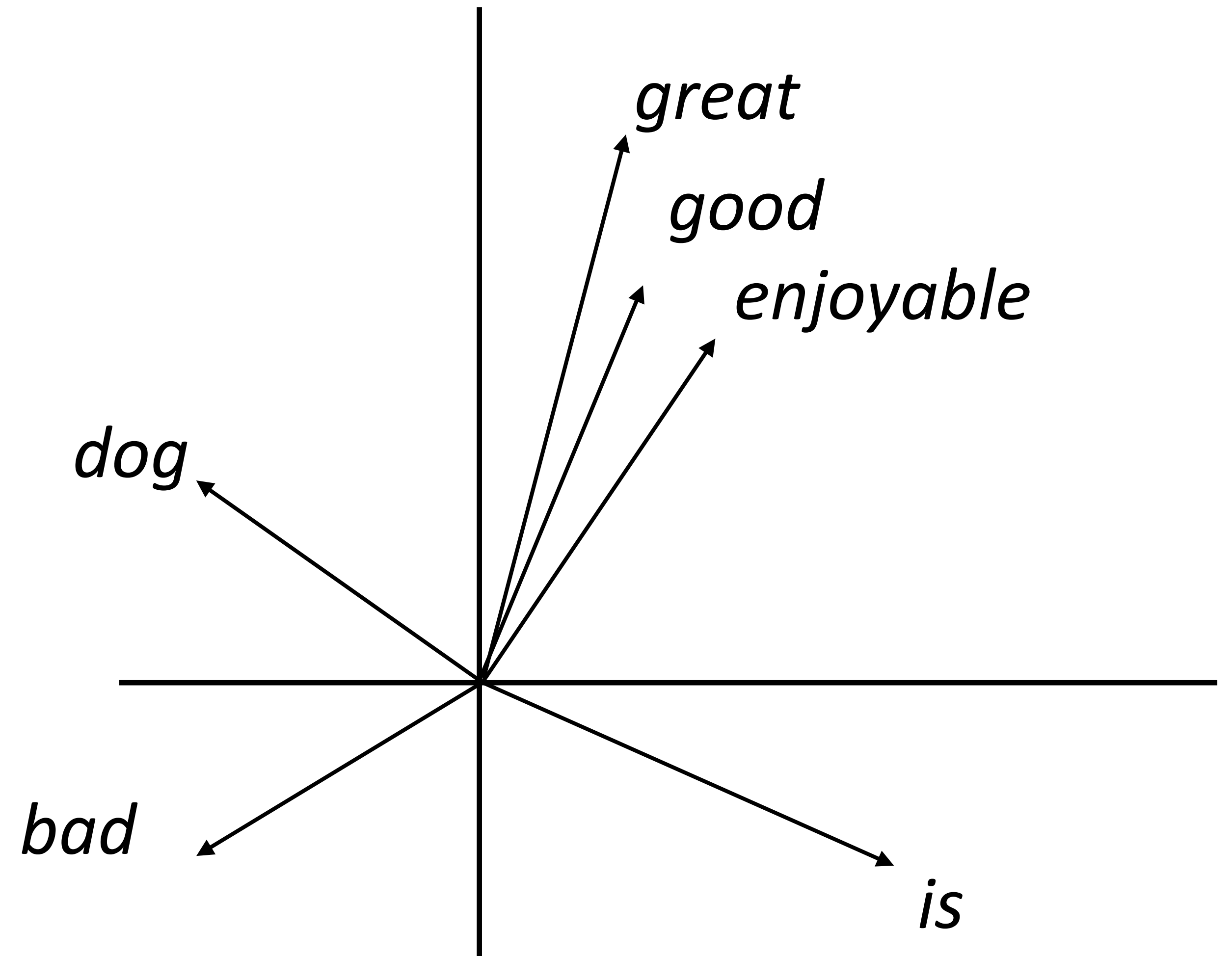
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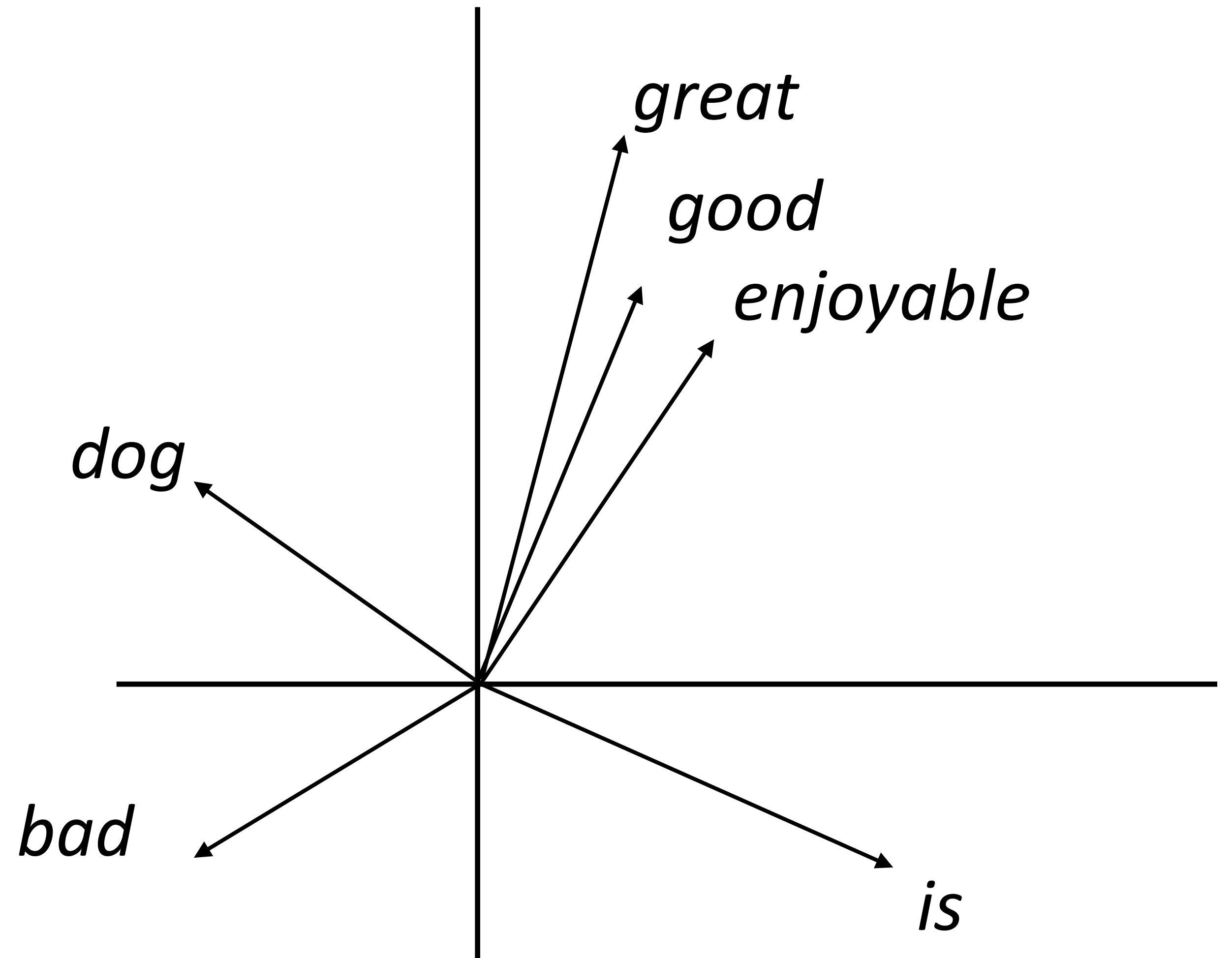
- ▶ Want a vector space where similar words have similar embeddings

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- ▶ Goal: come up with a way to produce these embeddings



word2vec/GloVe

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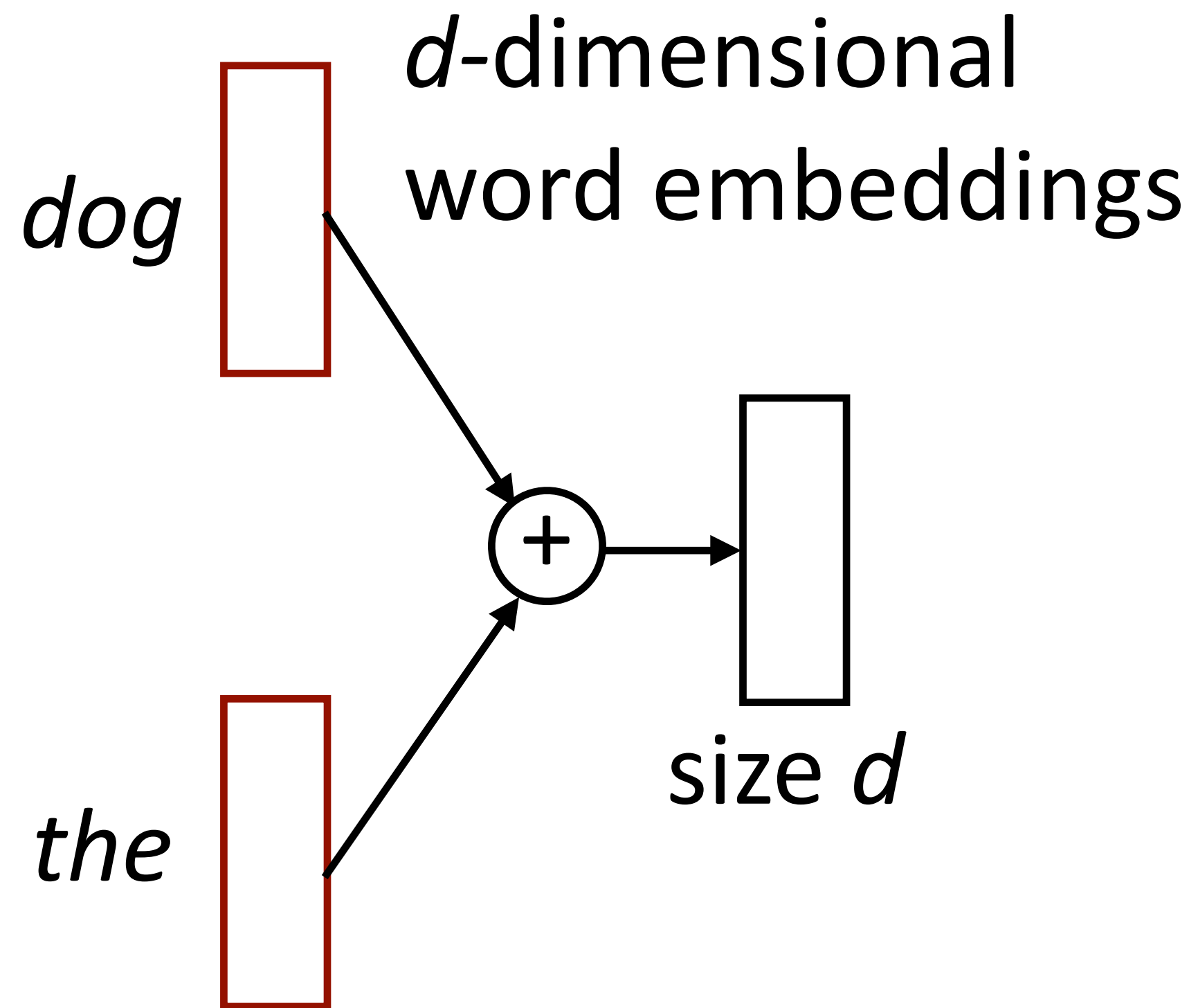
*dog*   $d$ -dimensional  
word embeddings

*the* 

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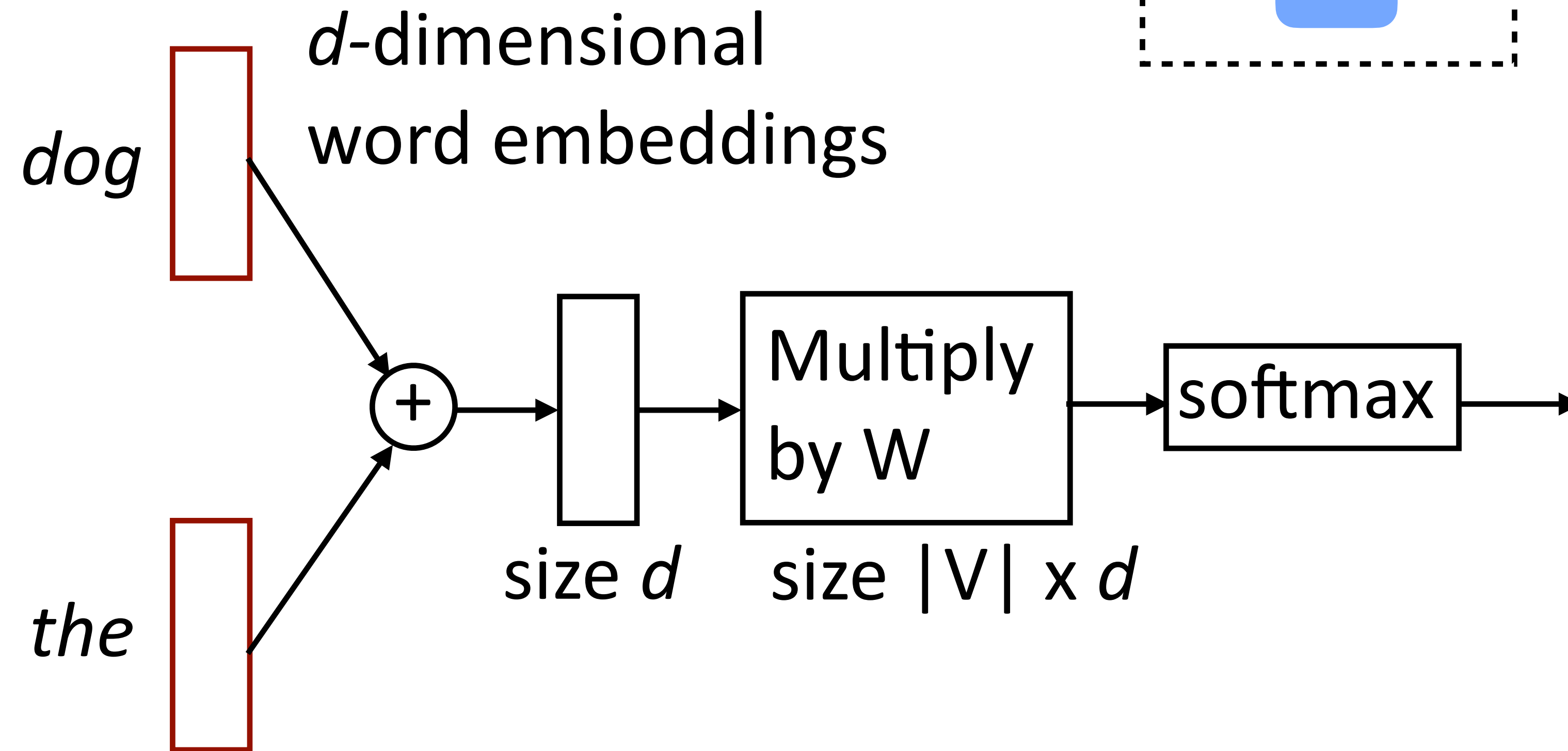
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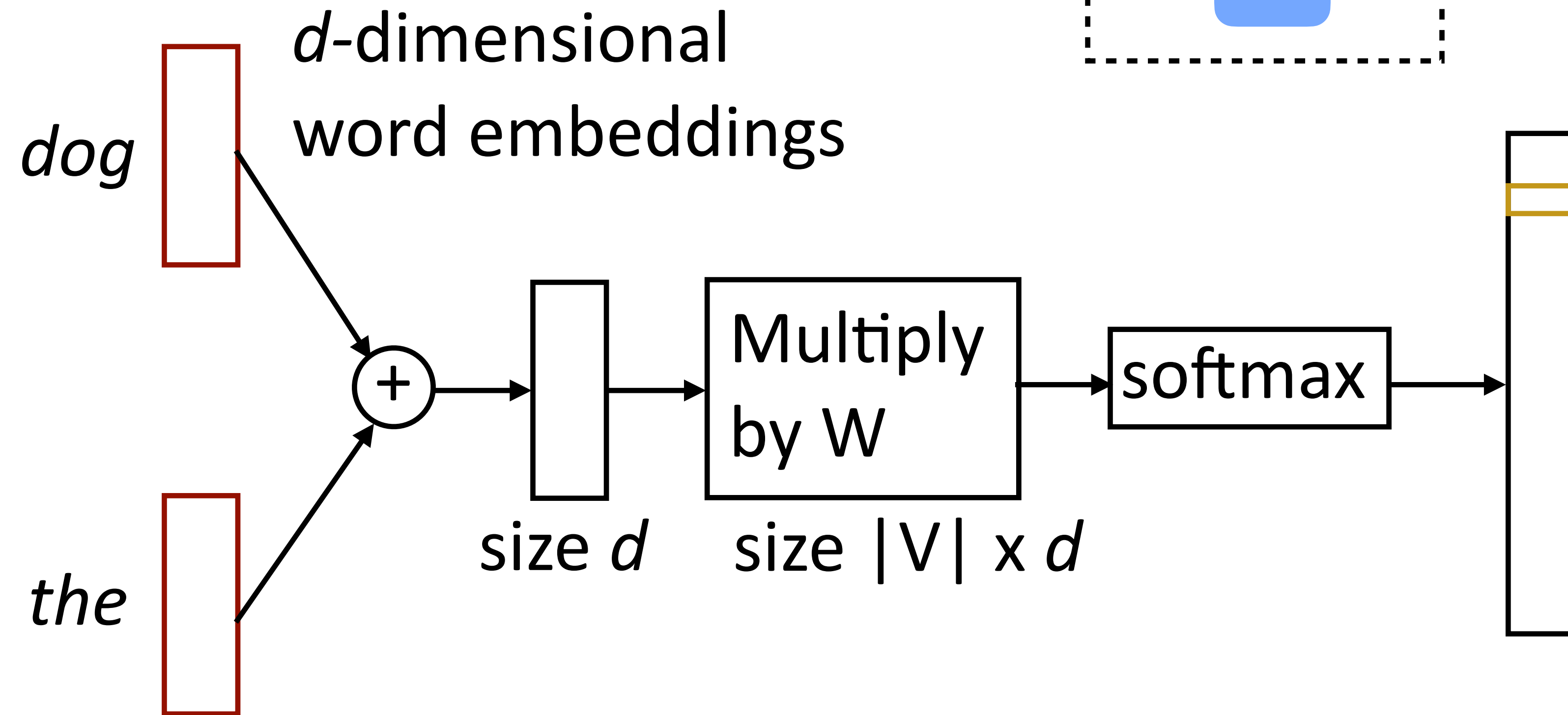
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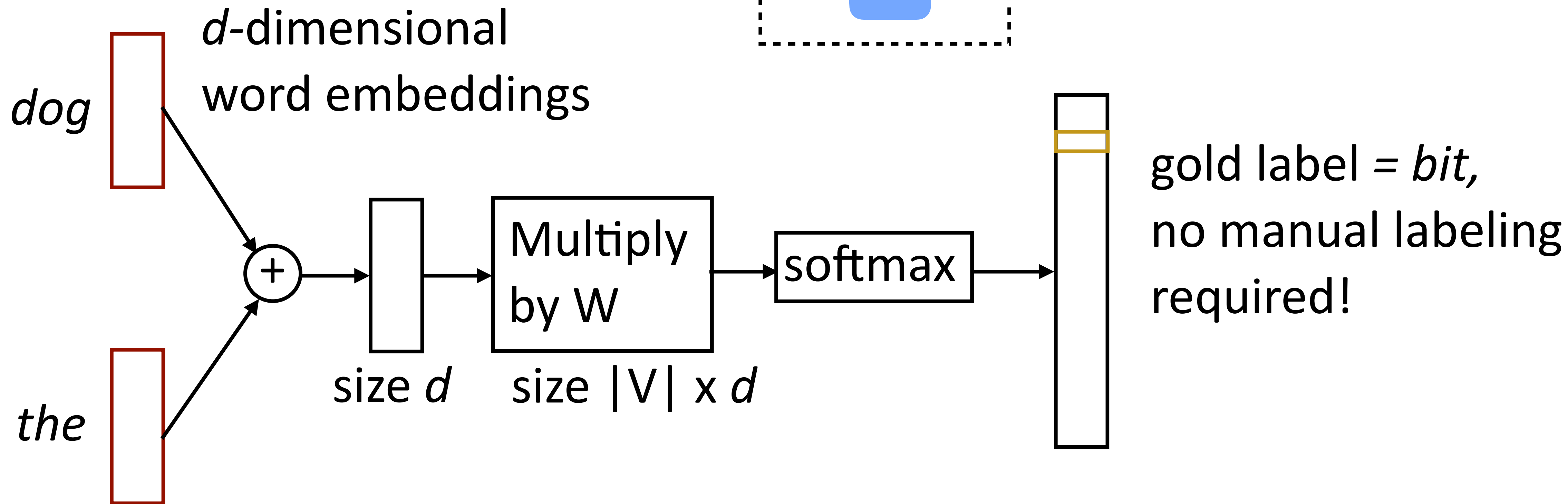
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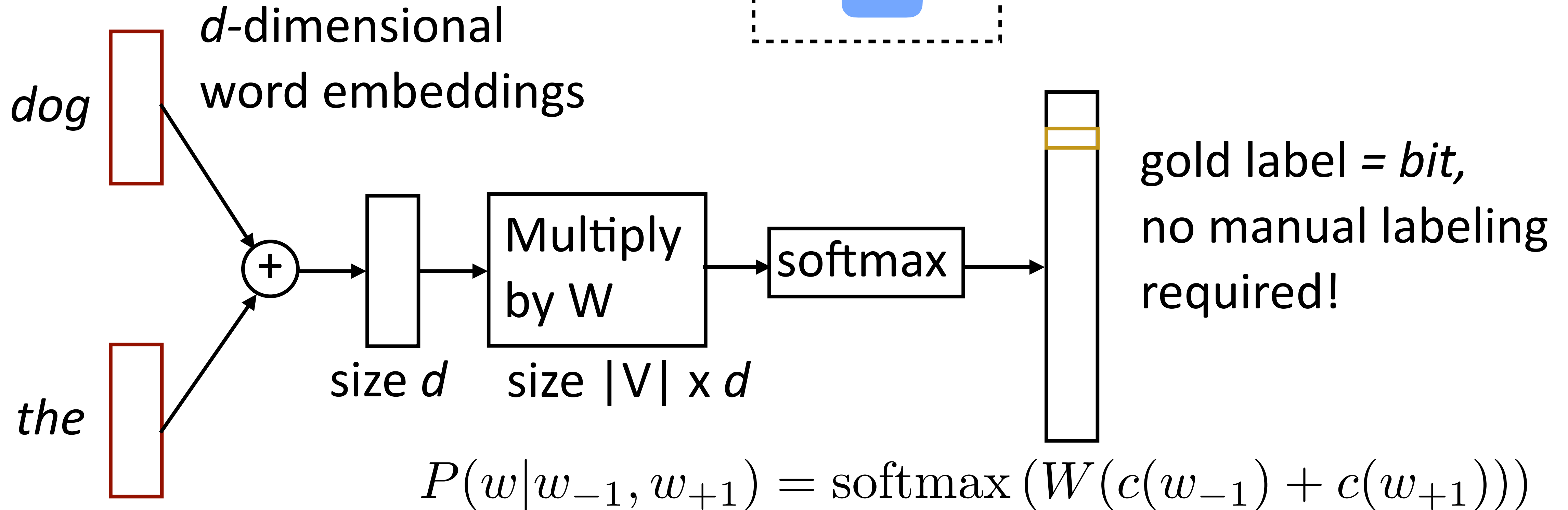




# Continuous Bag-of-Words

- ▶ Predict word from context

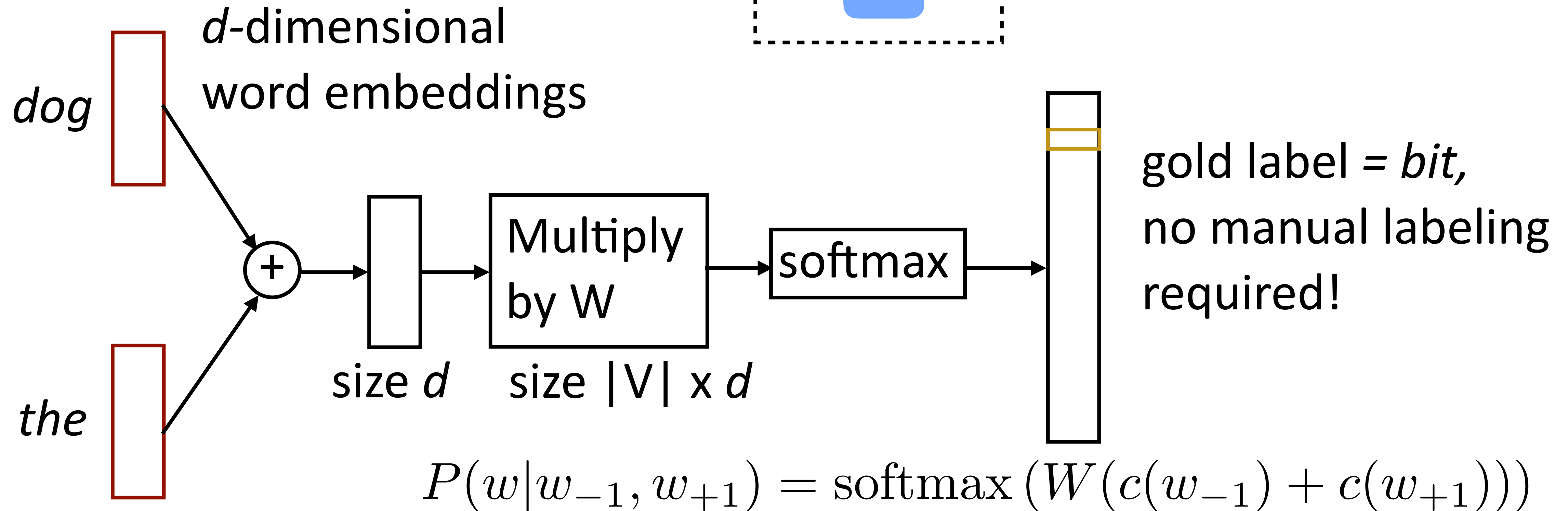
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# Continuous Bag-of-Words

- ▶ Predict word from context

*the dog **bit** the man*



- ▶ Parameters:  $d \times |V|$  (one  $d$ -length **vector per voc word**),  
 $|V| \times d$  output parameters (W)

Mikolov et al. (2013)

# Skip-Gram

---

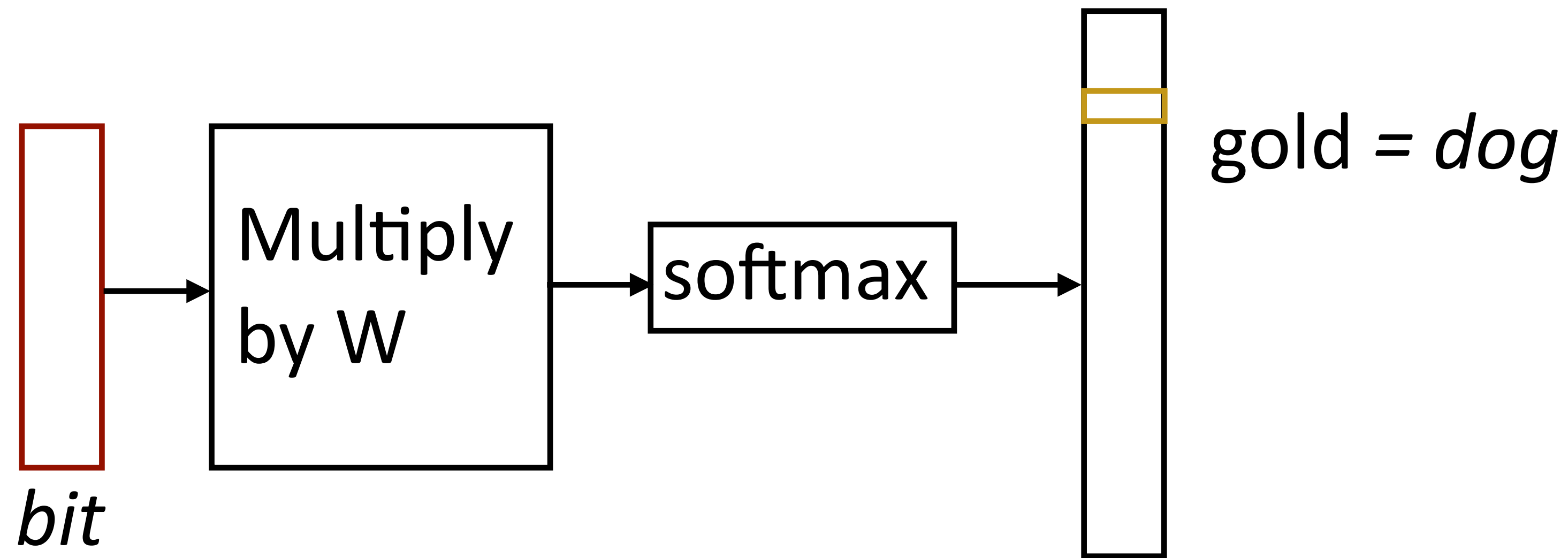
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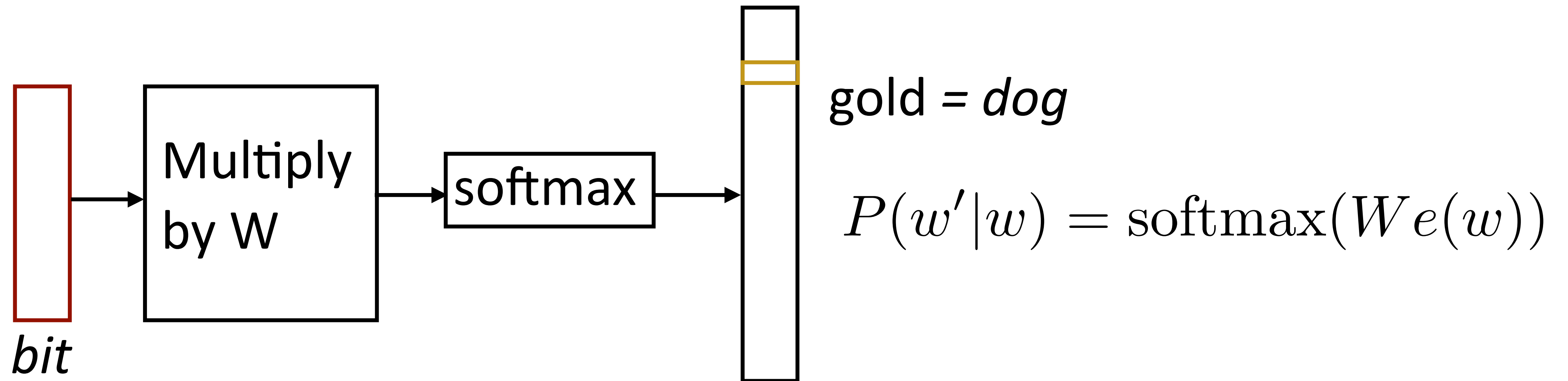
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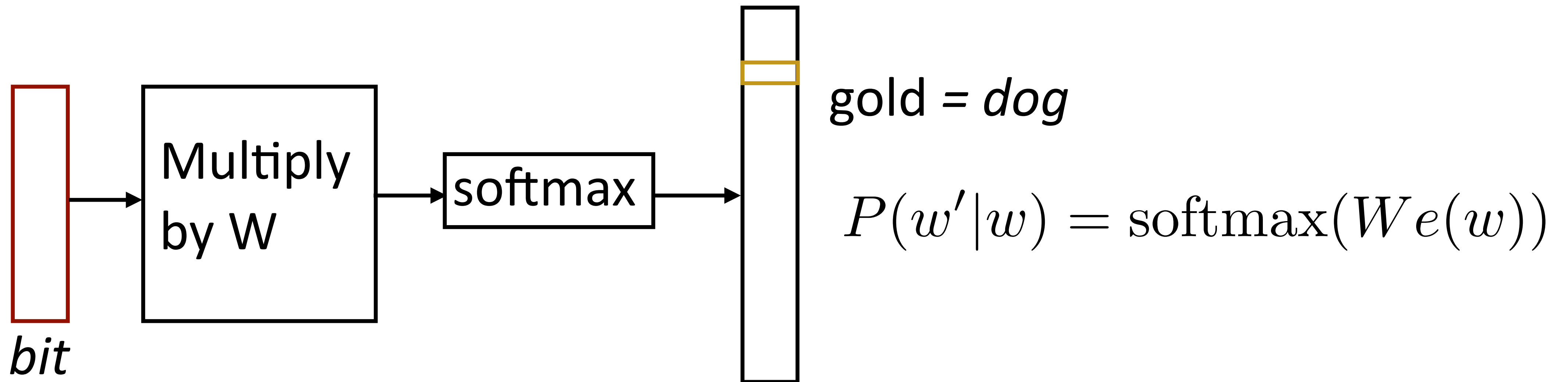
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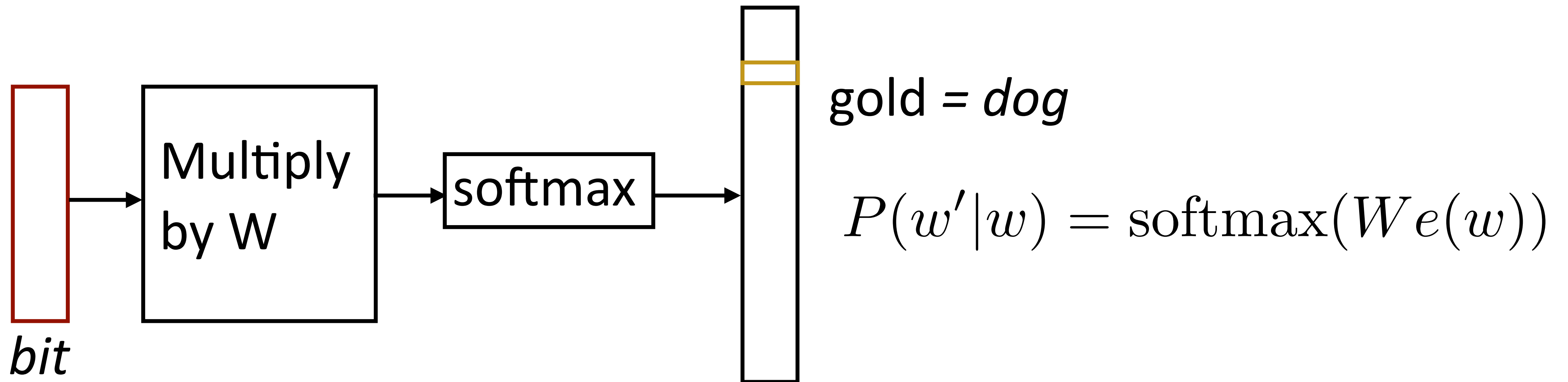


- ▶ Another training example: *bit* -> *the*

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- ▶ Predict one word of context from word

*the dog bit the man*



- ▶ Another training example: *bit* -> *the*
- ▶ Parameters:  $d \times |V|$  **vectors**,  $|V| \times d$  output parameters ( $W$ ) (also usable as vectors!)

# Hierarchical Softmax

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$$P(w|w_{-1}, w_{+1}) = \text{softmax}(W(c(w_{-1}) + c(w_{+1}))) \quad P(w'|w) = \text{softmax}(We(w))$$



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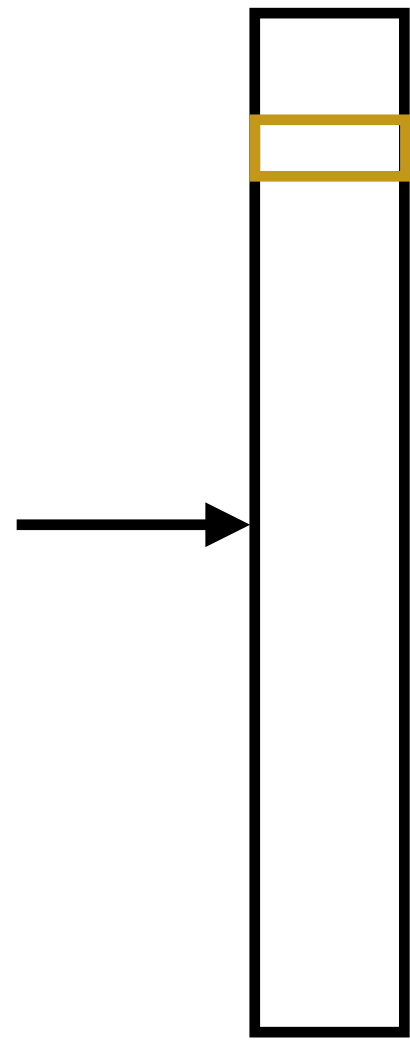
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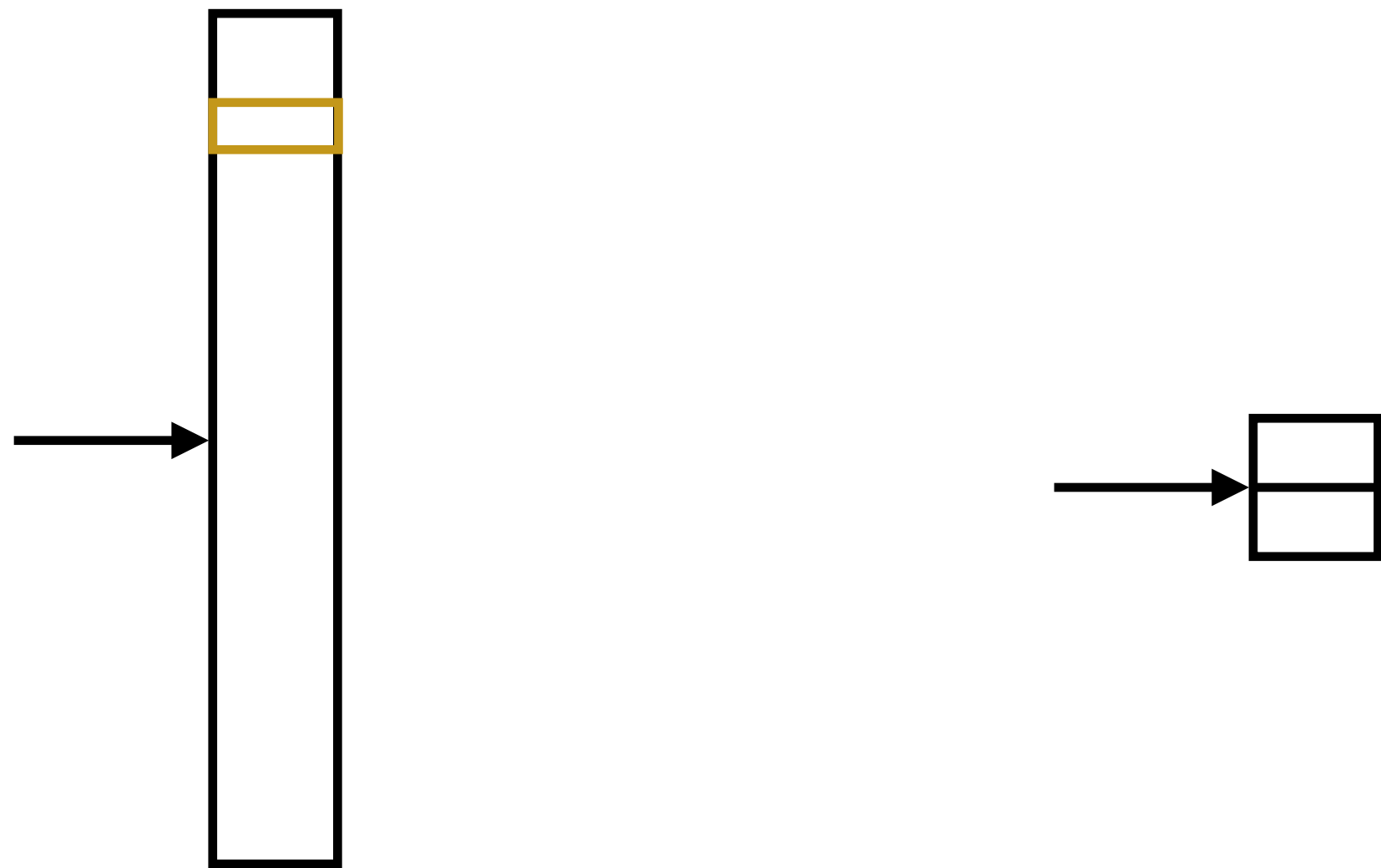
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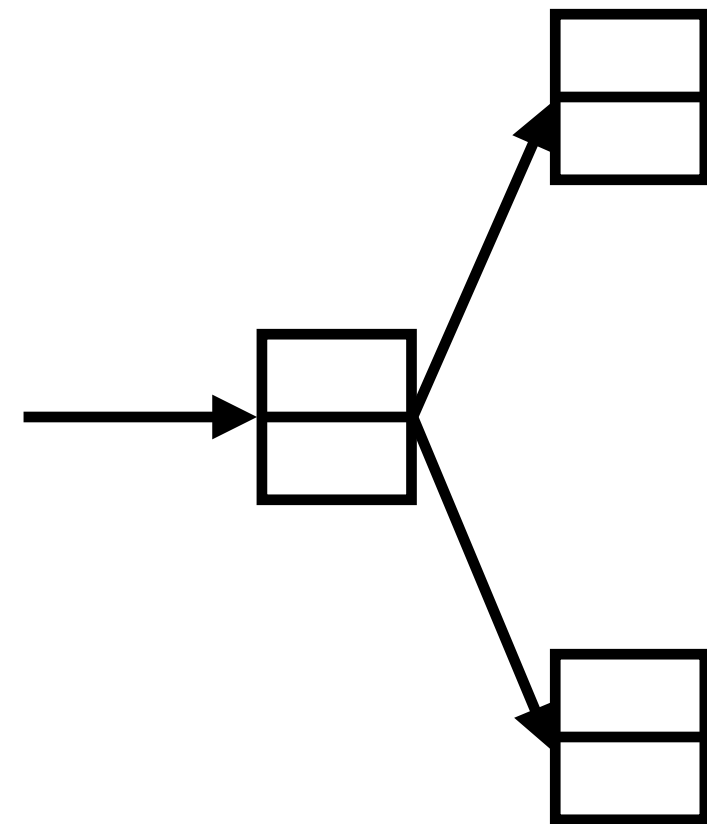
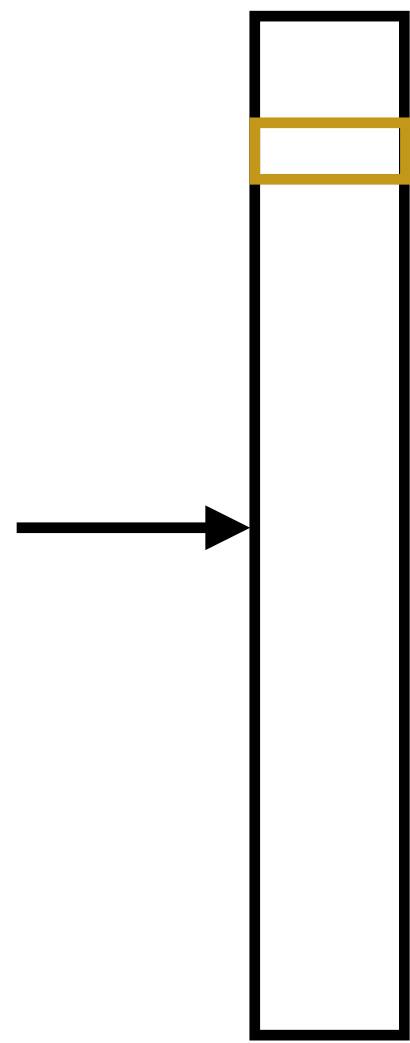
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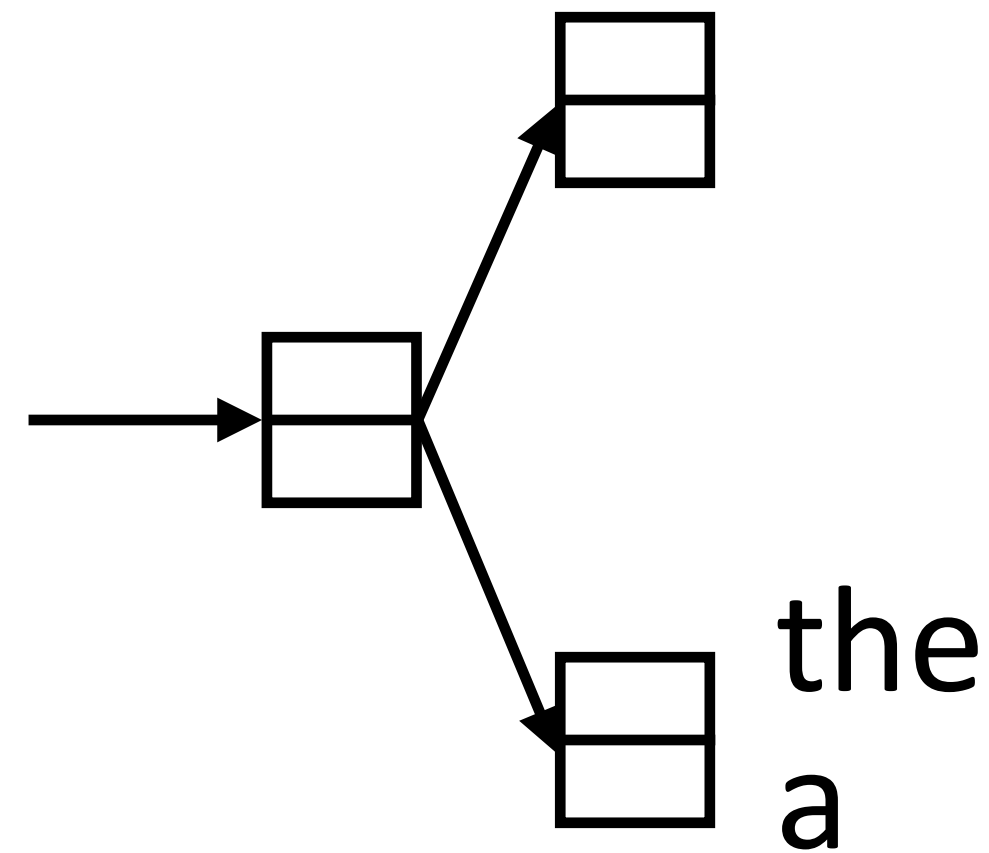
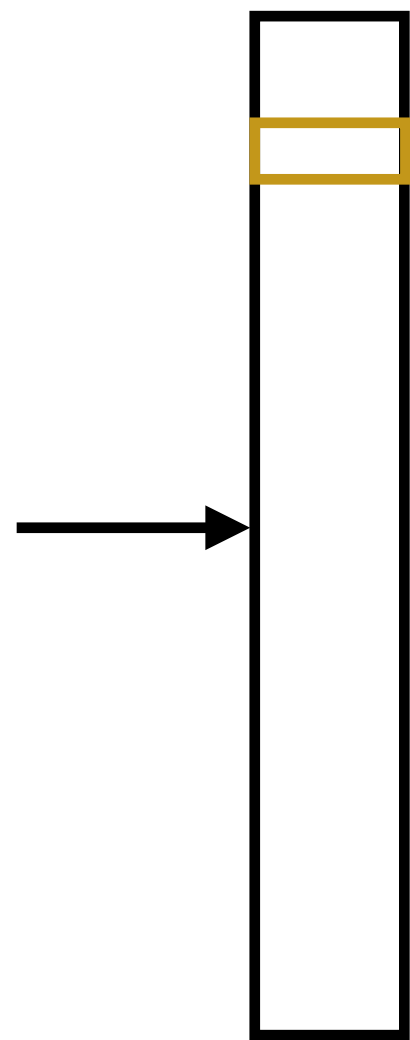
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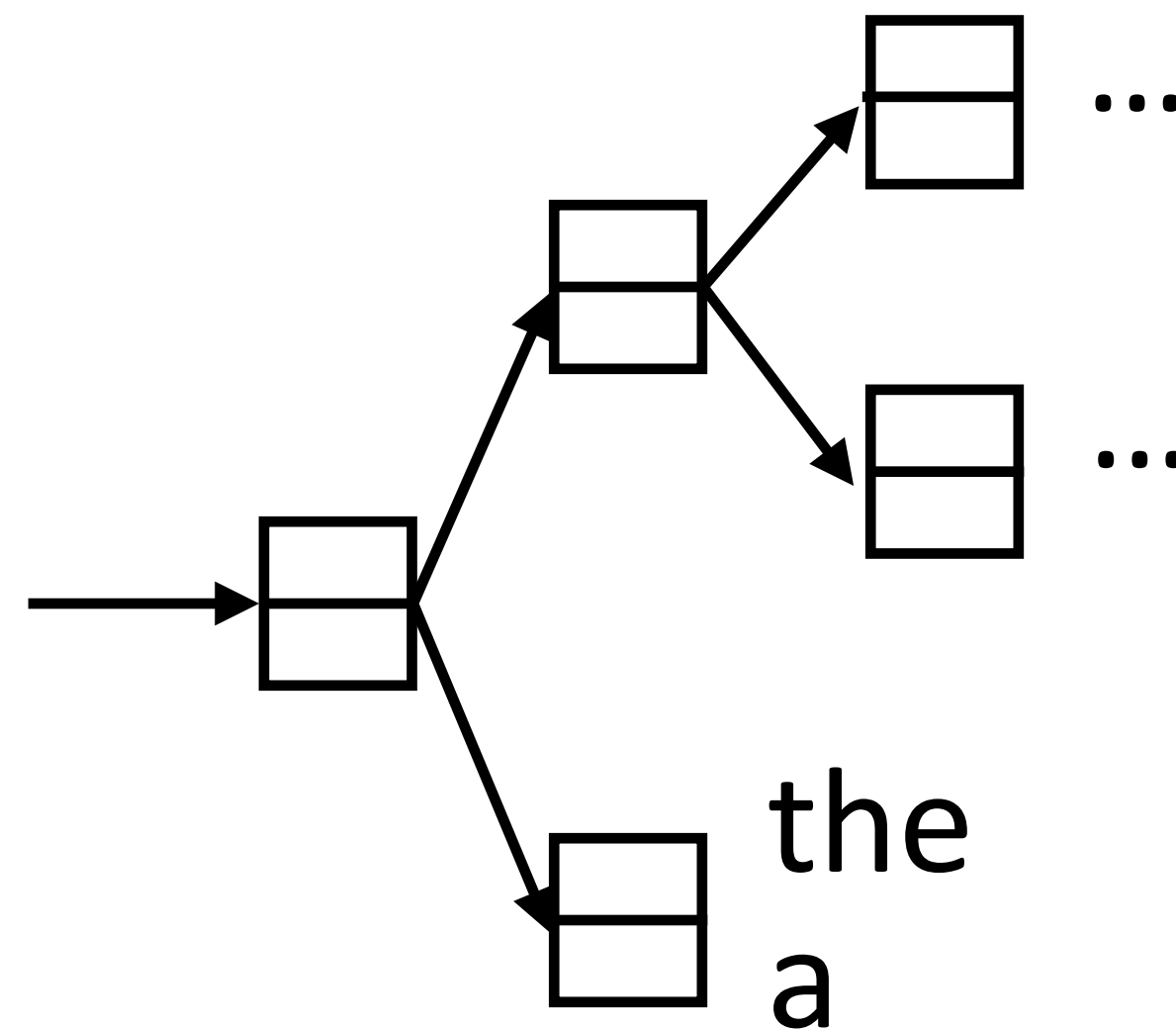
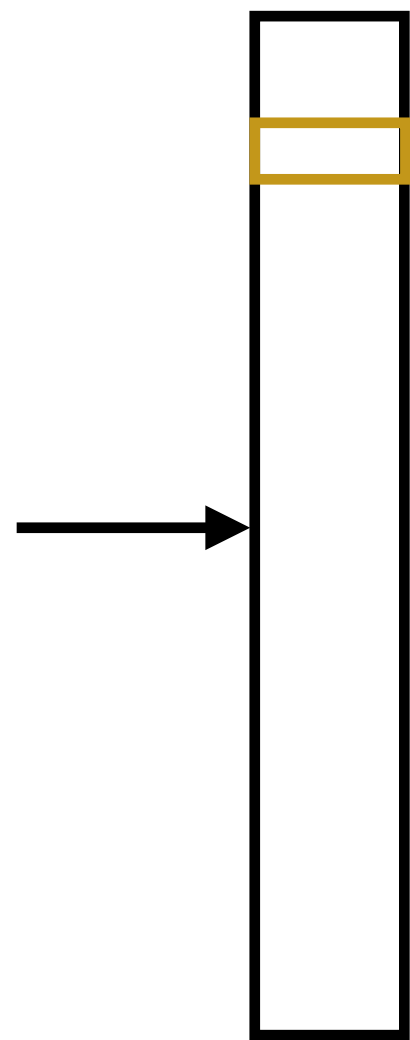


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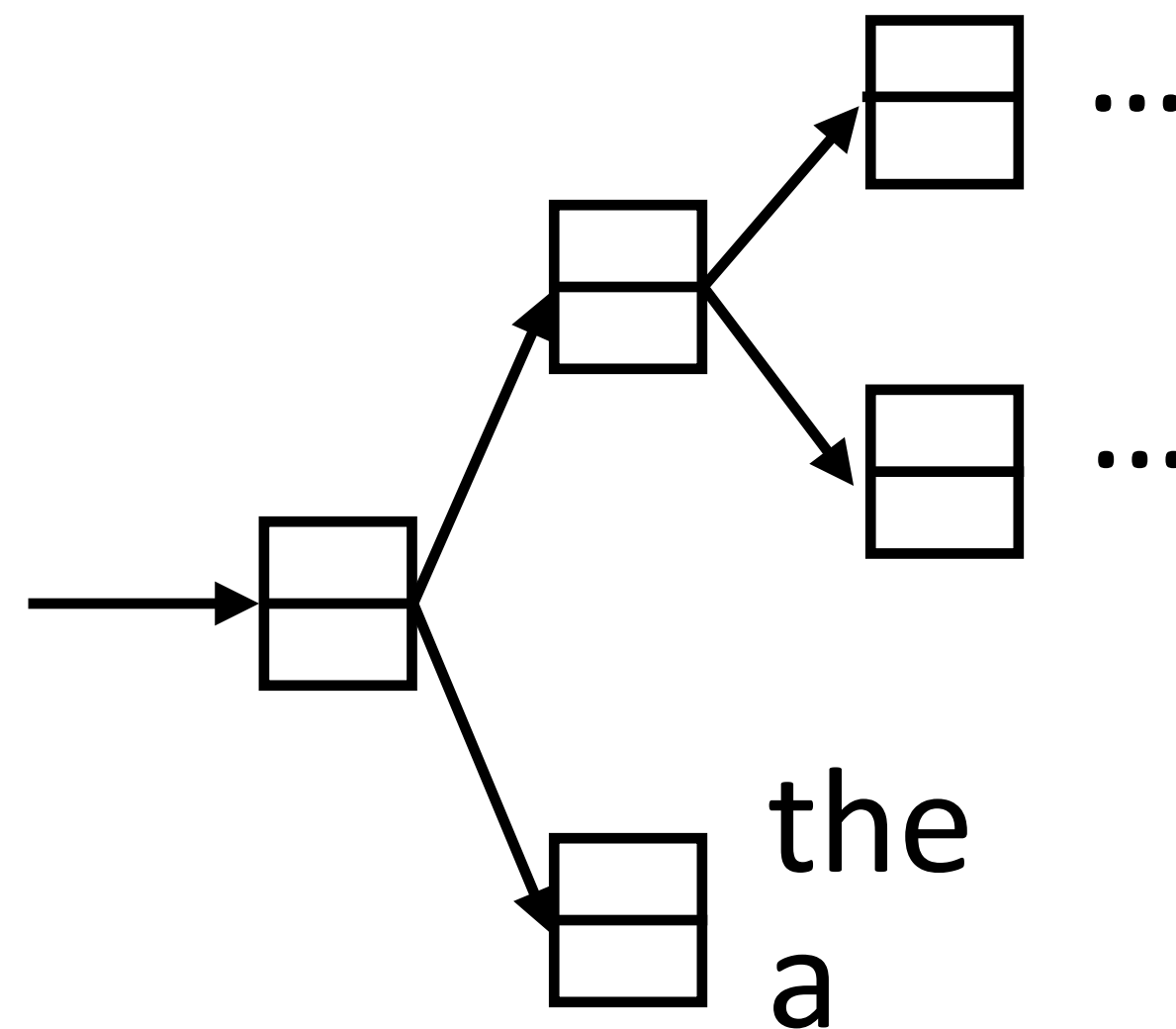
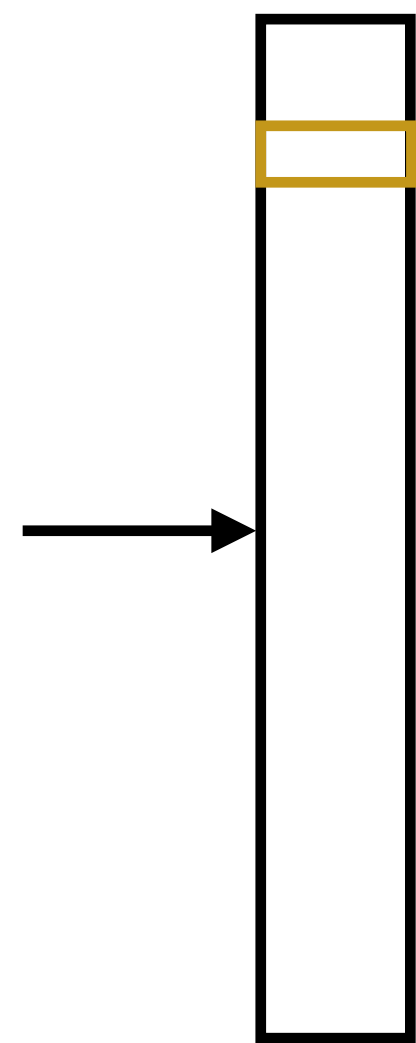


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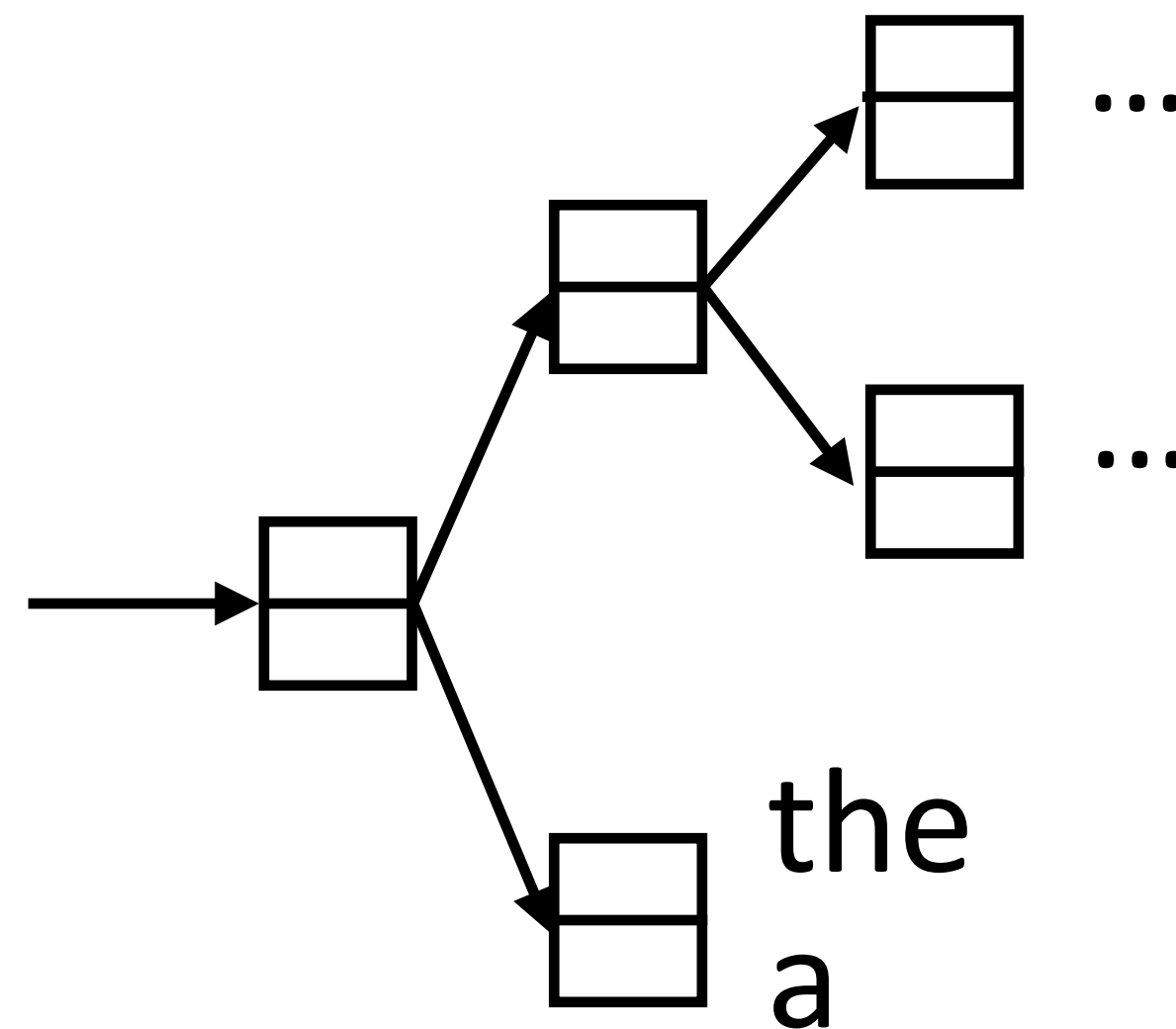
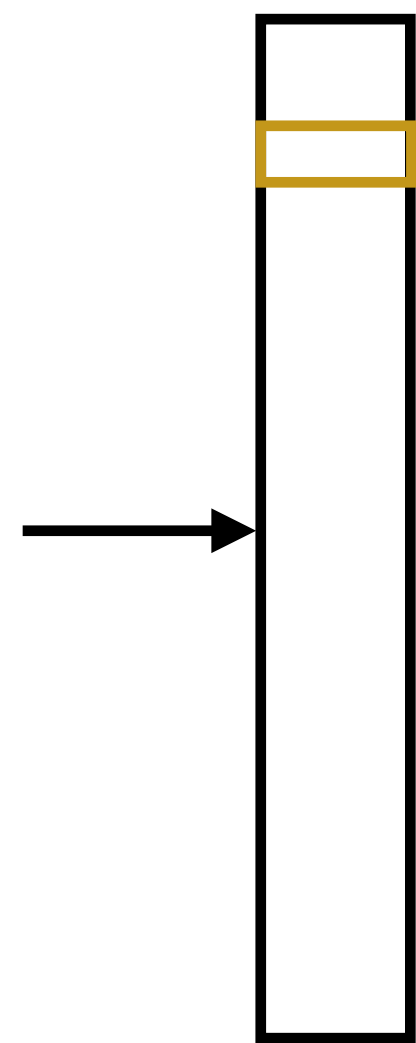
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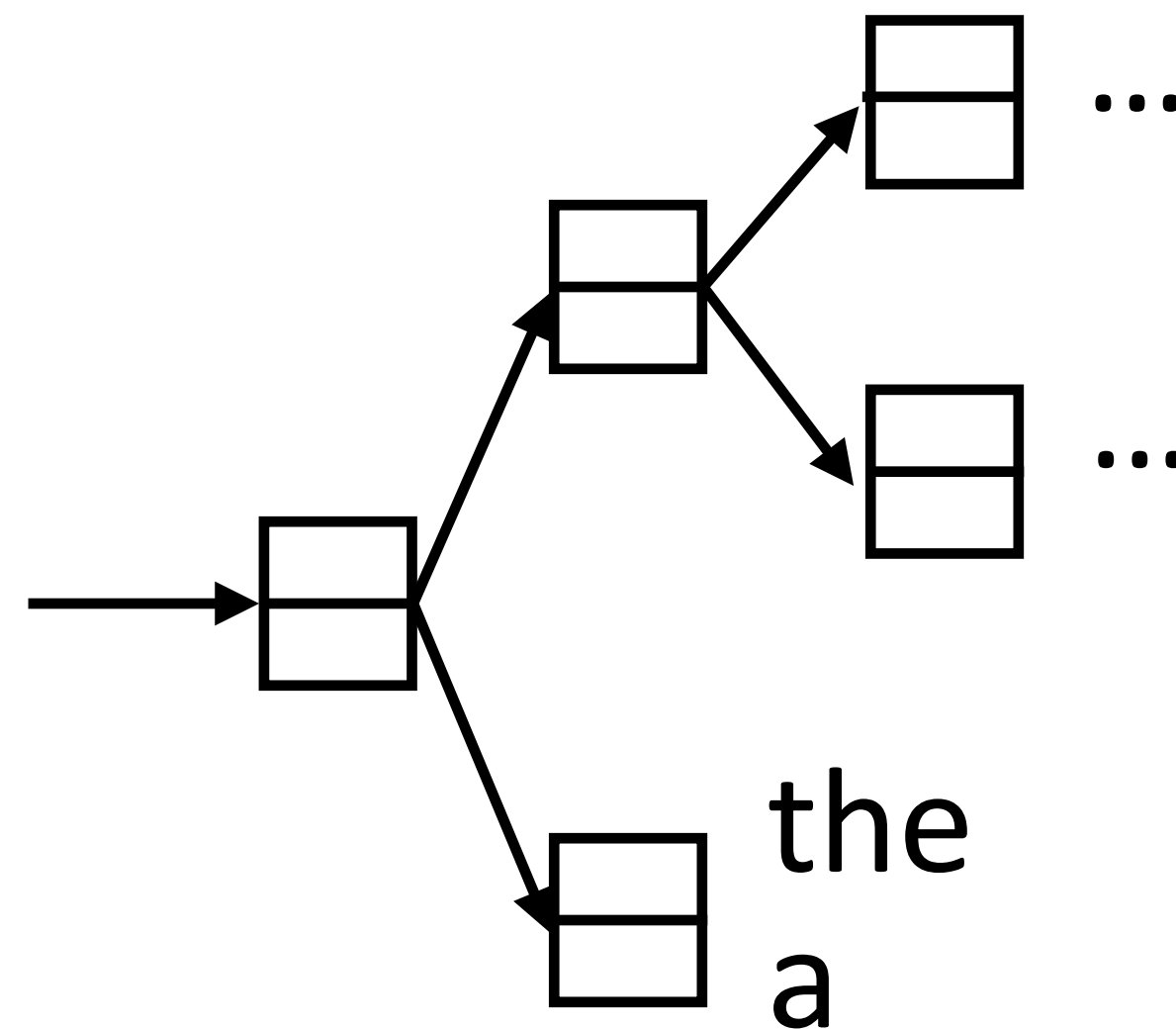
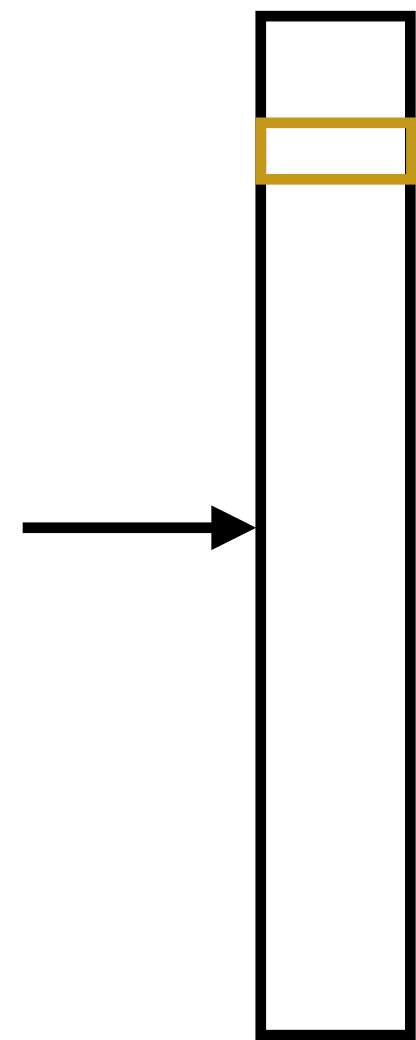
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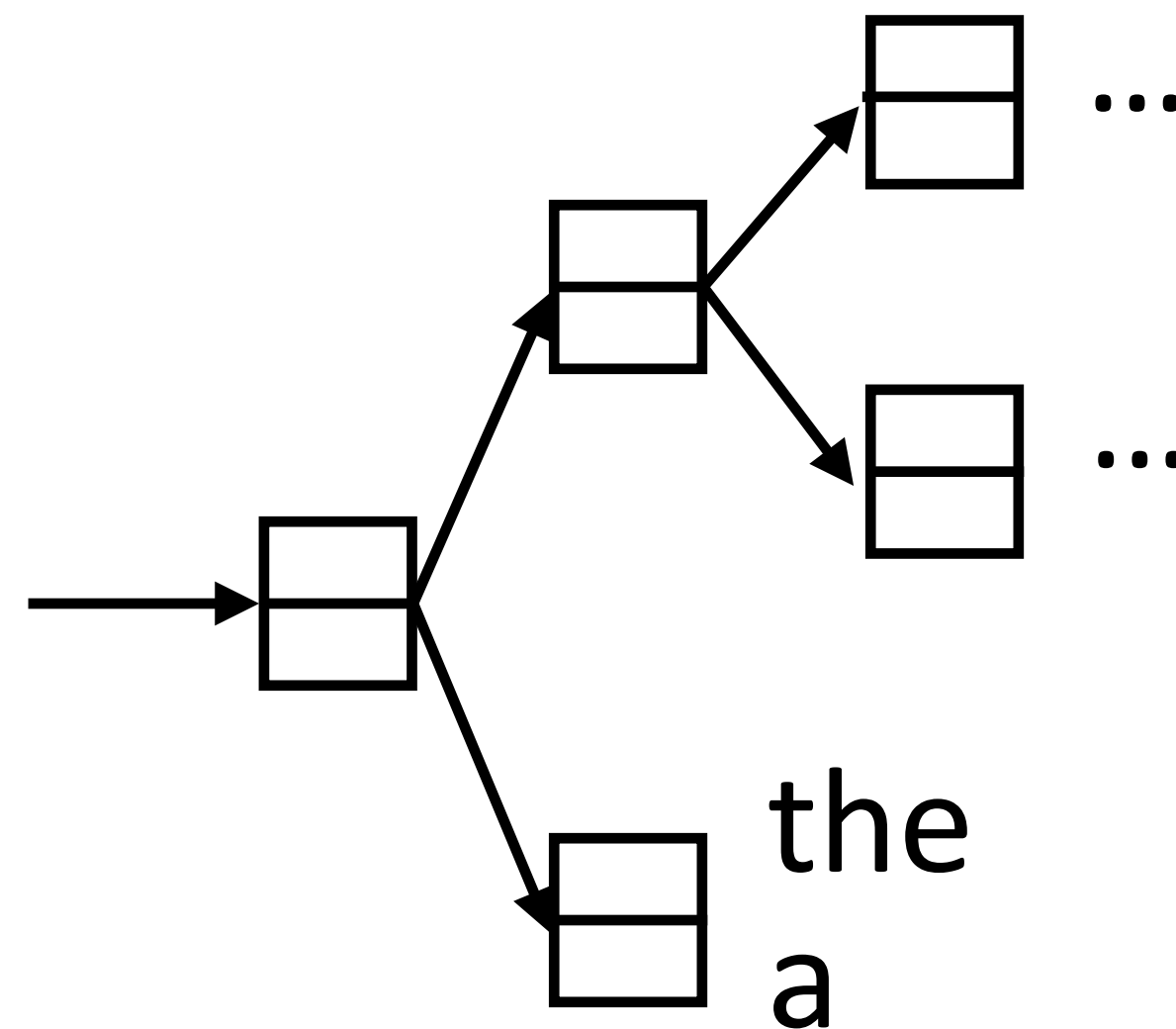
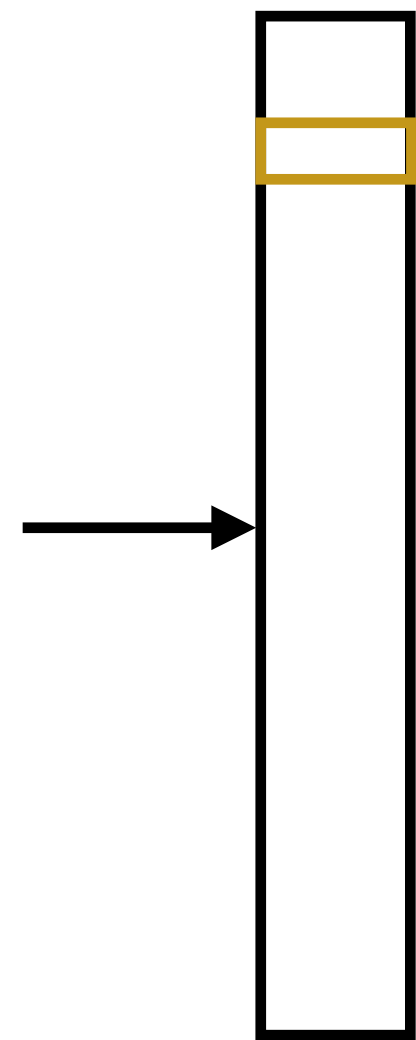
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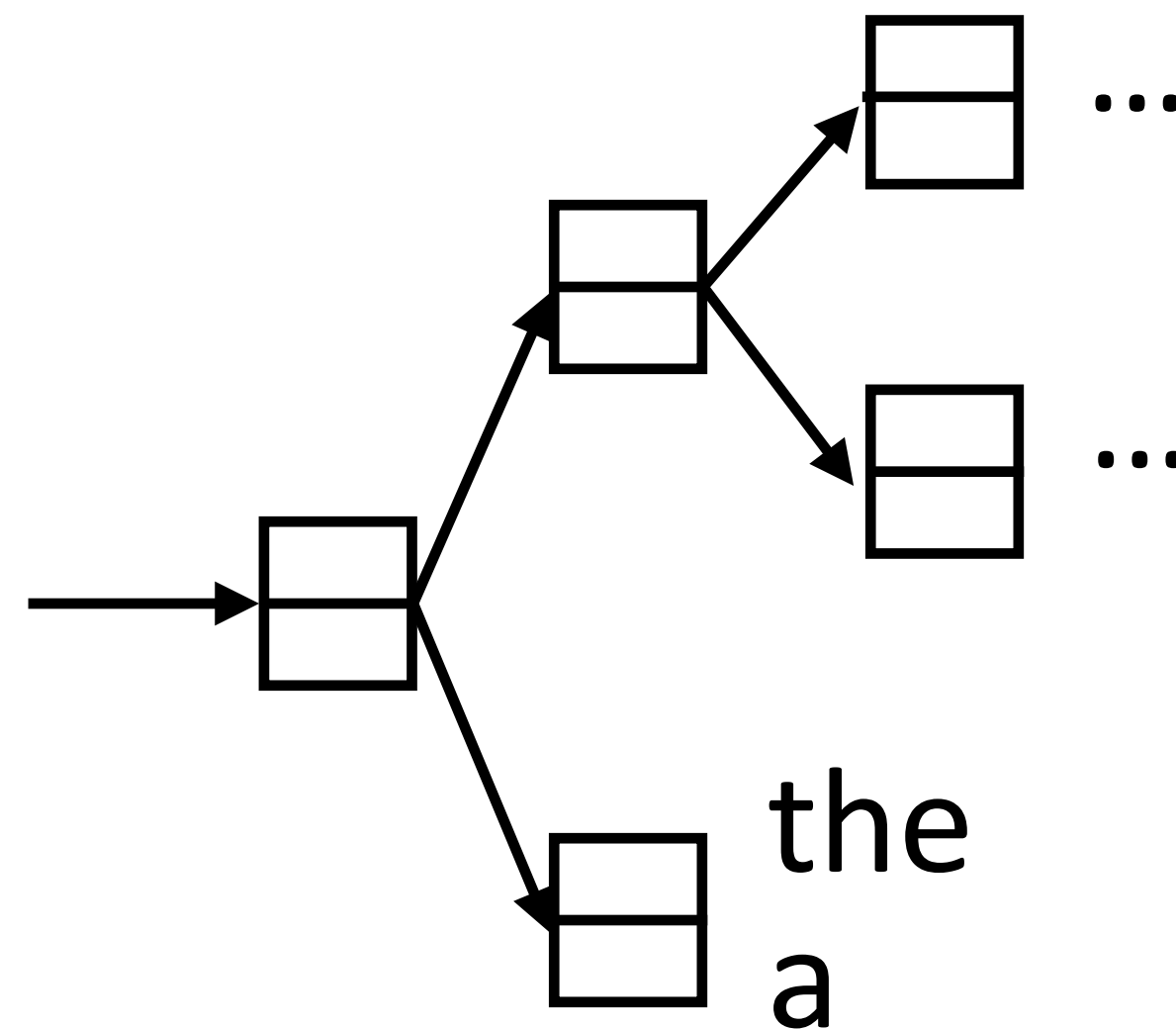
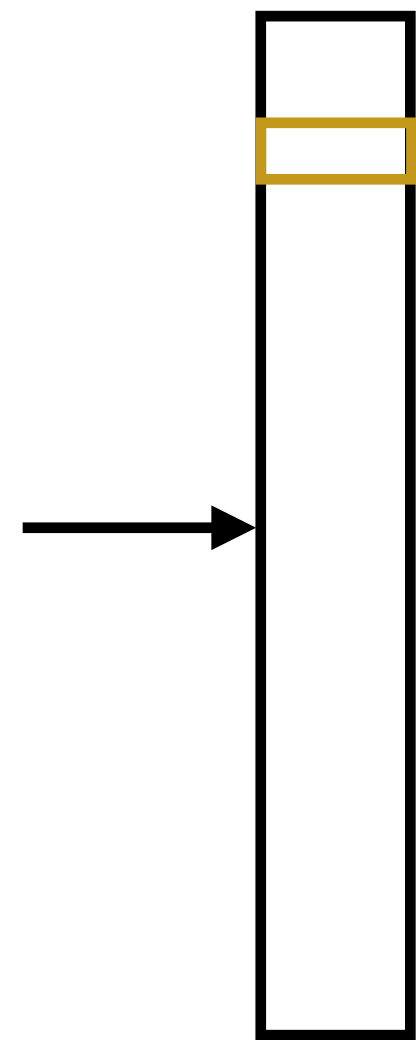
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Mikolov et al. (2013)

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Mikolov et al. (2013)

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sampled

Mikolov et al. (2013)

# Connections with Matrix Factorization

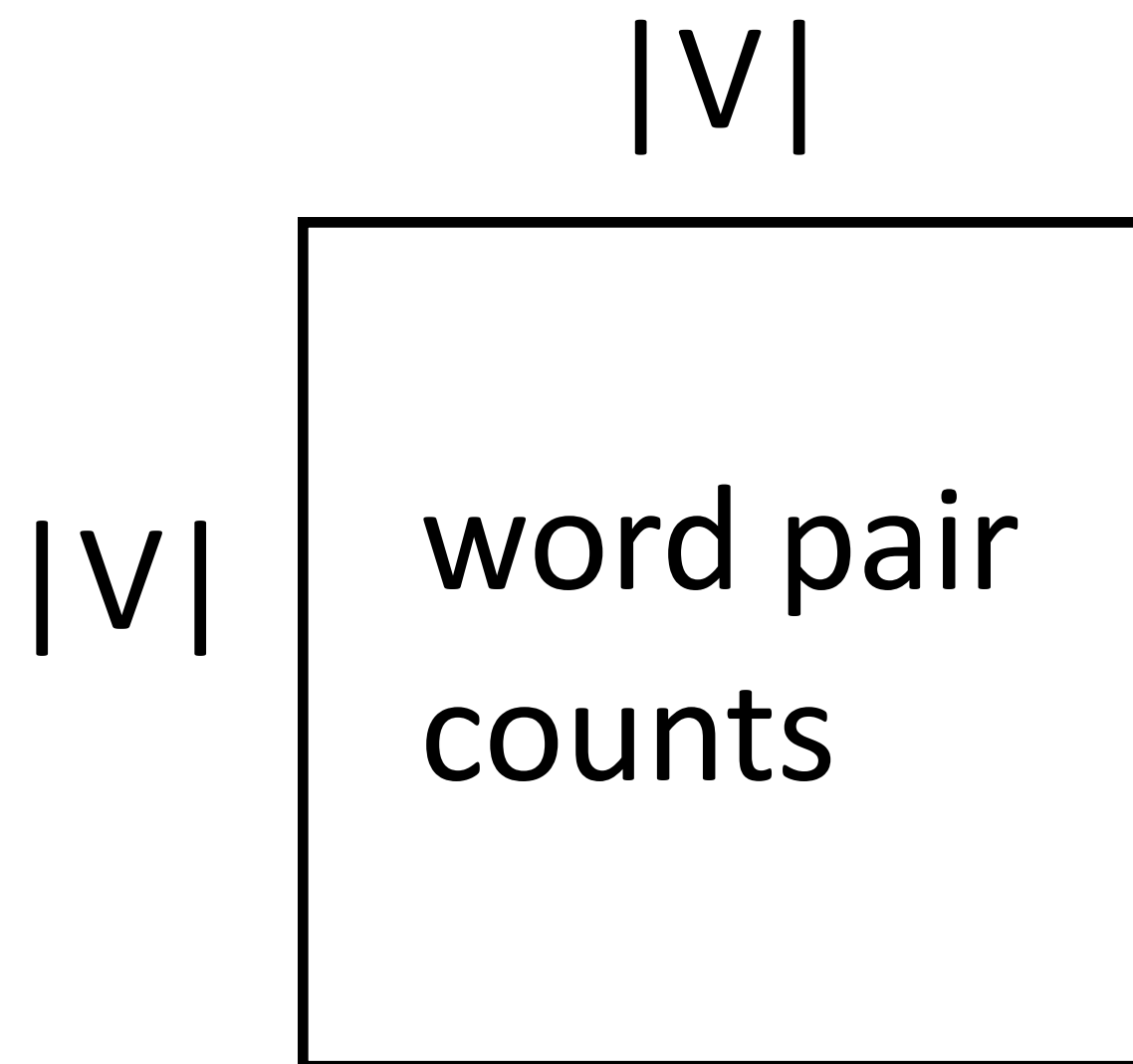
---

- ▶ Skip-gram model looks at word-word co-occurrences and produces two types of vectors

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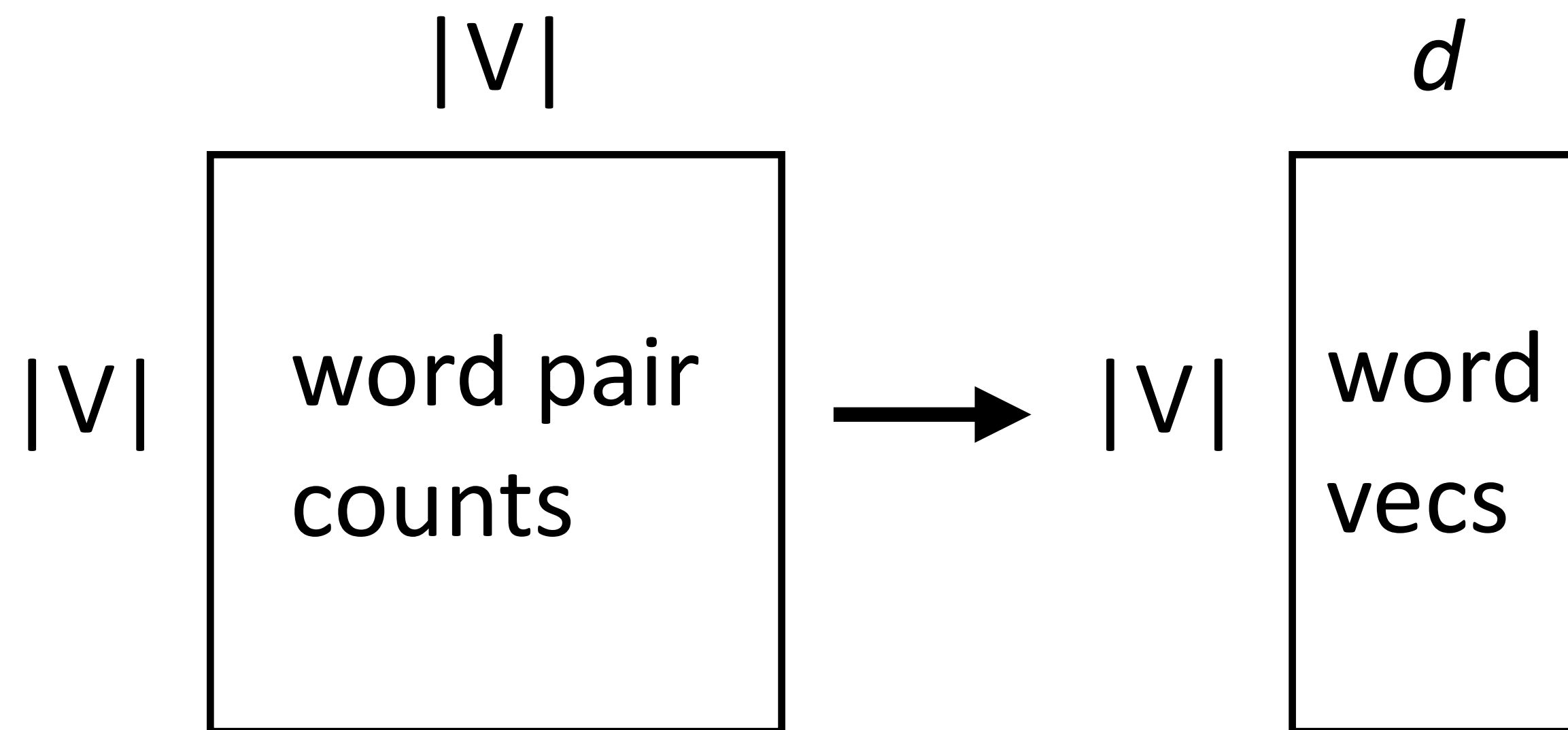
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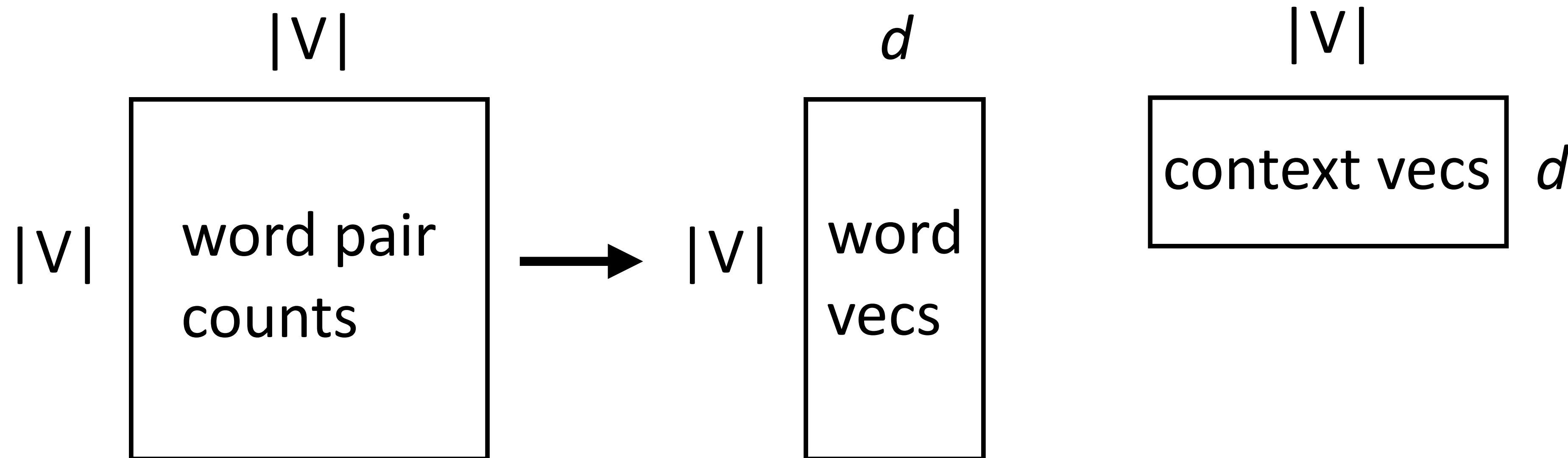




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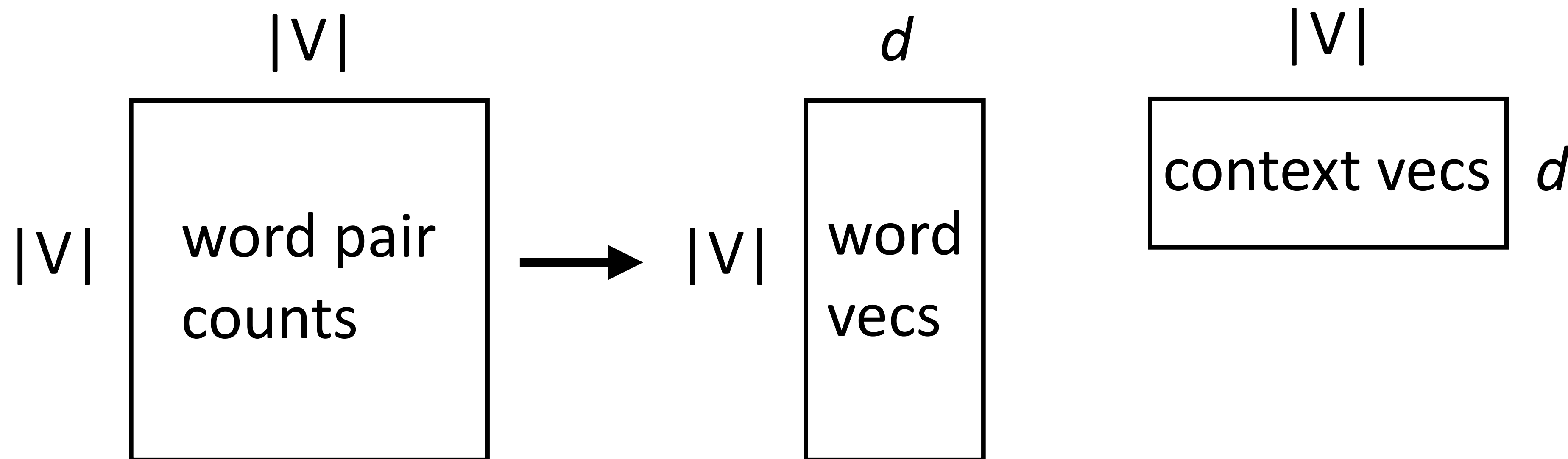
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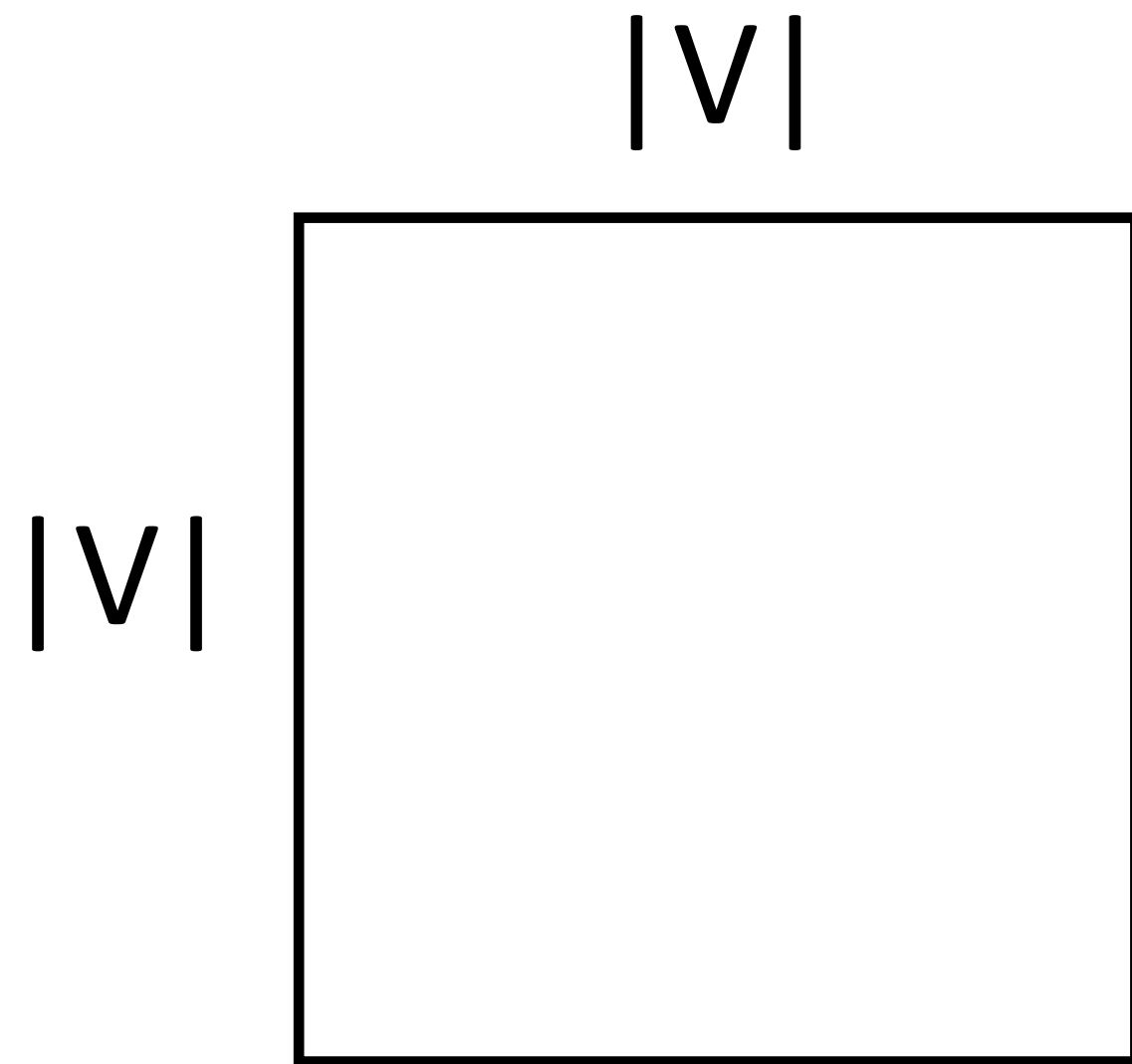
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- ▶ Looks almost like a matrix factorization...can we interpret it this way?

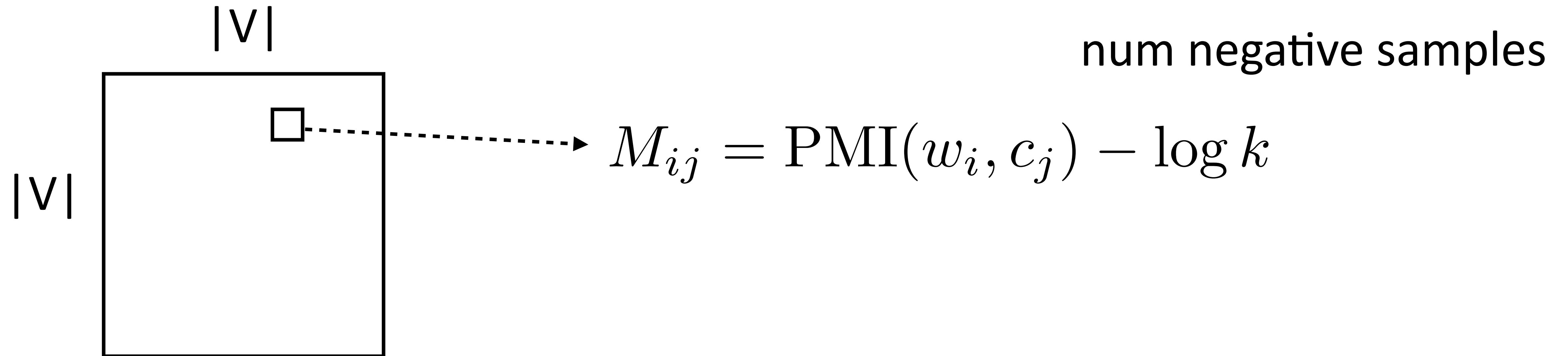
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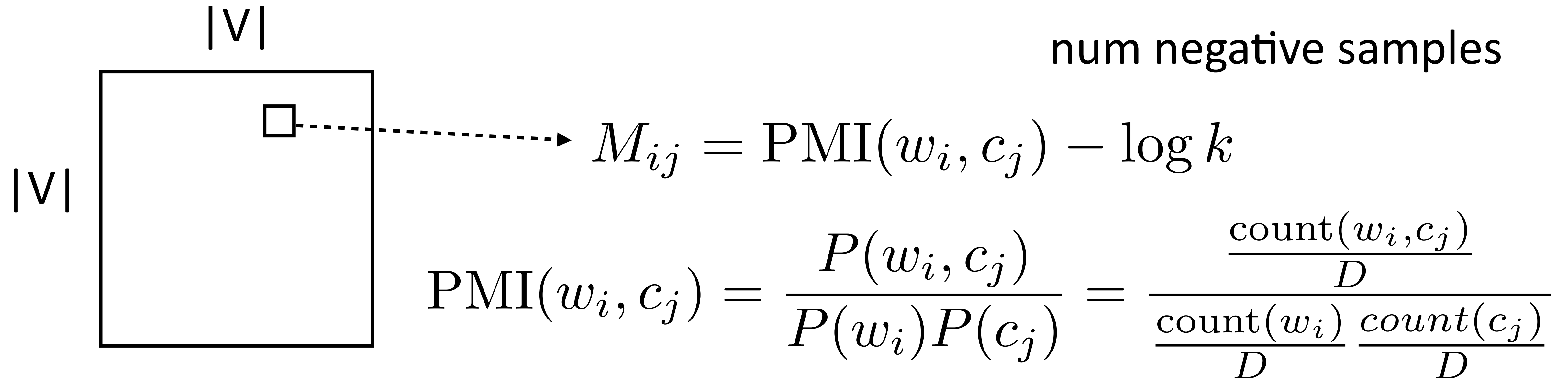
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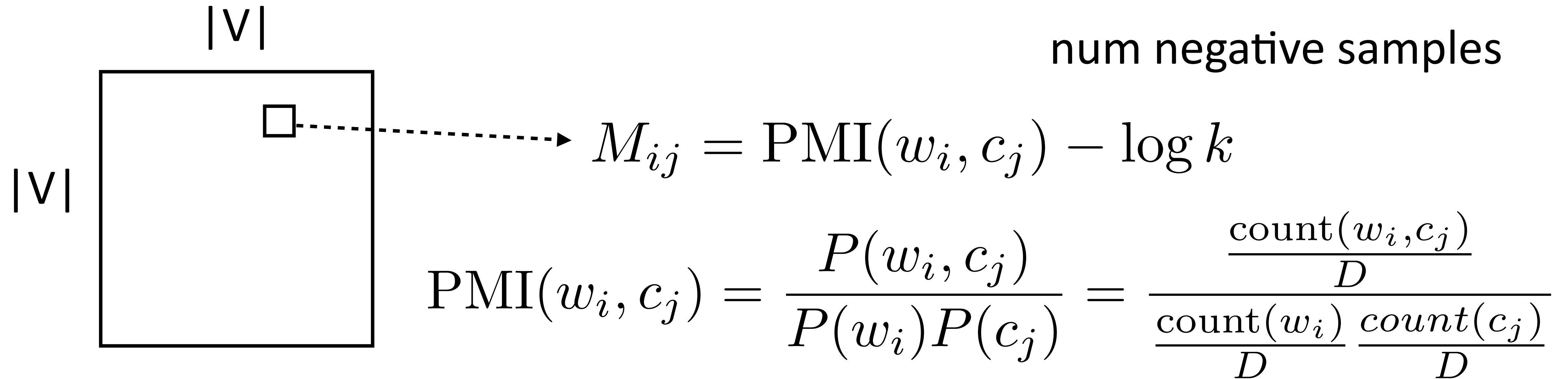
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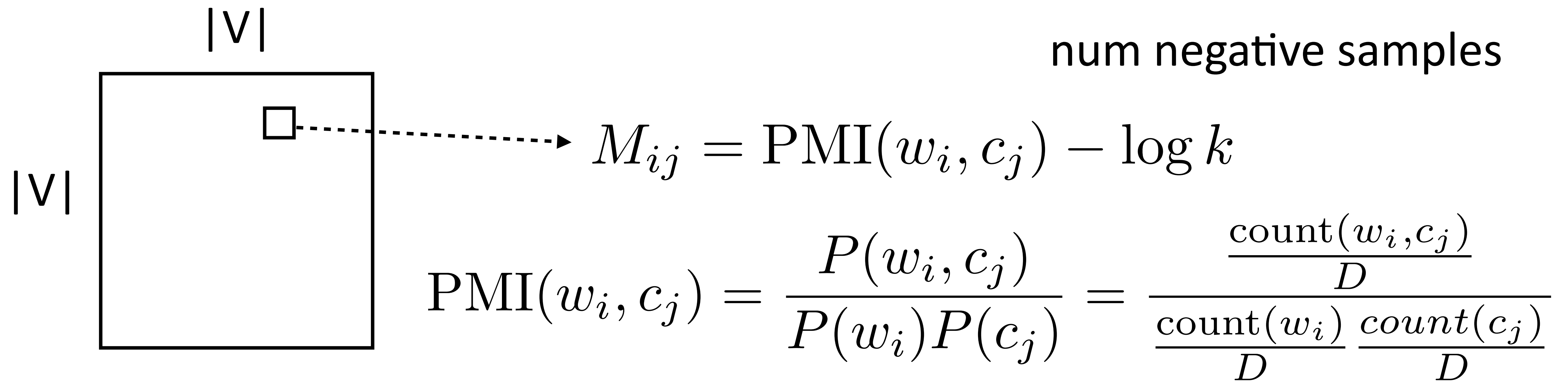
# Skip-Gram as Matrix Factorization

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Skip-gram objective *exactly* corresponds to factoring this matrix:

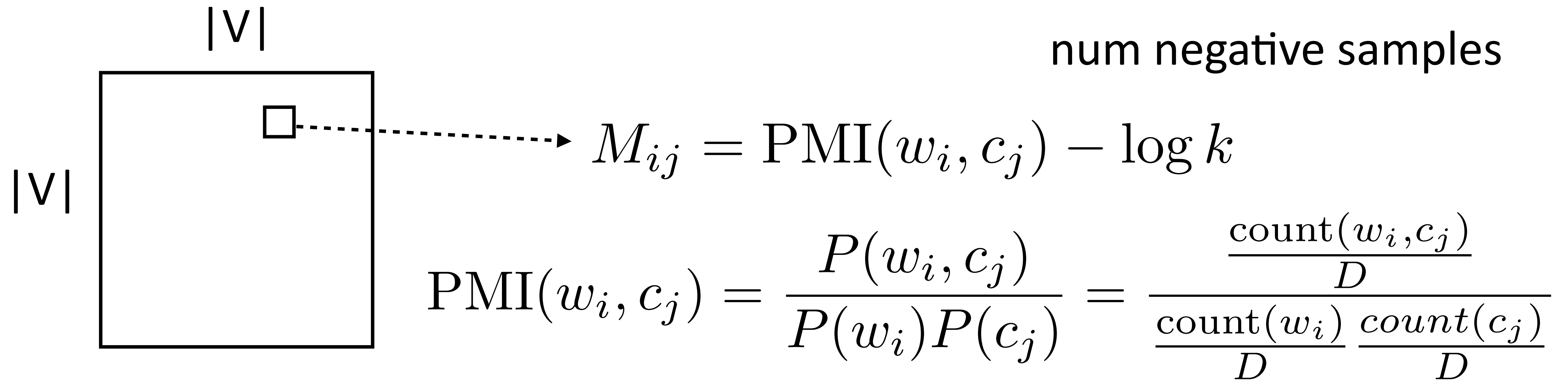
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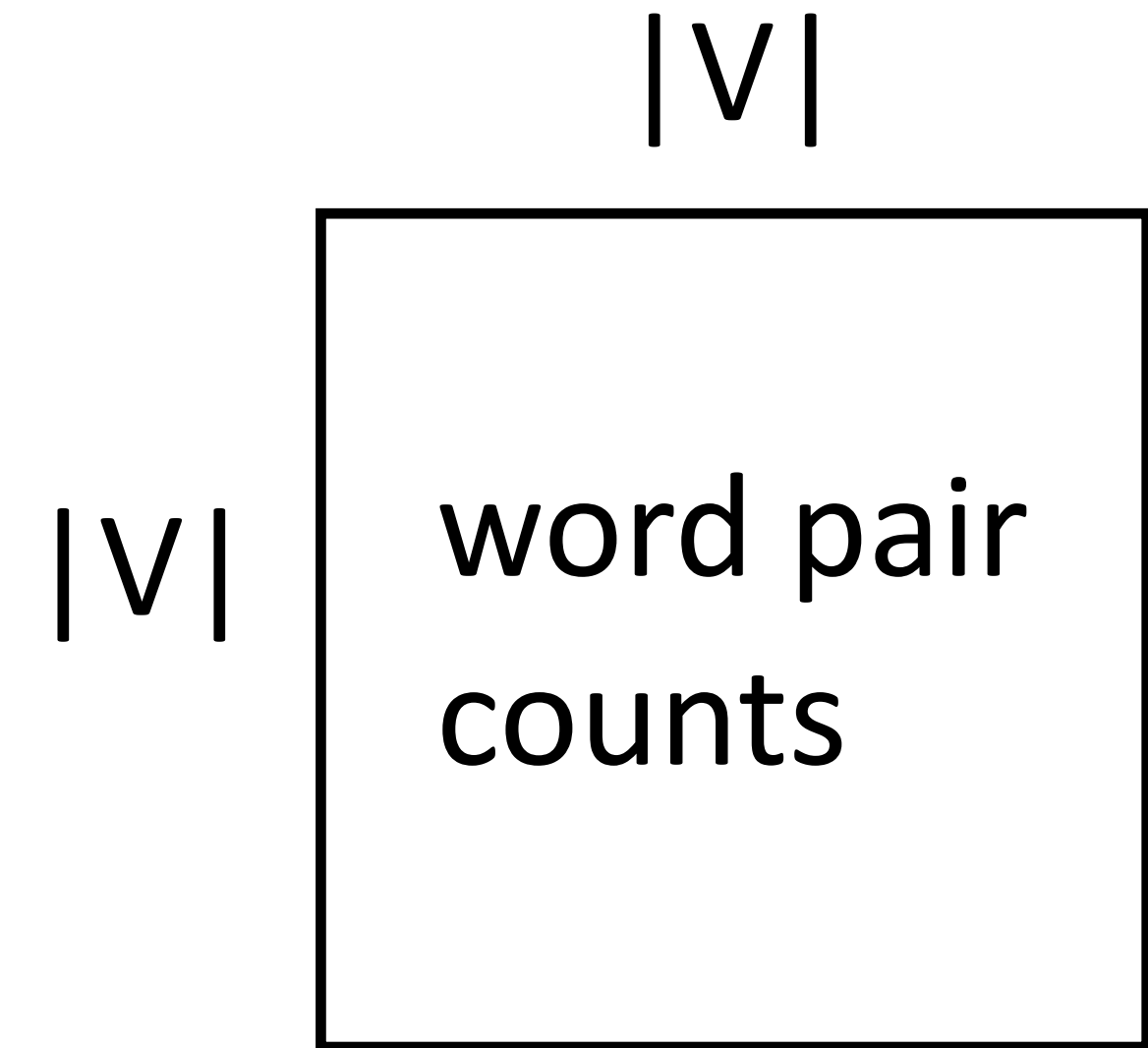
- ▶ *If* we sample negative examples from the uniform distribution over words
- ▶ ...and it's a *weighted* factorization problem (weighted by word freq)



# GloVe (Global Vectors)

---

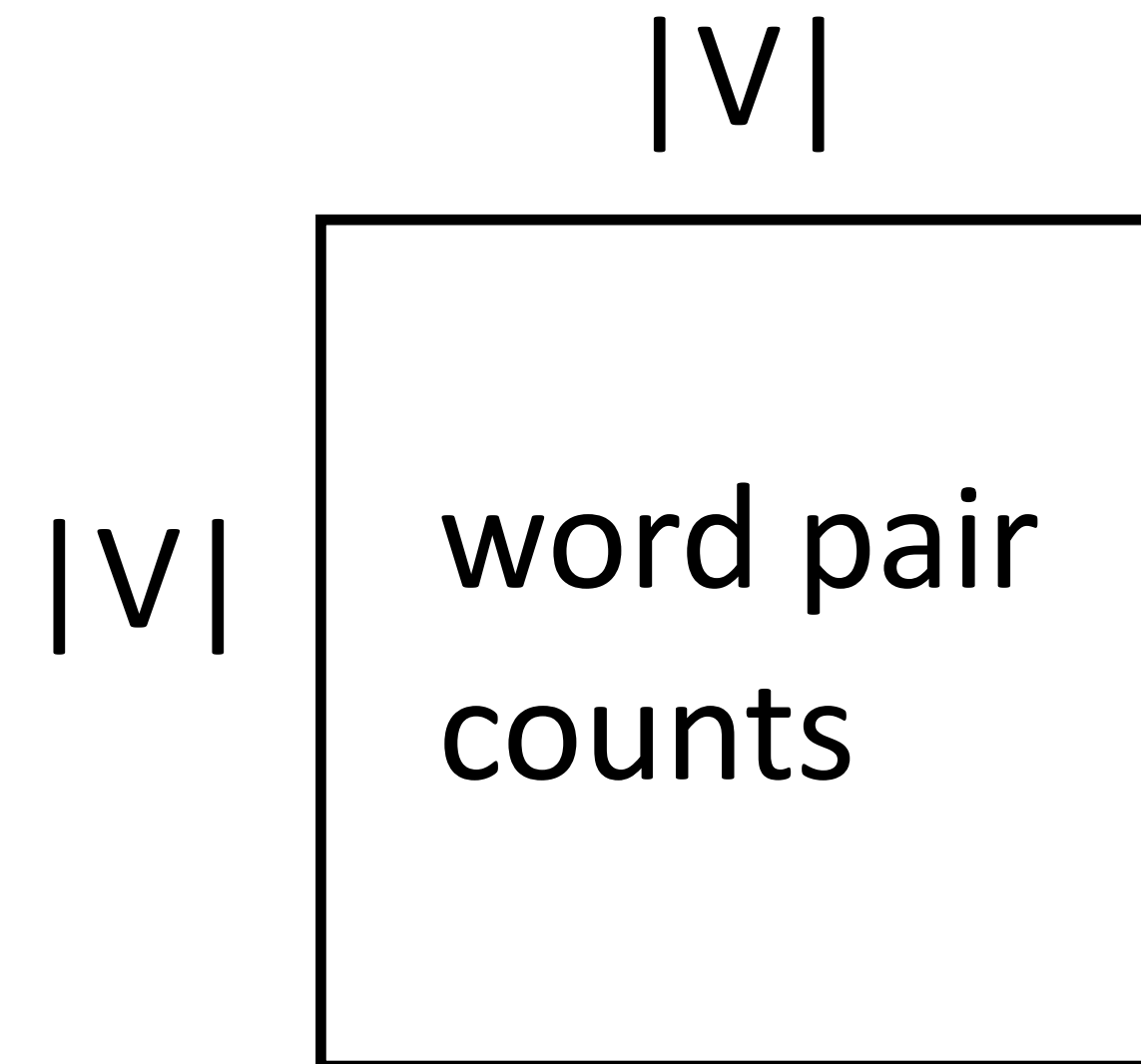
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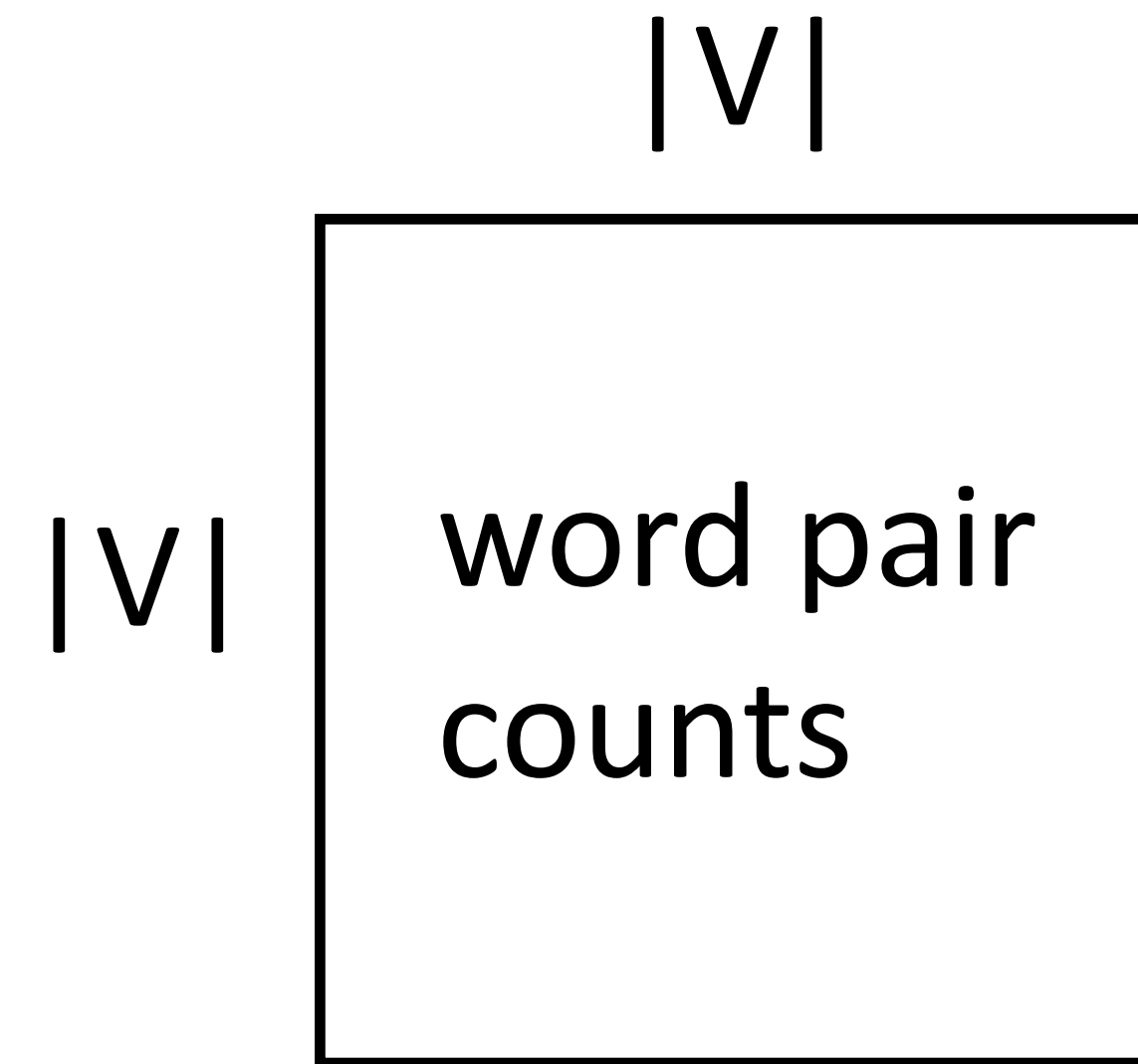


- ▶ **Loss**  $= \sum_{i,j} f(\text{count}(w_i, c_j)) (w_i^\top c_j + a_i + b_j - \log \text{count}(w_i, c_j))^2$

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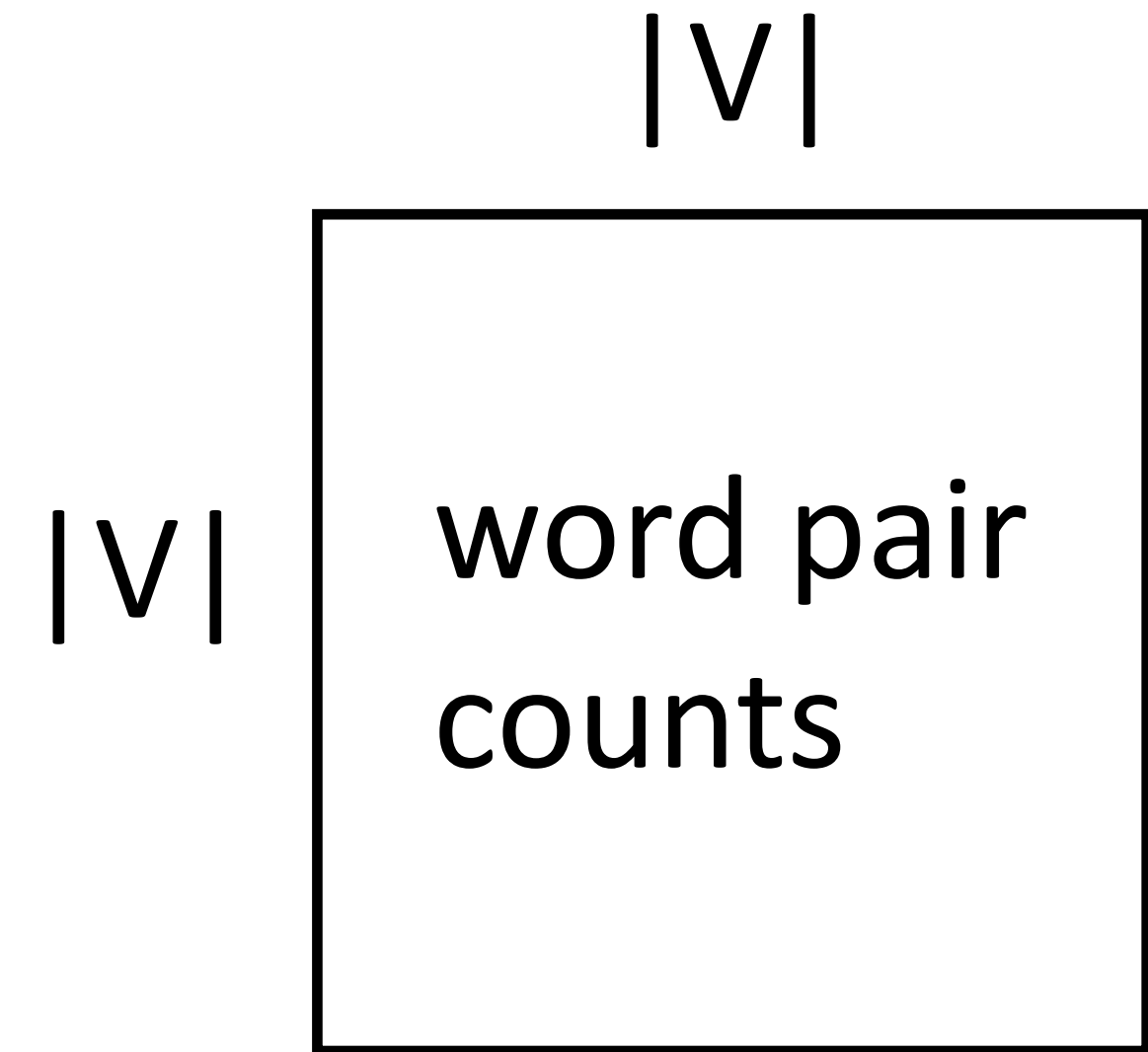


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- ▶ By far the most common (uncontextualized) word vectors used today (20,000+ citations)

# Preview: Context-dependent Embeddings

---

- ▶ How to handle different word senses? One vector for *balls*

they dance at balls

they hit the balls

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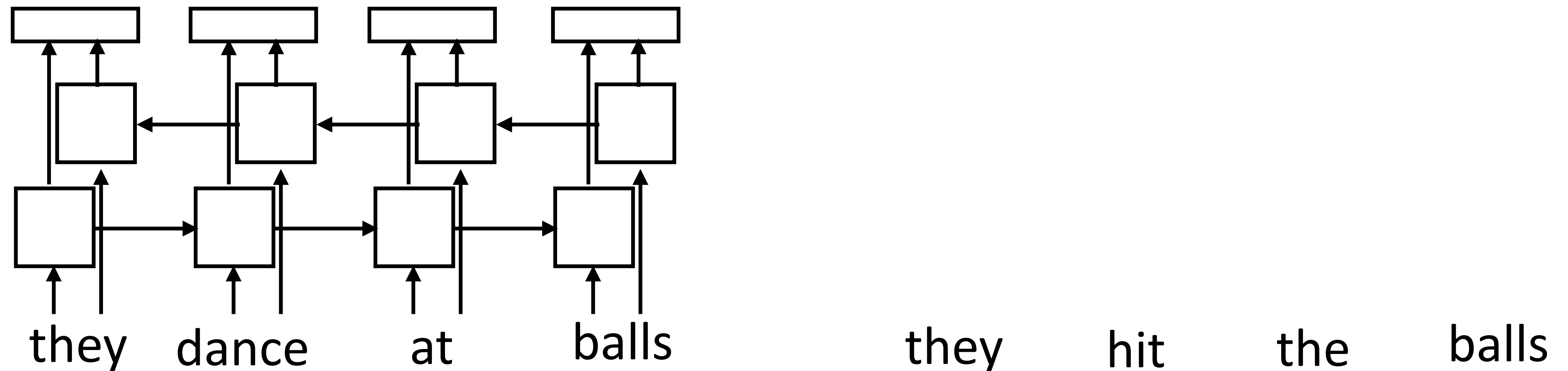
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- ▶ Train a neural language model to predict the next word given previous words in the sentence, use its internal representations as word vectors

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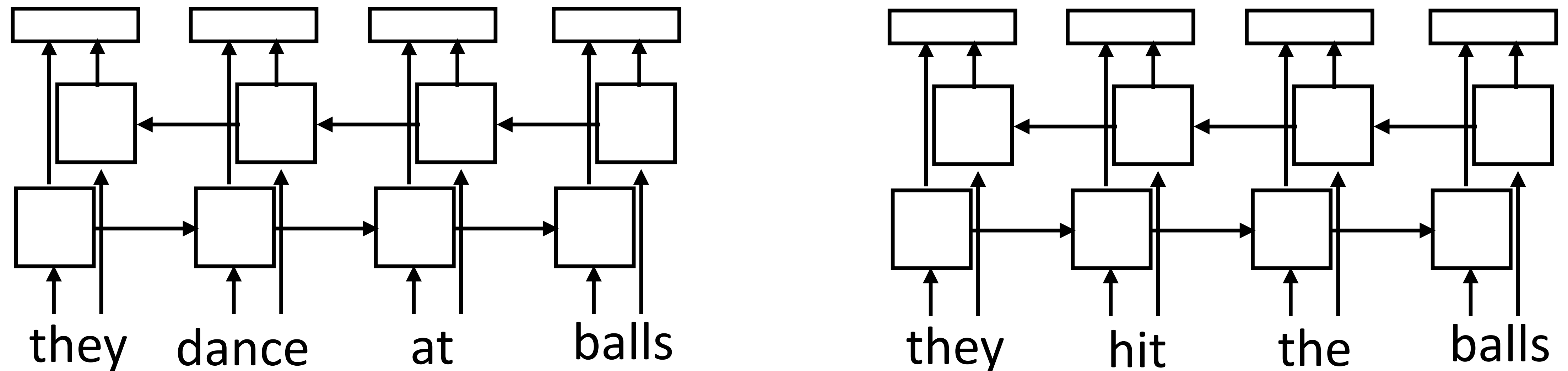
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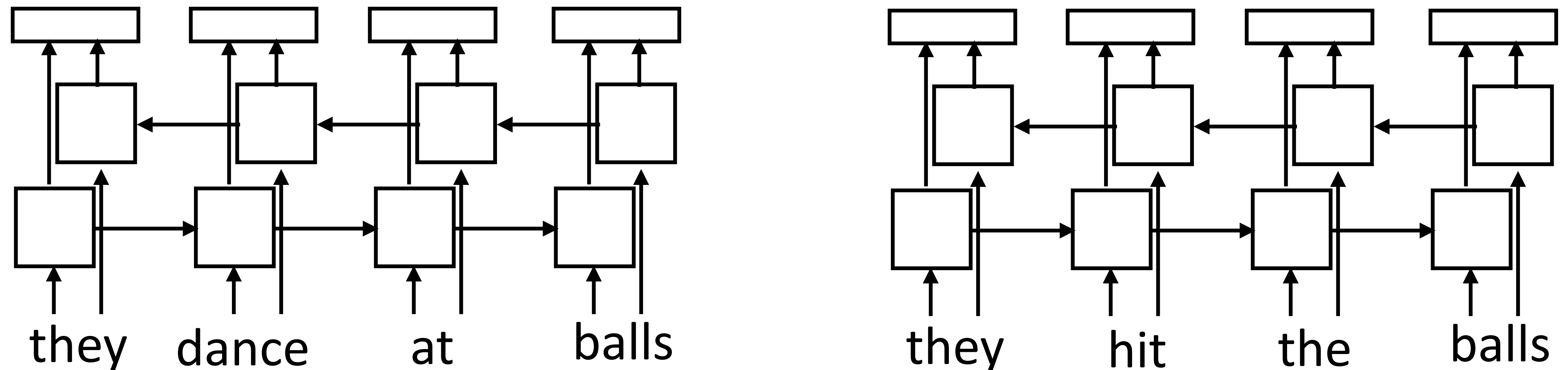


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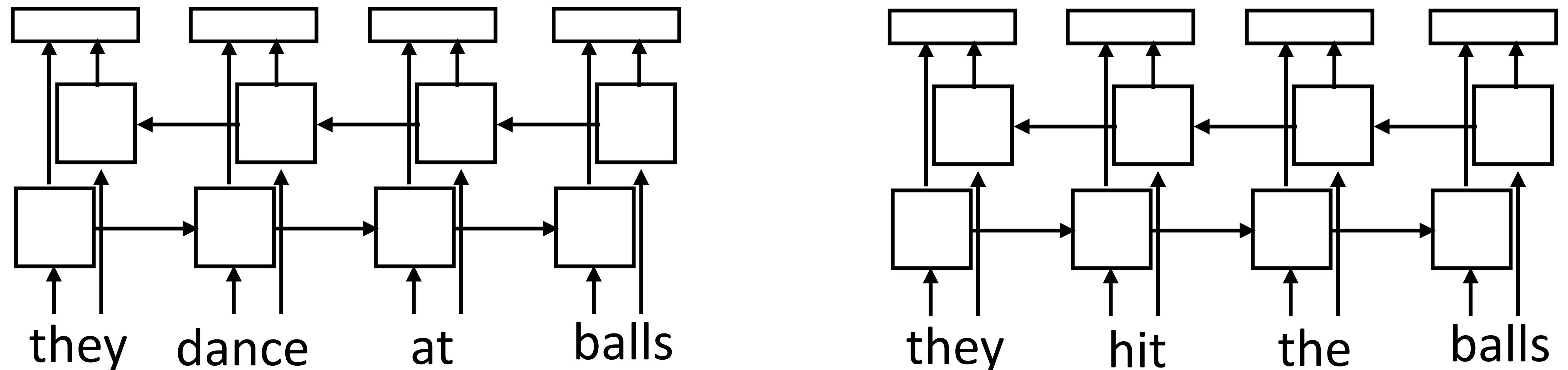
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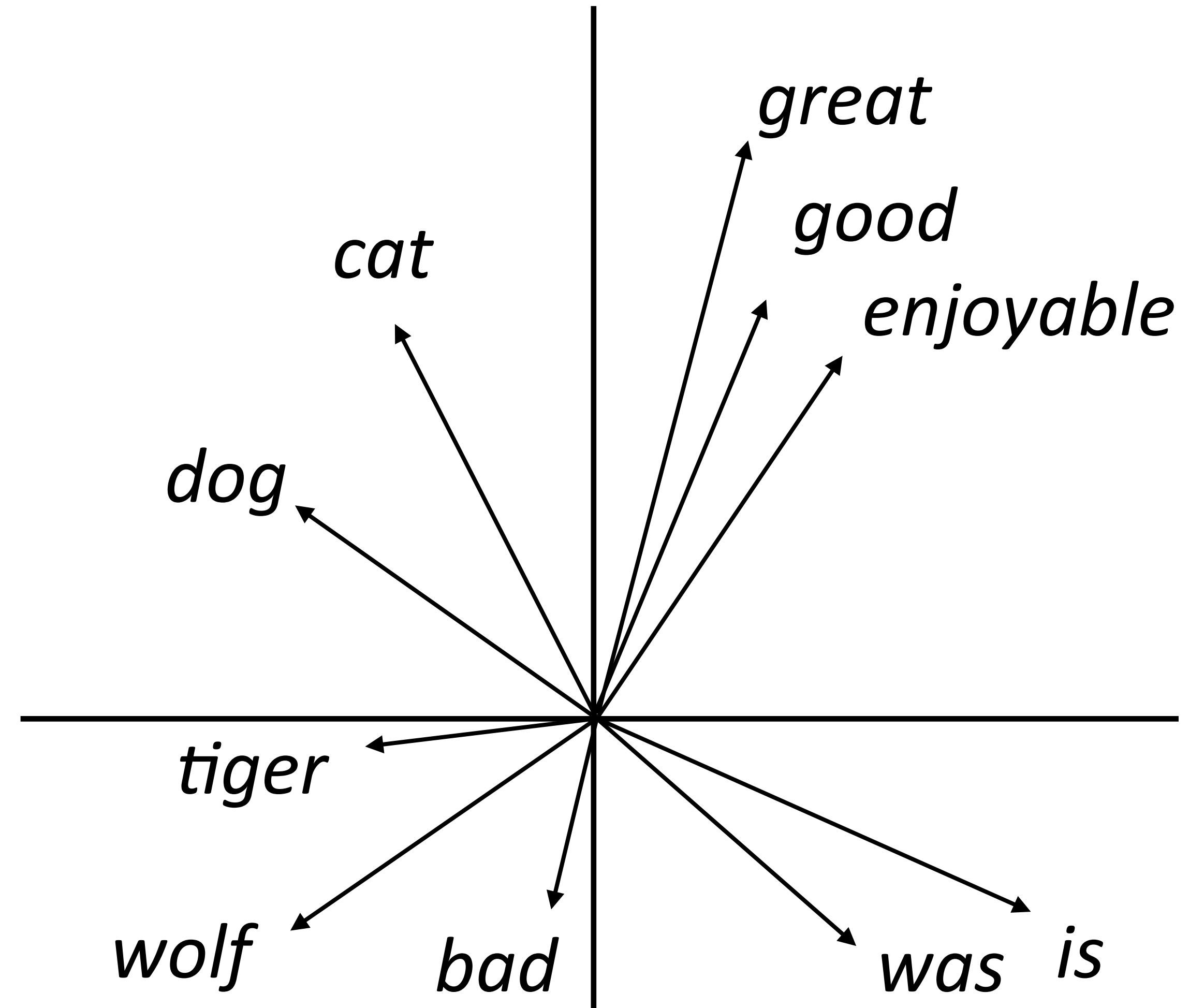
- ▶ Train a neural language model to predict the next word given previous words in the sentence, use its internal representations as word vectors
- ▶ *Context-sensitive* word embeddings: depend on rest of the sentence
- ▶ *Huge* improvements across nearly all NLP tasks over GloVe

# Evaluation

# Evaluating Word Embeddings

---

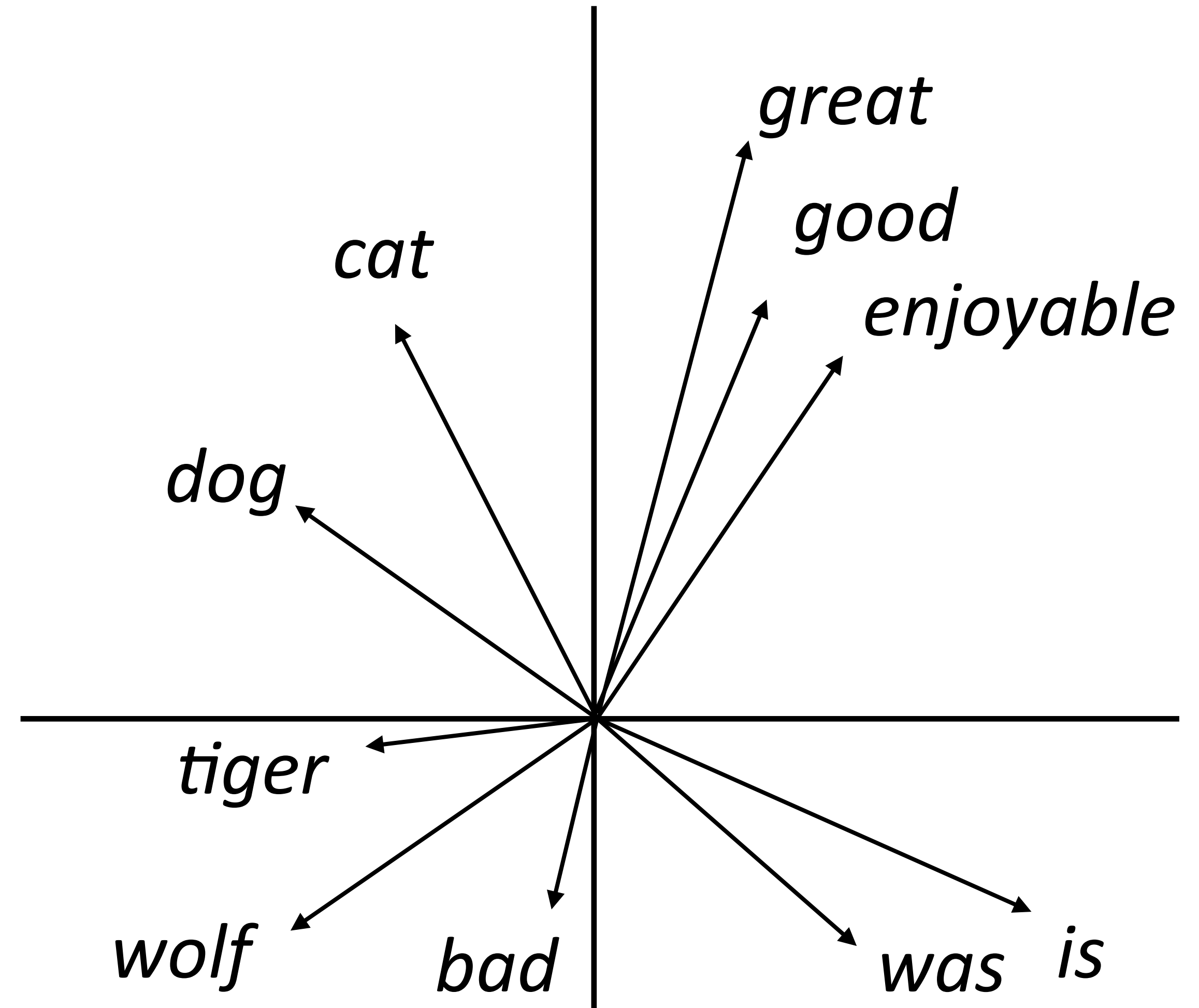
- ▶ What properties of language should word embeddings capture?



# Evaluating Word Embeddings

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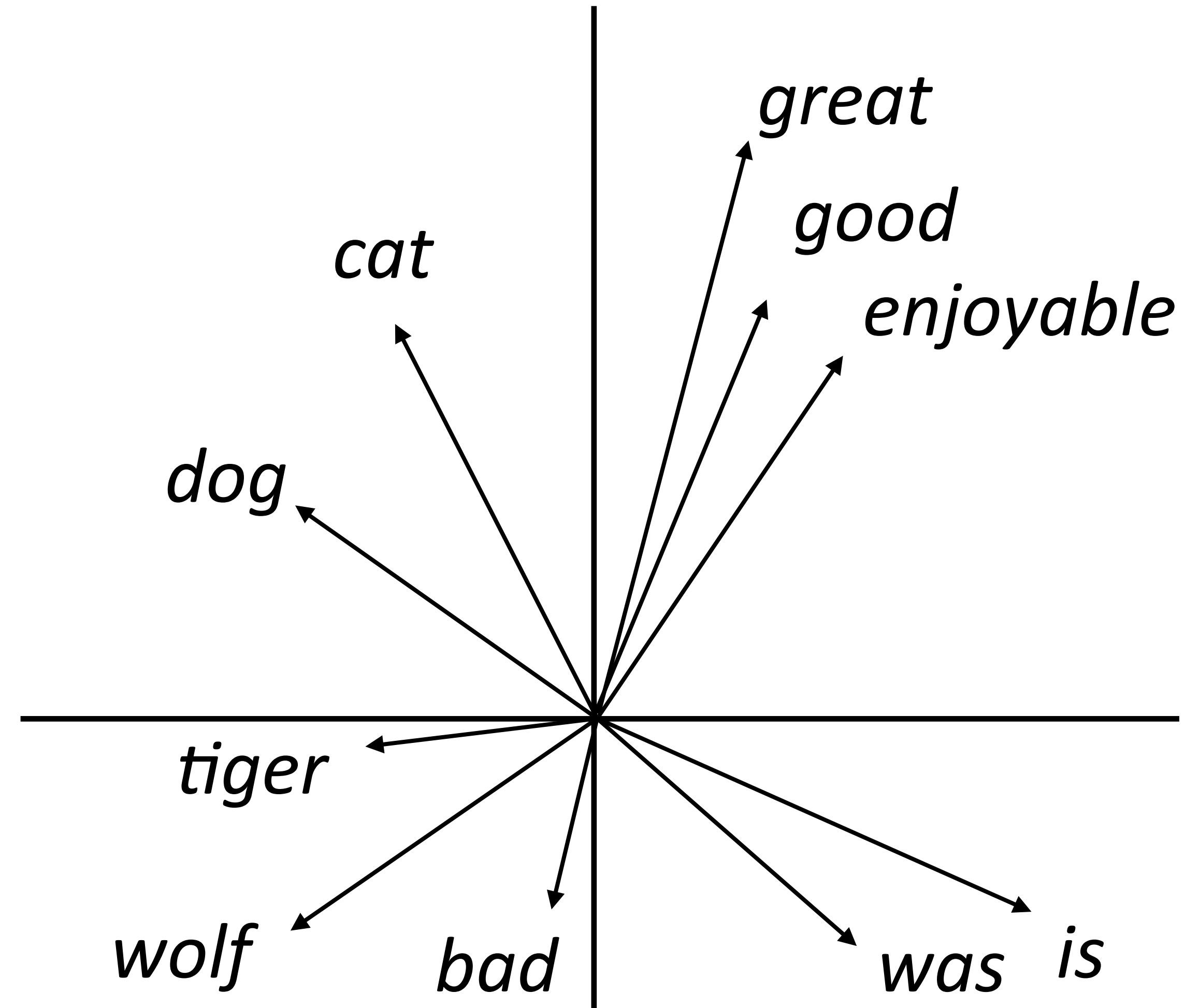
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# Evaluating Word Embeddings

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# Evaluating Word Embeddings

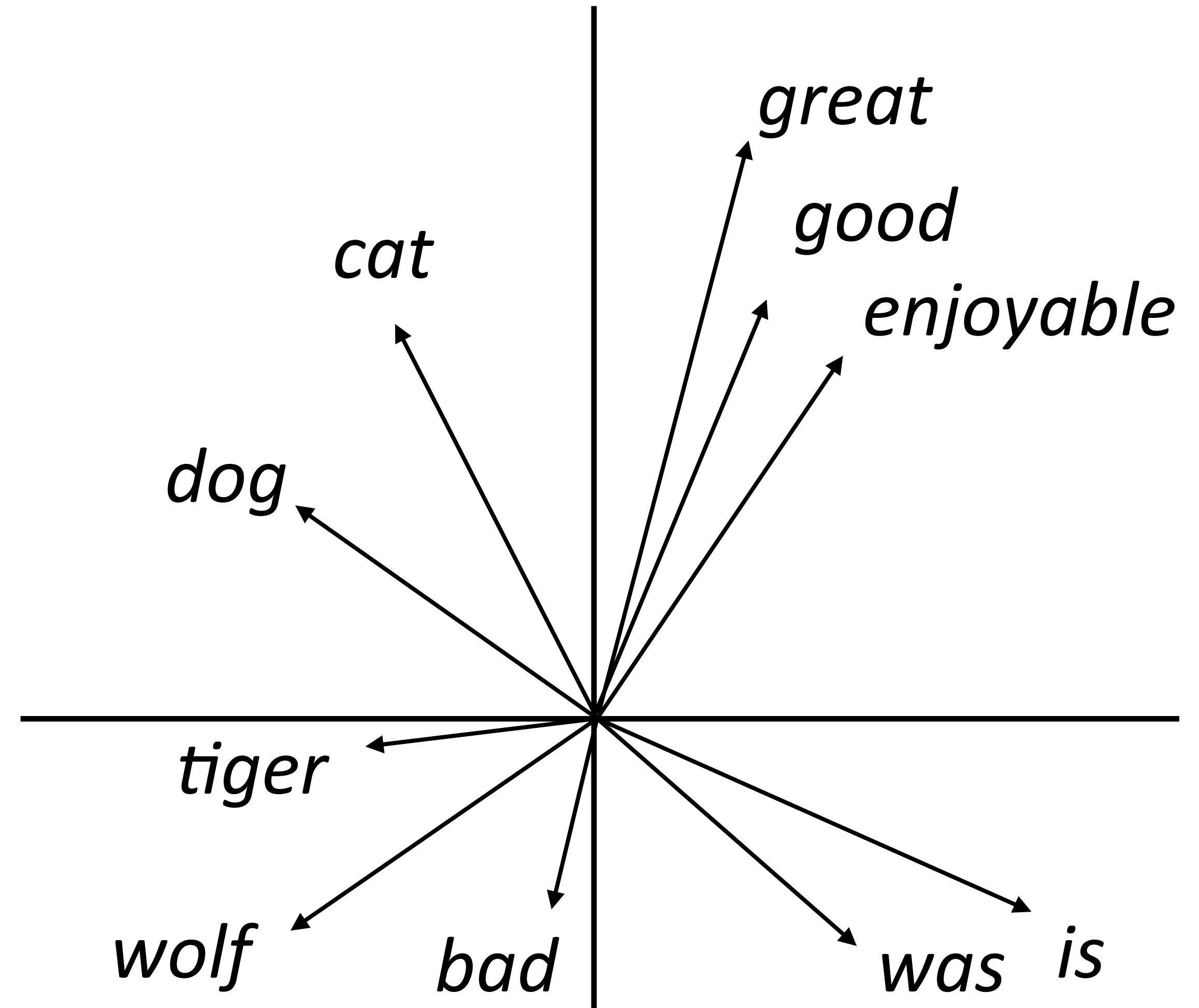
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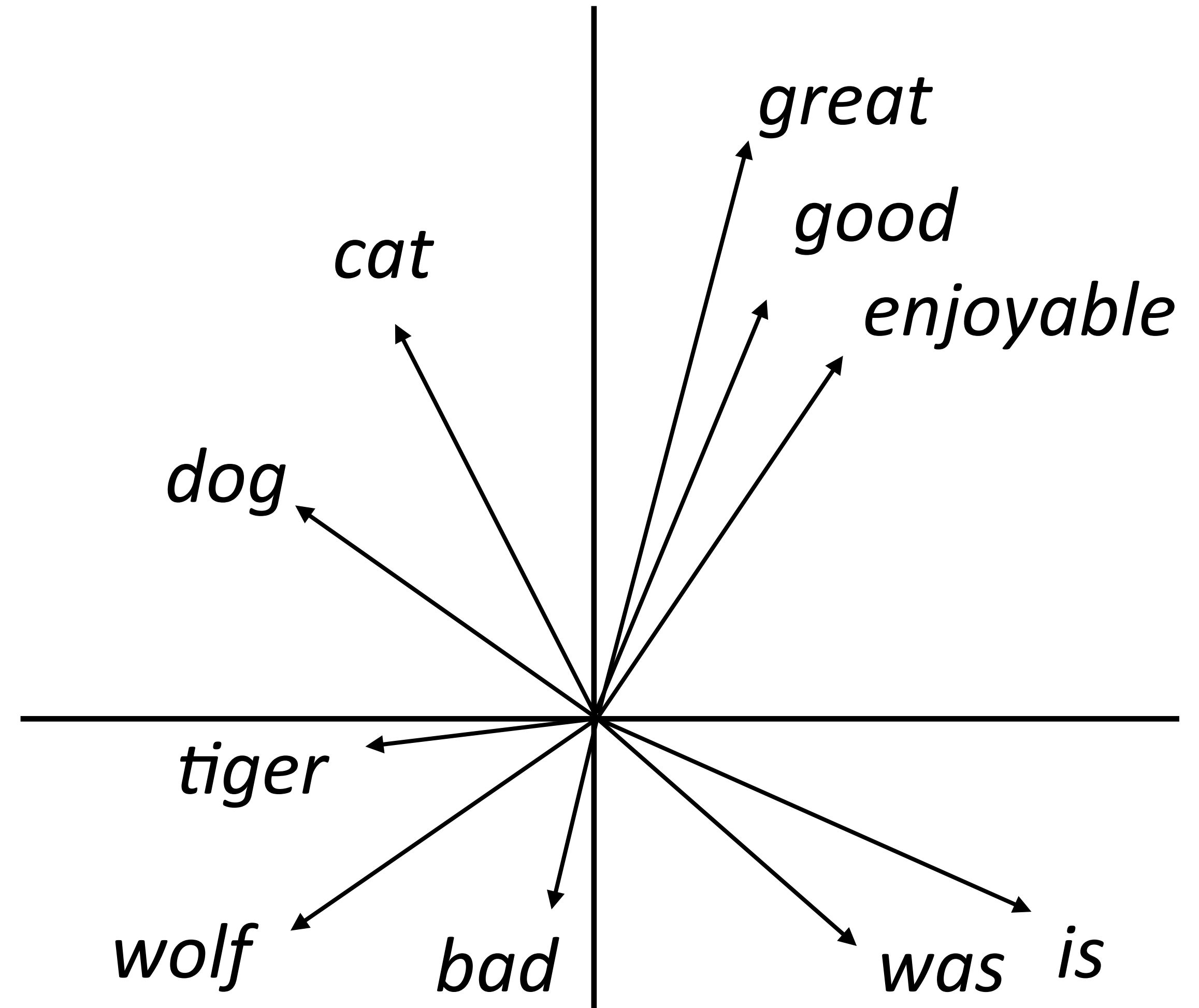
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Paris is to France as Tokyo is to ???





# Similarity

Method	WordSim Similarity	WordSim Relatedness	Bruni et al. MEN	Radinsky et al. M. Turk	Luong et al. Rare Words	Hill et al. SimLex
PPMI	.755	<b>.697</b>	.745	.686	.462	.393
SVD	<b>.793</b>	.691	<b>.778</b>	.666	<b>.514</b>	.432
SGNS	<b>.793</b>	.685	.774	<b>.693</b>	.470	<b>.438</b>
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- ▶ SVD = singular value decomposition on PMI matrix
- ▶ GloVe does not appear to be the best when experiments are carefully controlled, but it depends on hyperparameters + these distinctions don't matter in practice

# Hypernymy Detection

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Random	52.0	30.8	24.5	55.2	23.2
Word2Vec + C	52.1	<b>39.5</b>	20.7	<b>63.0</b>	25.3
GE + C	53.9	36.0	21.6	58.2	26.1
GE + KL	52.0	39.4	23.7	54.4	25.9
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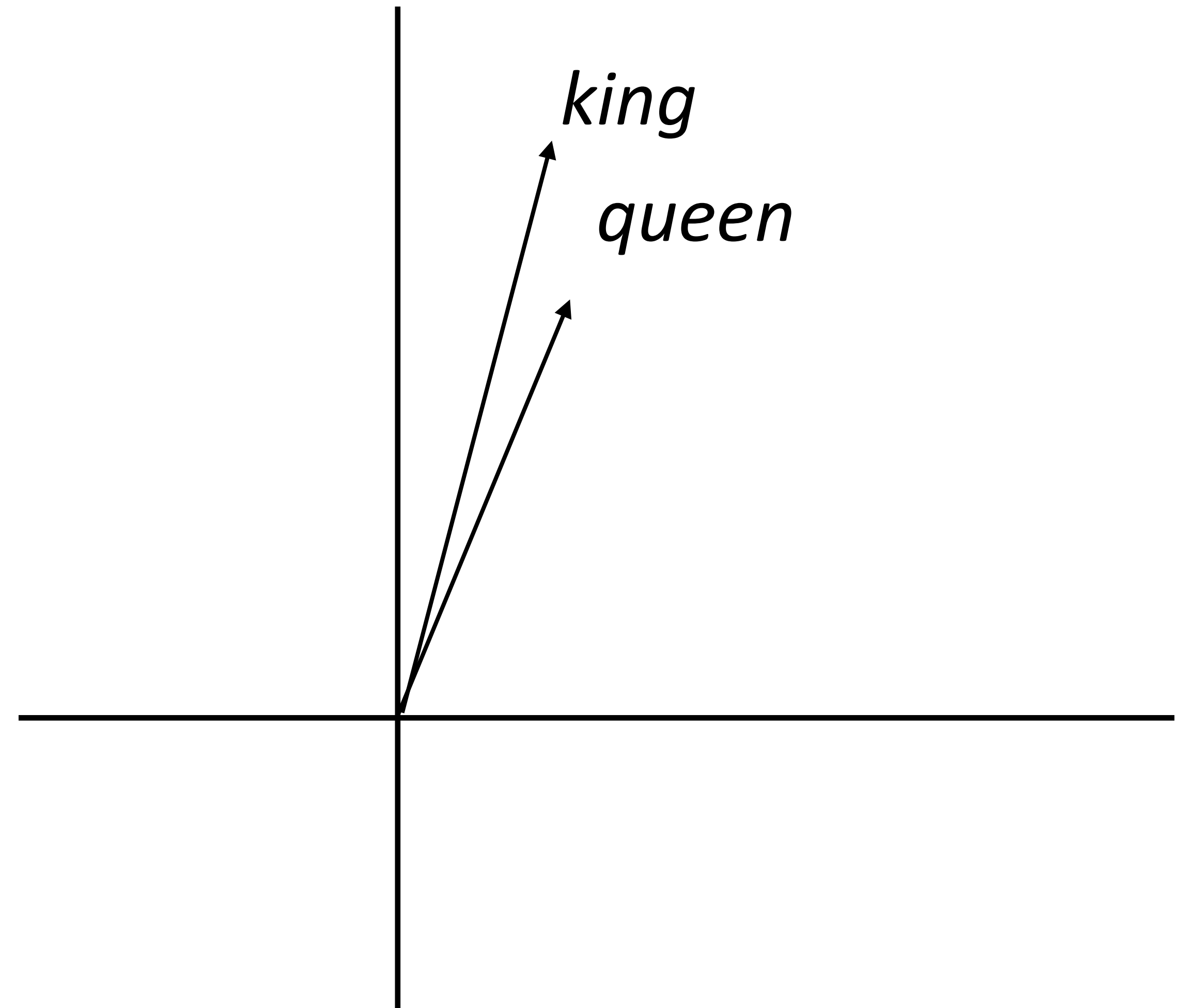
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- ▶ word2vec (SGNS) works barely better than random guessing here

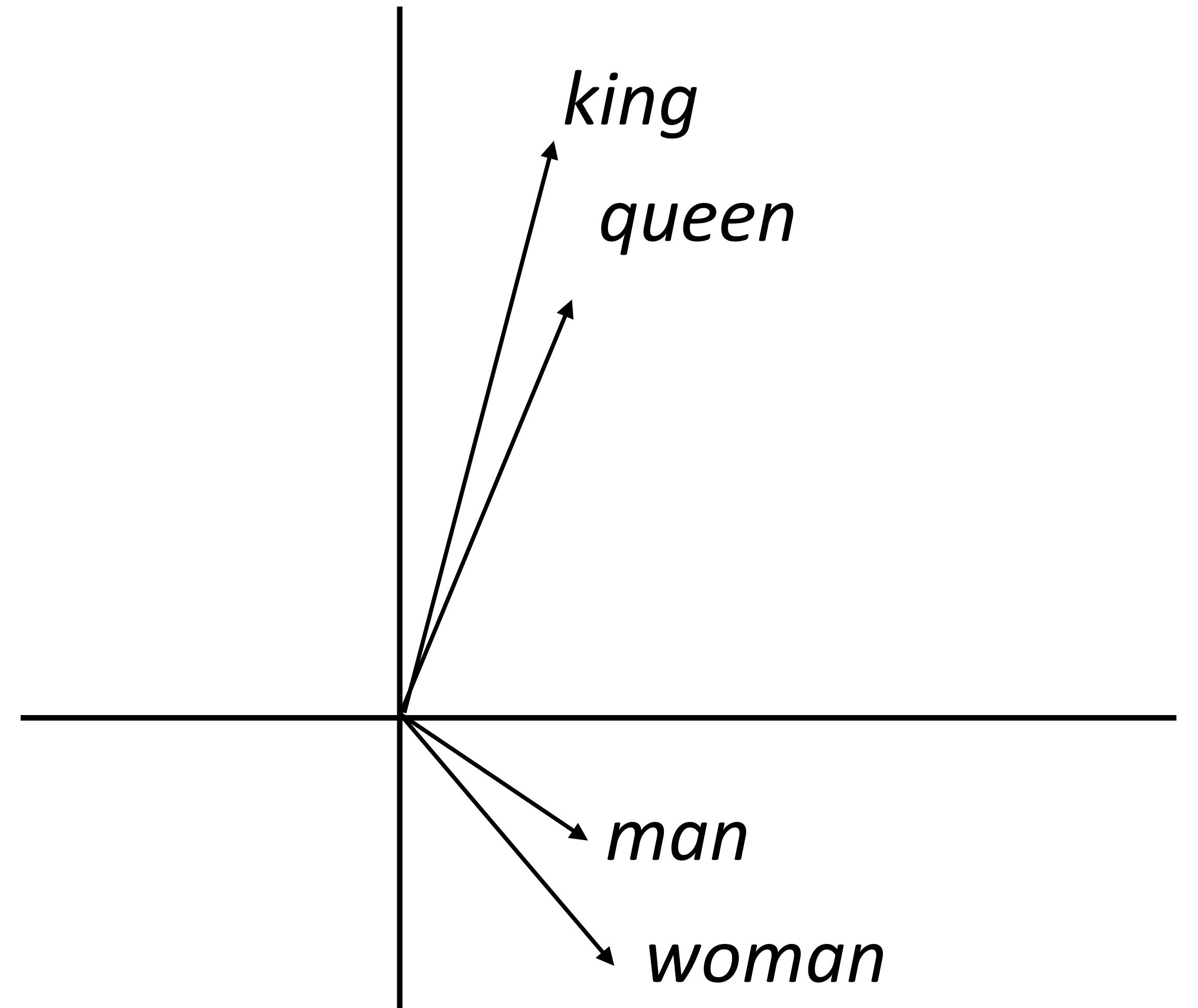
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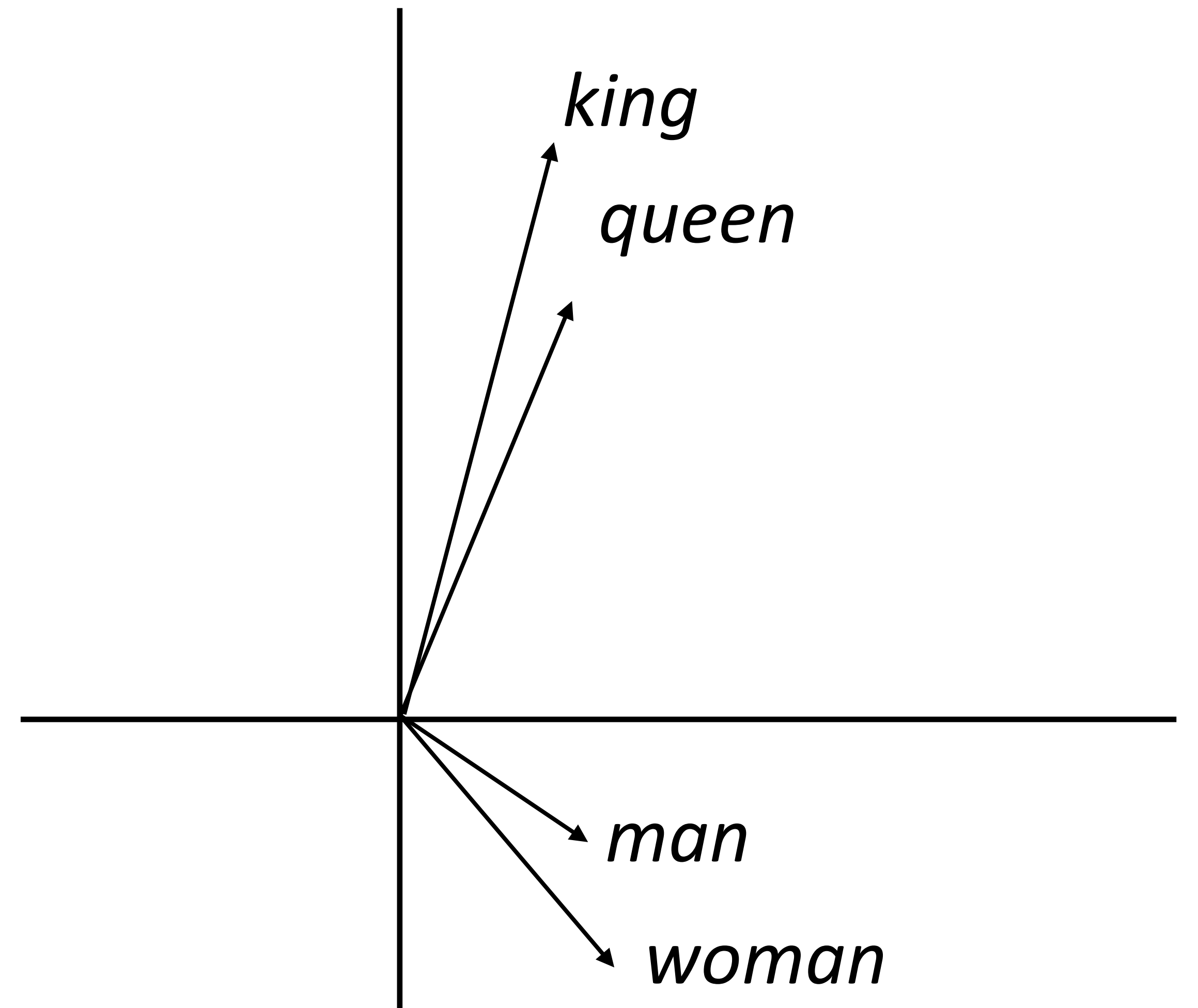




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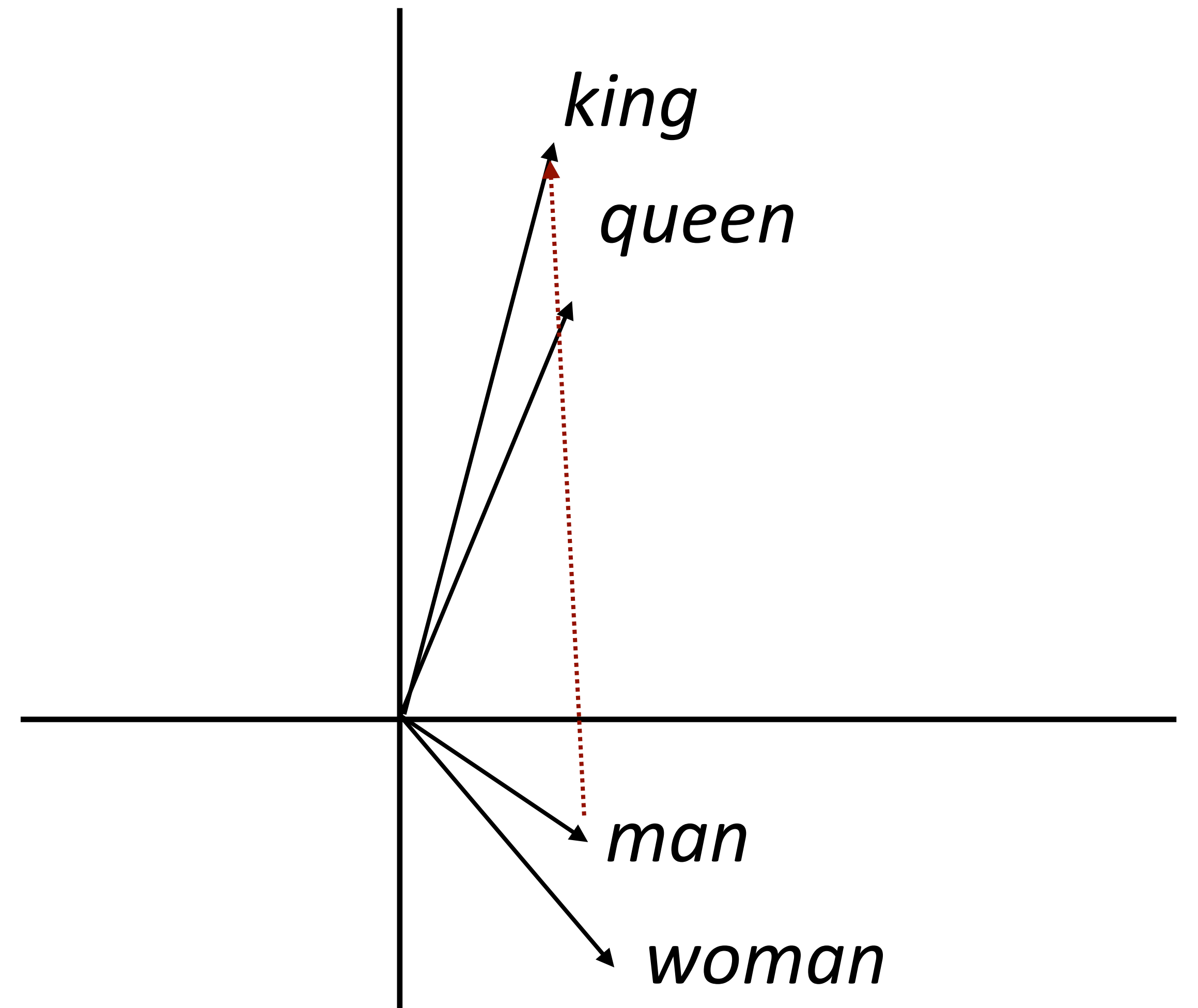
*(king - man) + woman = queen*



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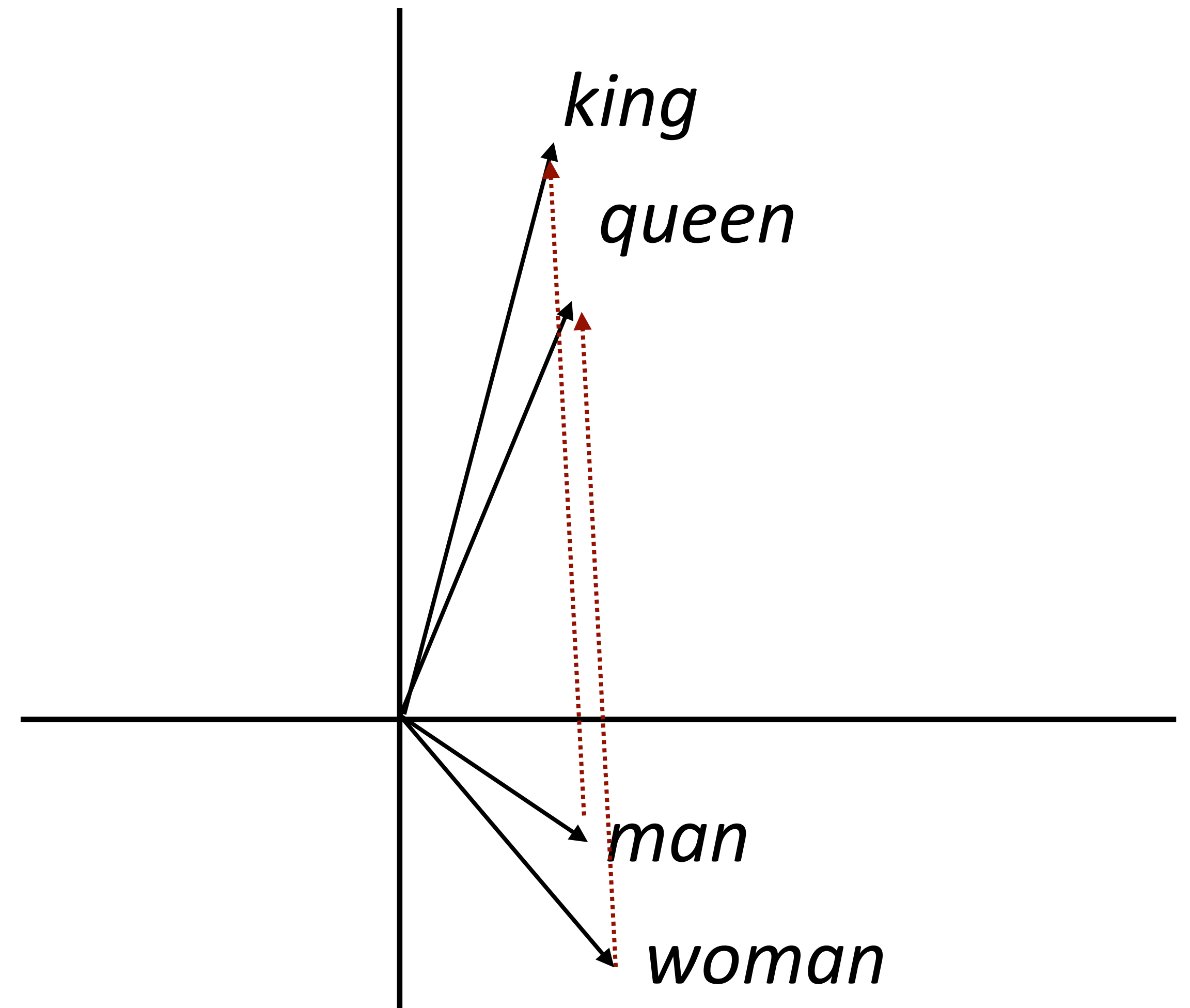
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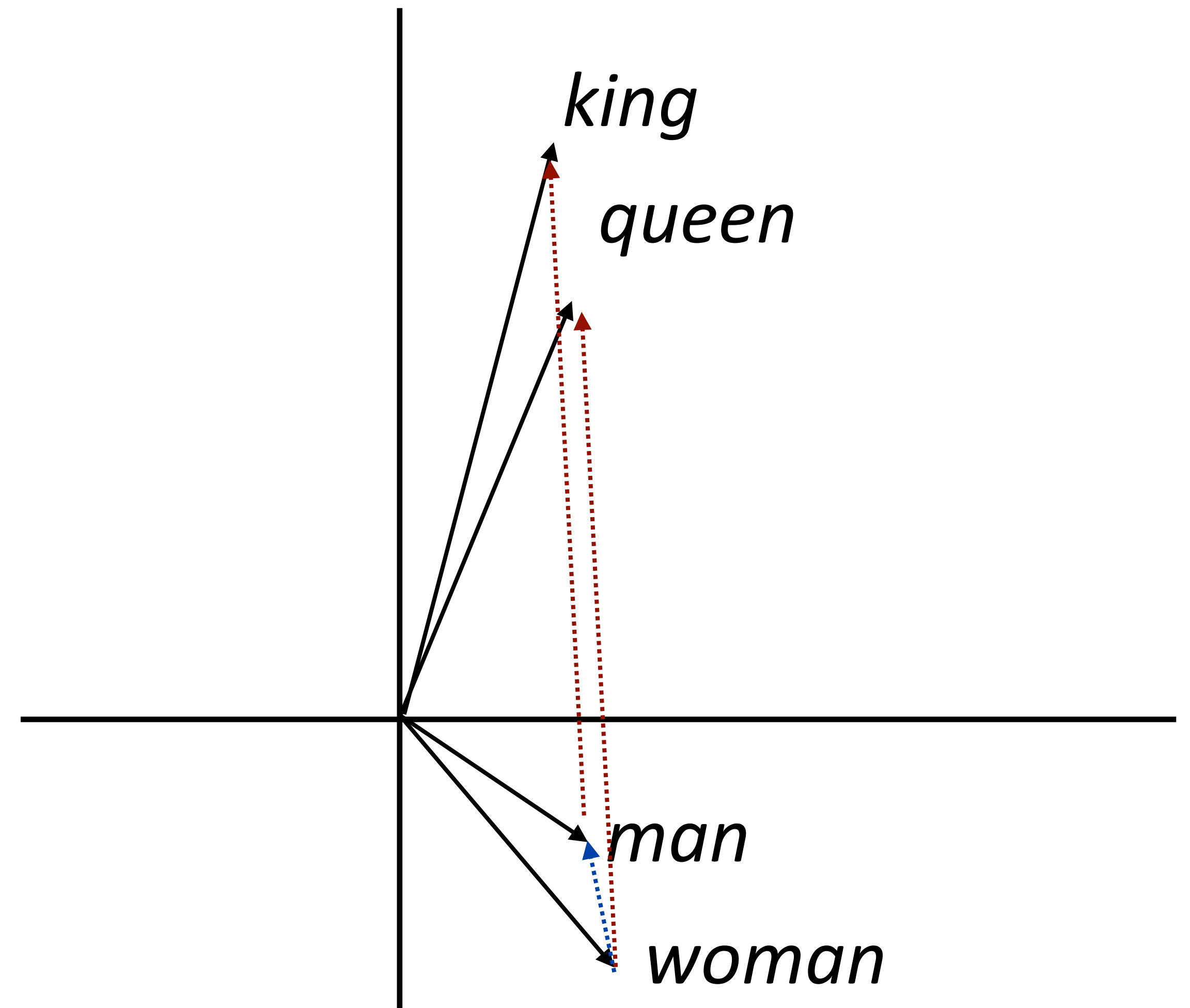
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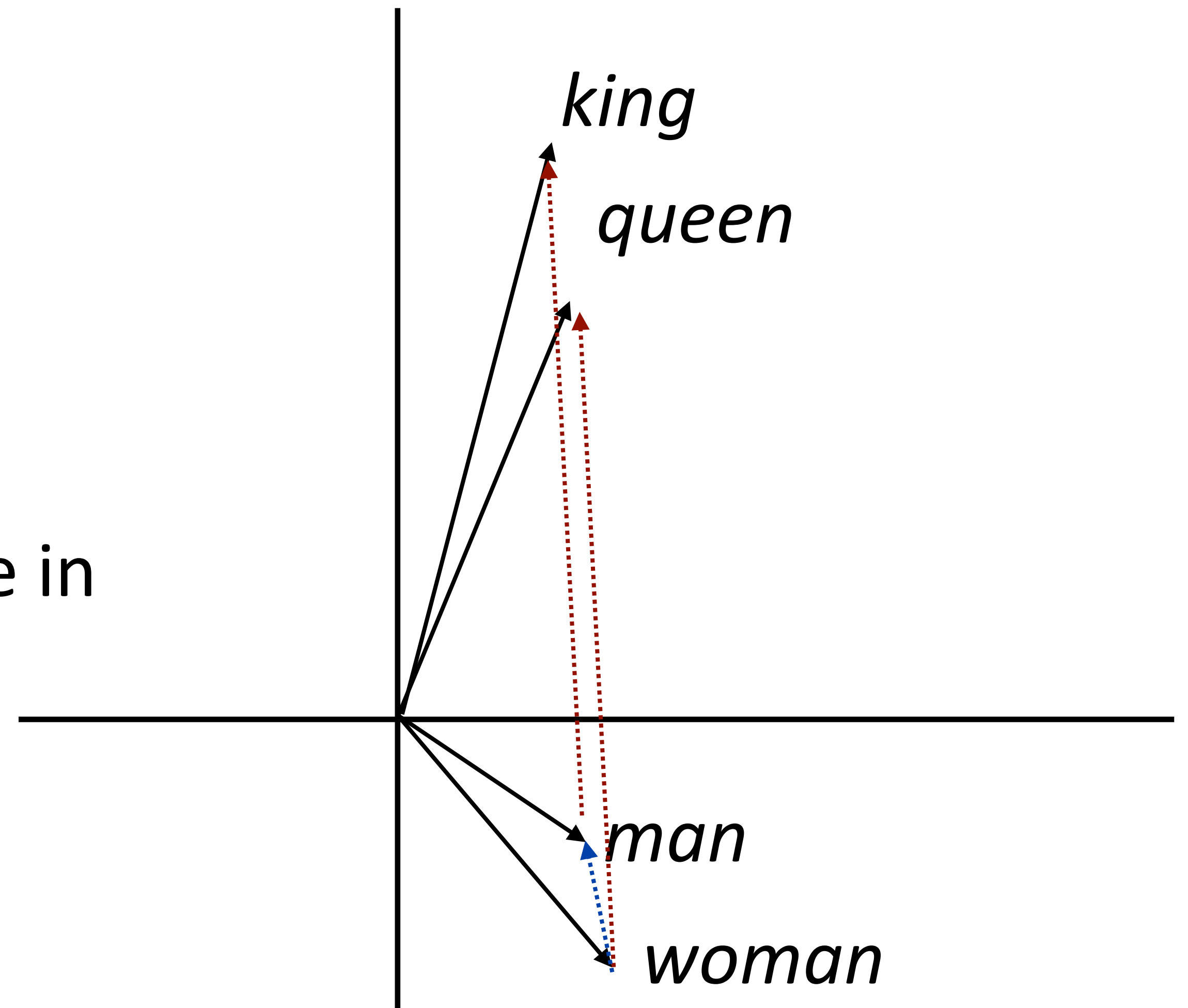
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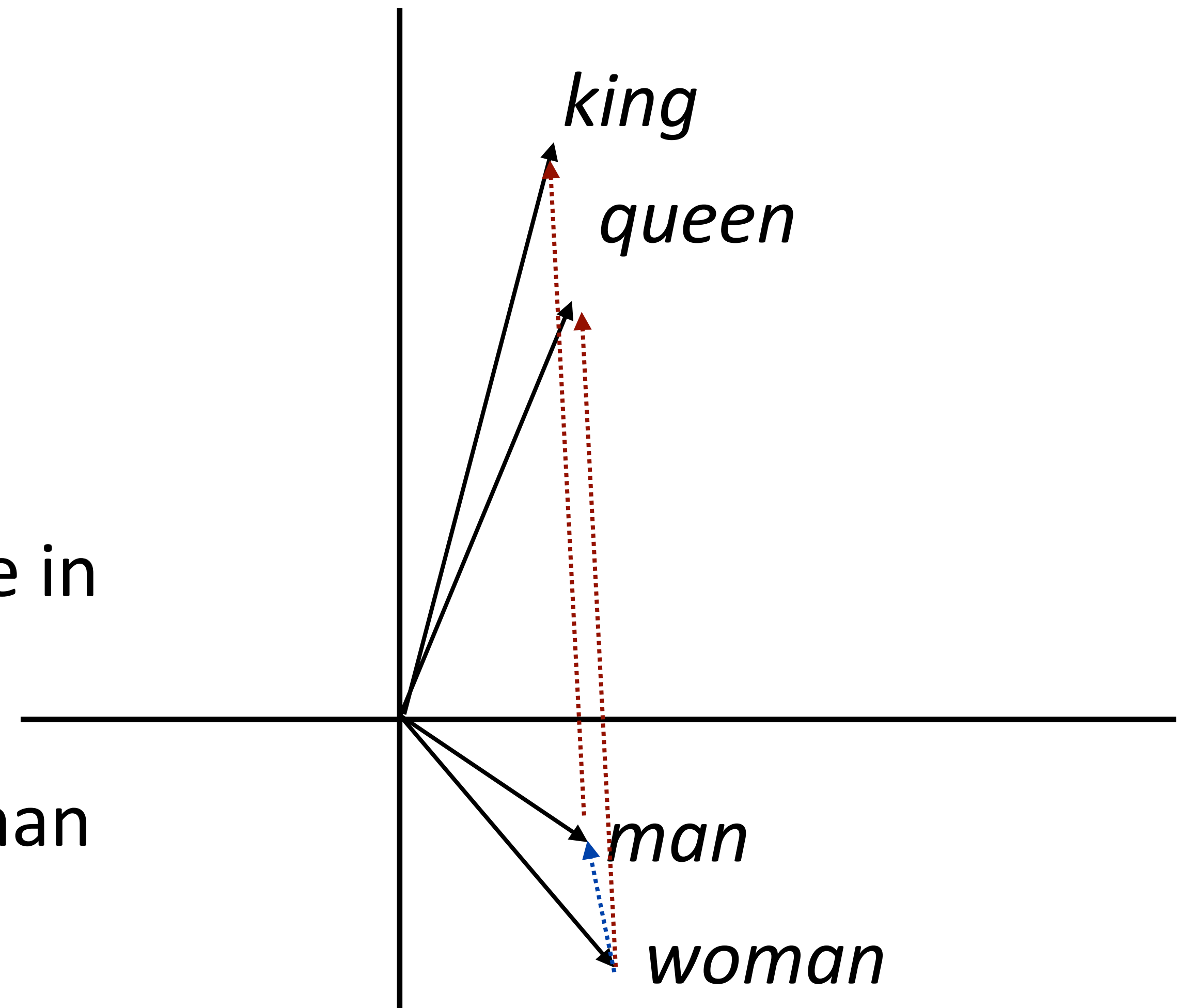


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- ▶ Why would this be?
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- ▶ Dominant change: more “he” with man and “she” with woman — similar to difference between king and queen



# Analogies

---

Method	Google	MSR
	Add / Mul	Add / Mul
PPMI	.553 / .679	.306 / .535
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$$\text{Maximizing for } b: \text{Add} = \cos(b, a_2 - a_1 + b_1) \quad \text{Mul} = \frac{\cos(b_2, a_2) \cos(b_2, b_1)}{\cos(b_2, a_1) + \epsilon}$$

Levy et al. (2015)

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- ▶ Approach 2: initialize using GloVe/ELMo, keep fixed
  - ▶ Faster because no need to update these parameters
- ▶ Approach 3: initialize using GloVe, fine-tune
  - ▶ Works best for some tasks, but not used for ELMo

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- ▶ Will return to this in a few weeks

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- ▶ Lots of pretrained embeddings work well in practice, they capture some desirable properties
- ▶ Even better: context-sensitive word embeddings (ELMo)
- ▶ Next time: RNNs and CNNs