Lecture 7: Tricks + Word Embeddings

Alan Ritter

(many slides from Greg Durrett)

Recall: Feedforward NNs

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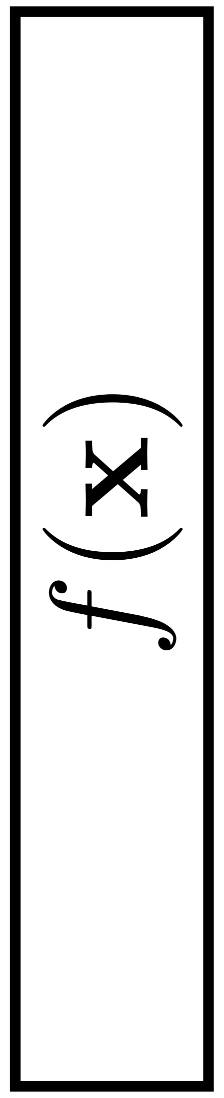

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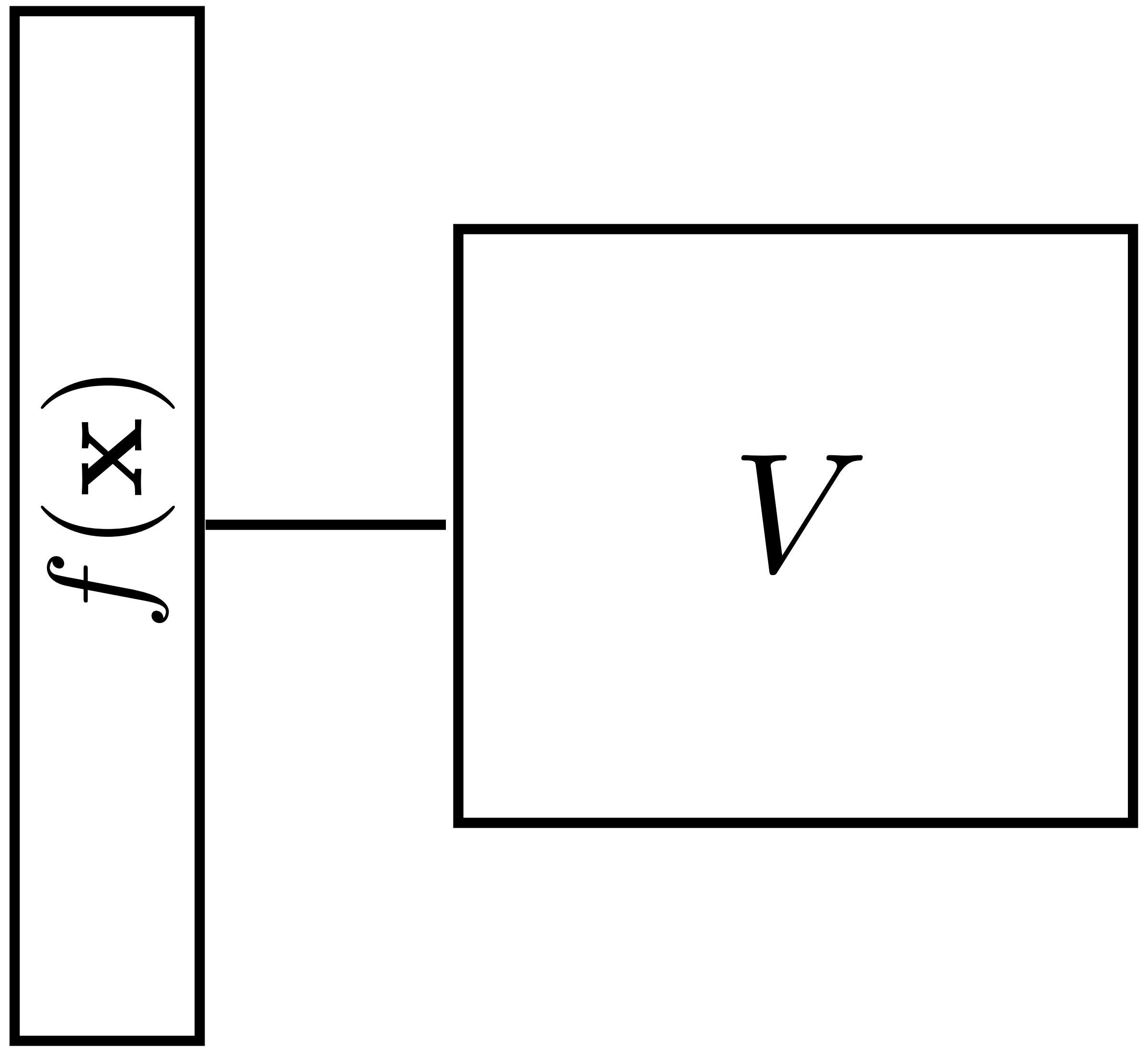

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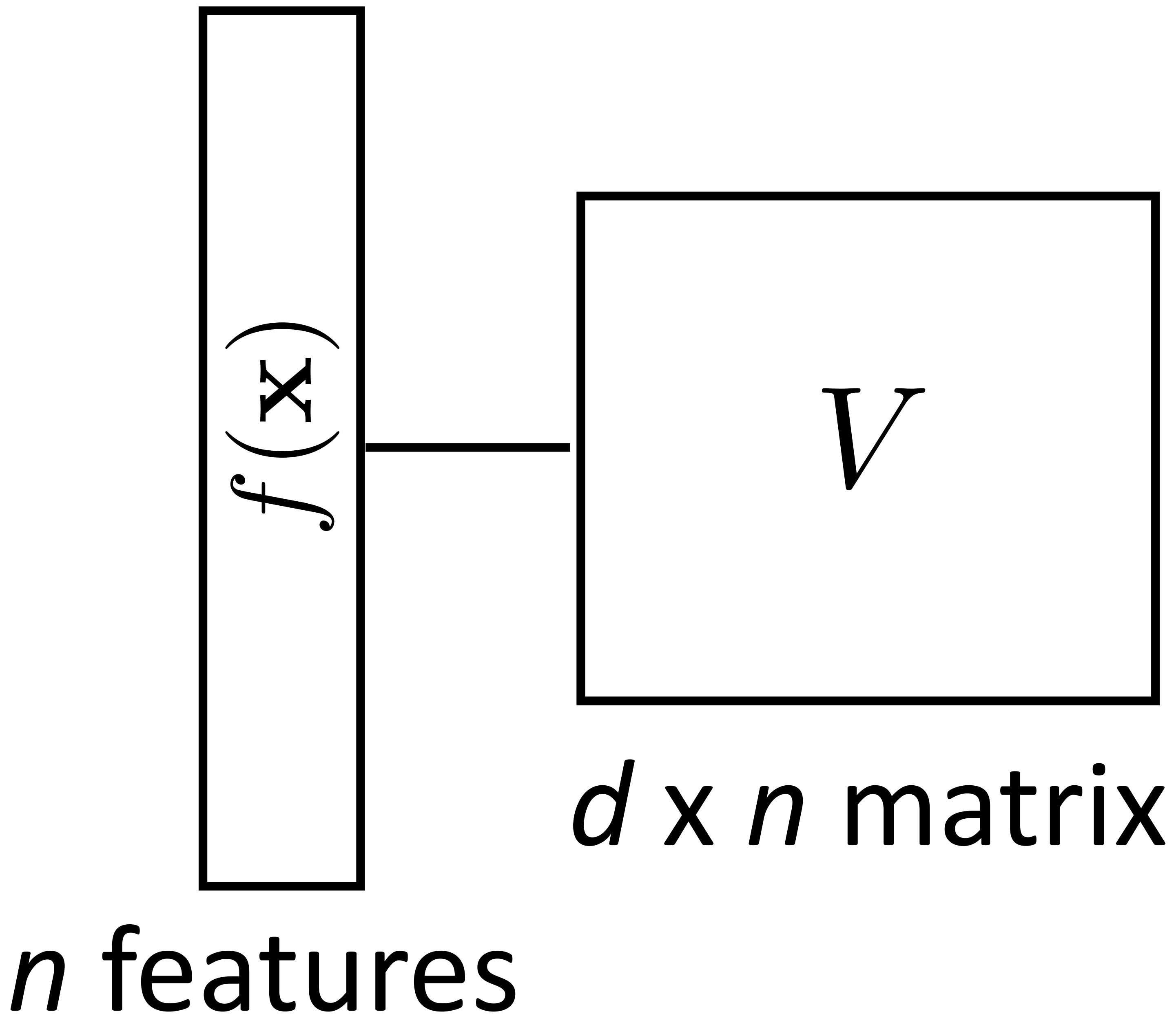

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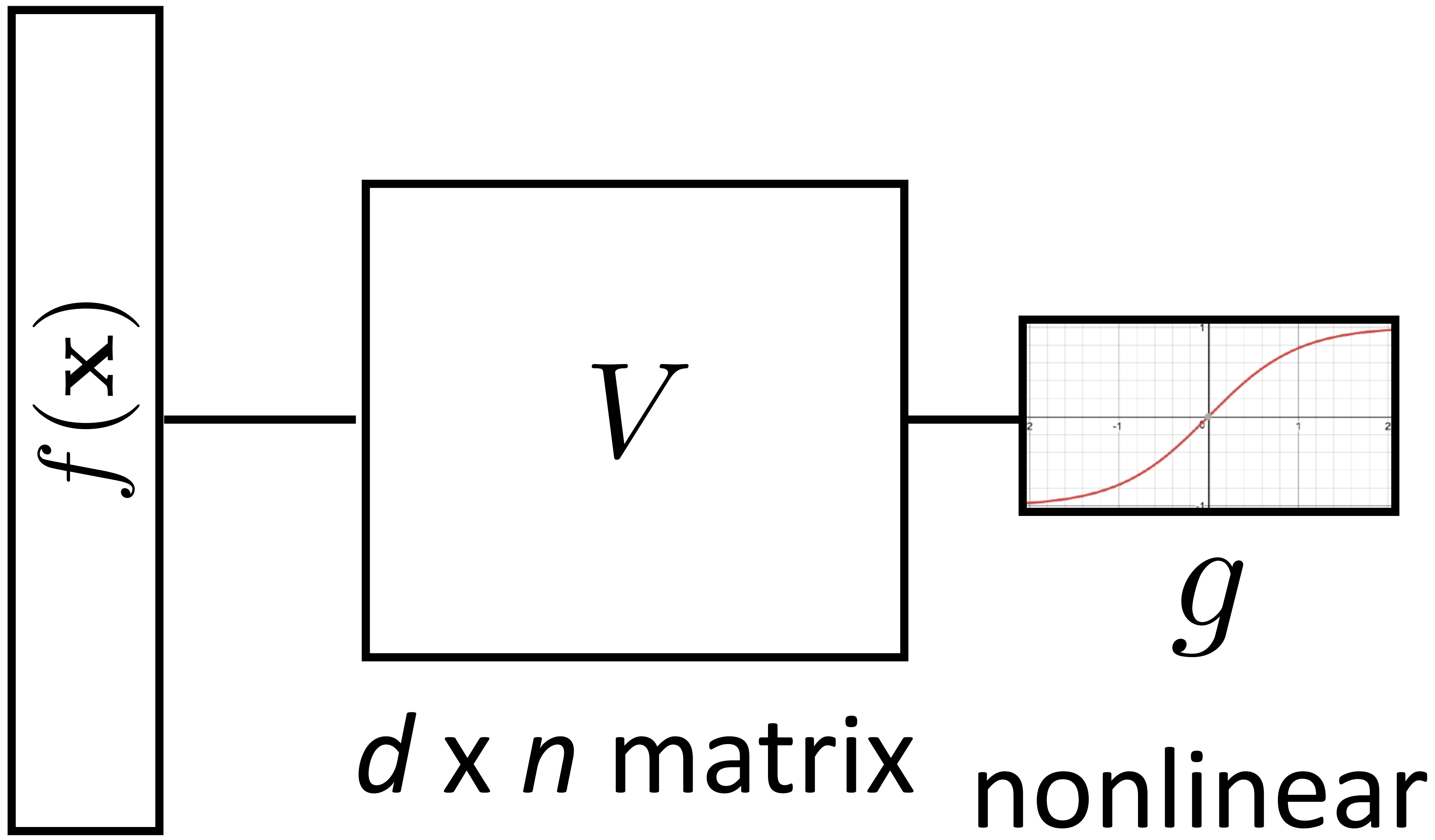

n features

d x *n* matrix

nonlinearity
(tanh, relu, …)

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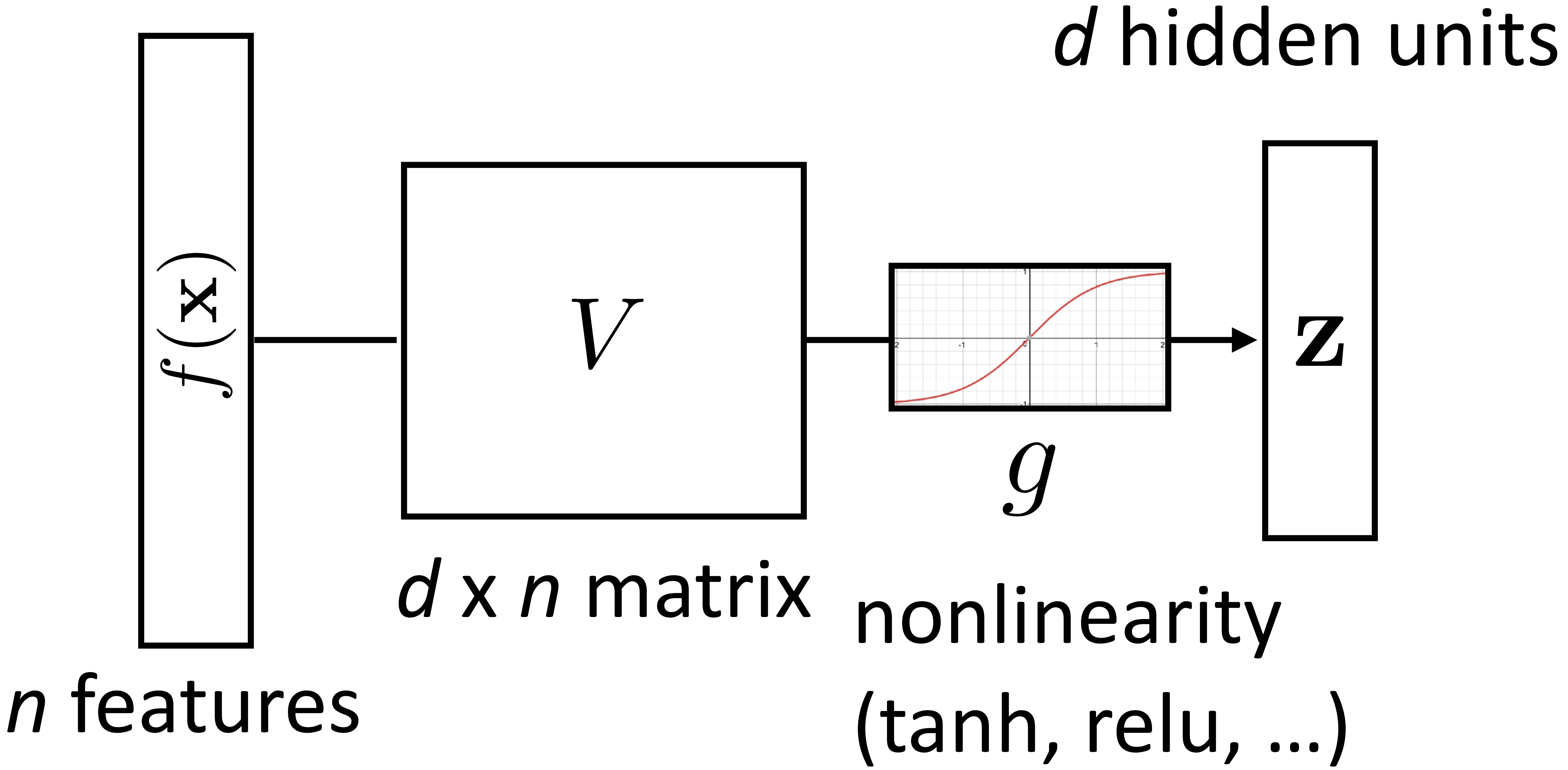

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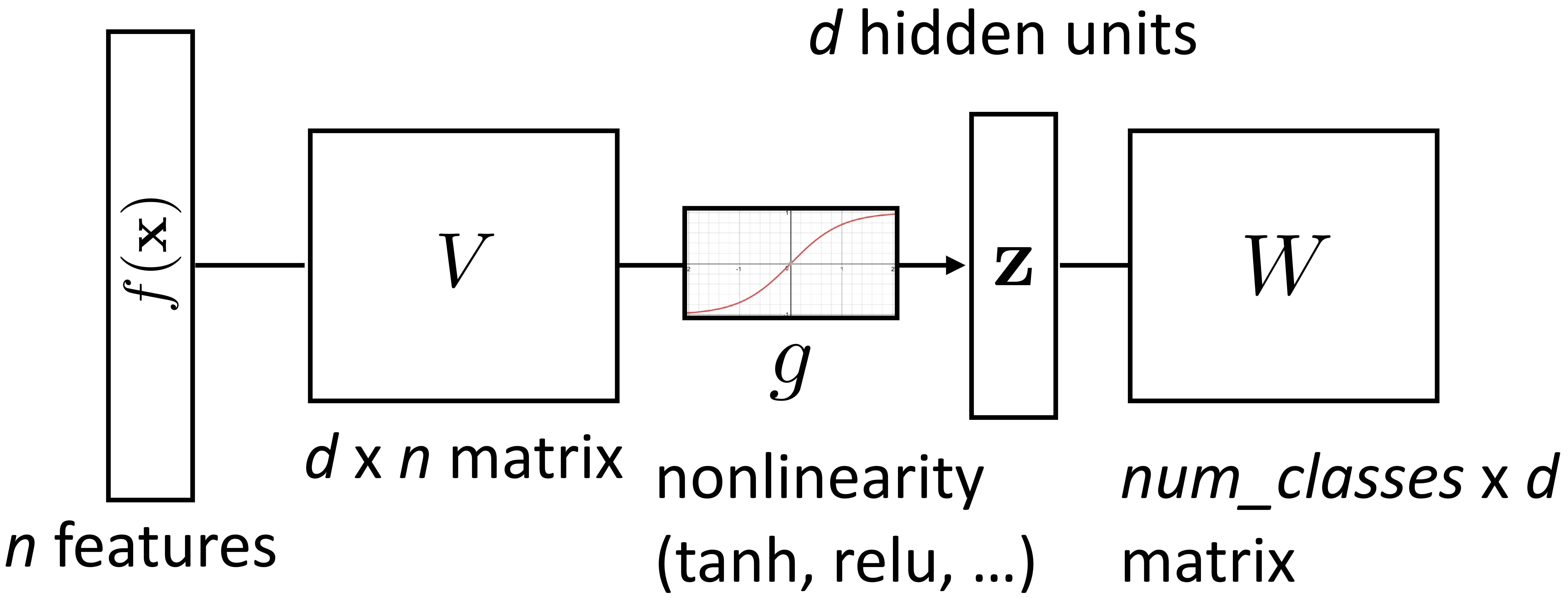

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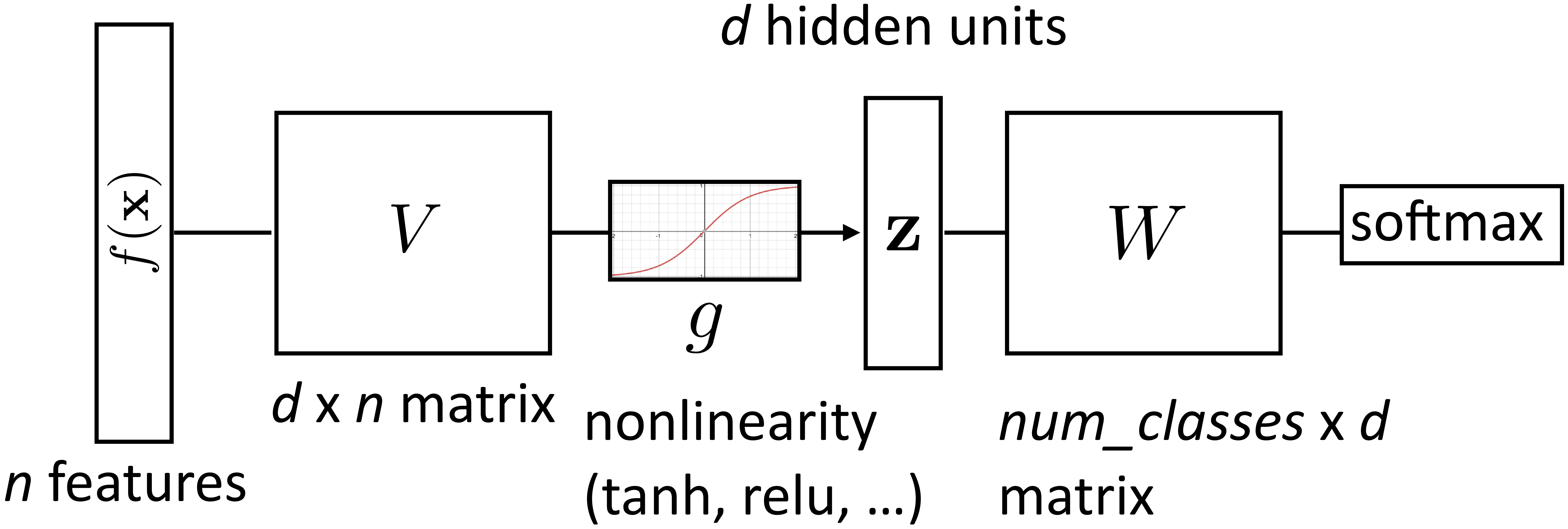

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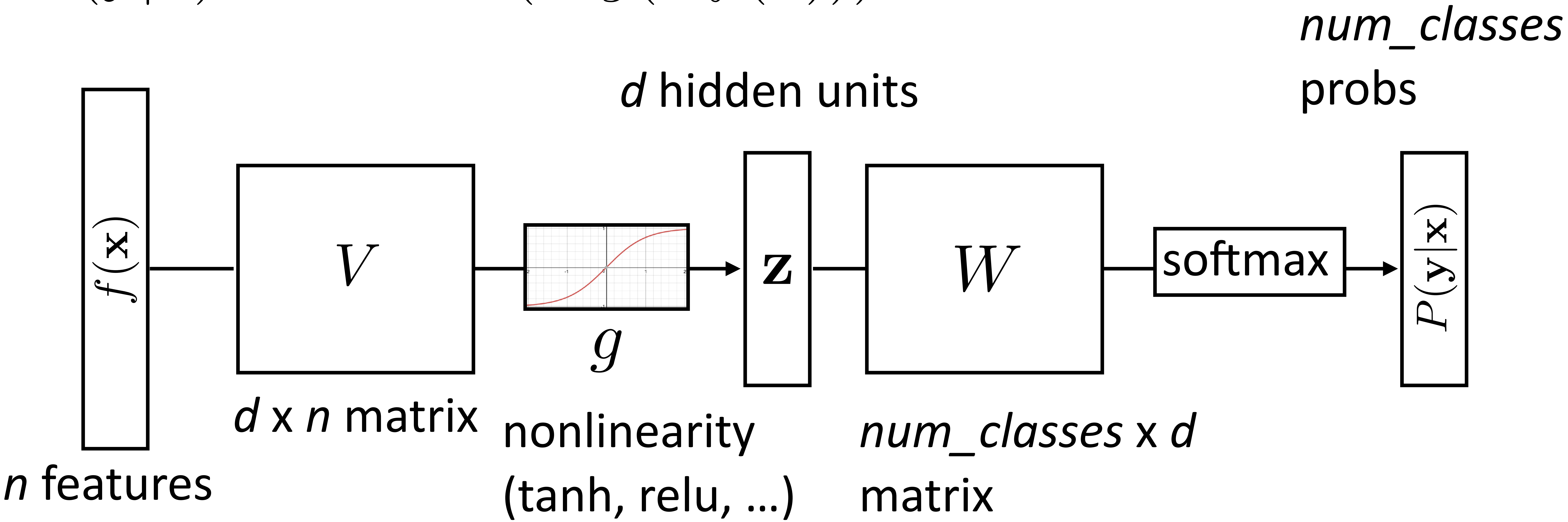

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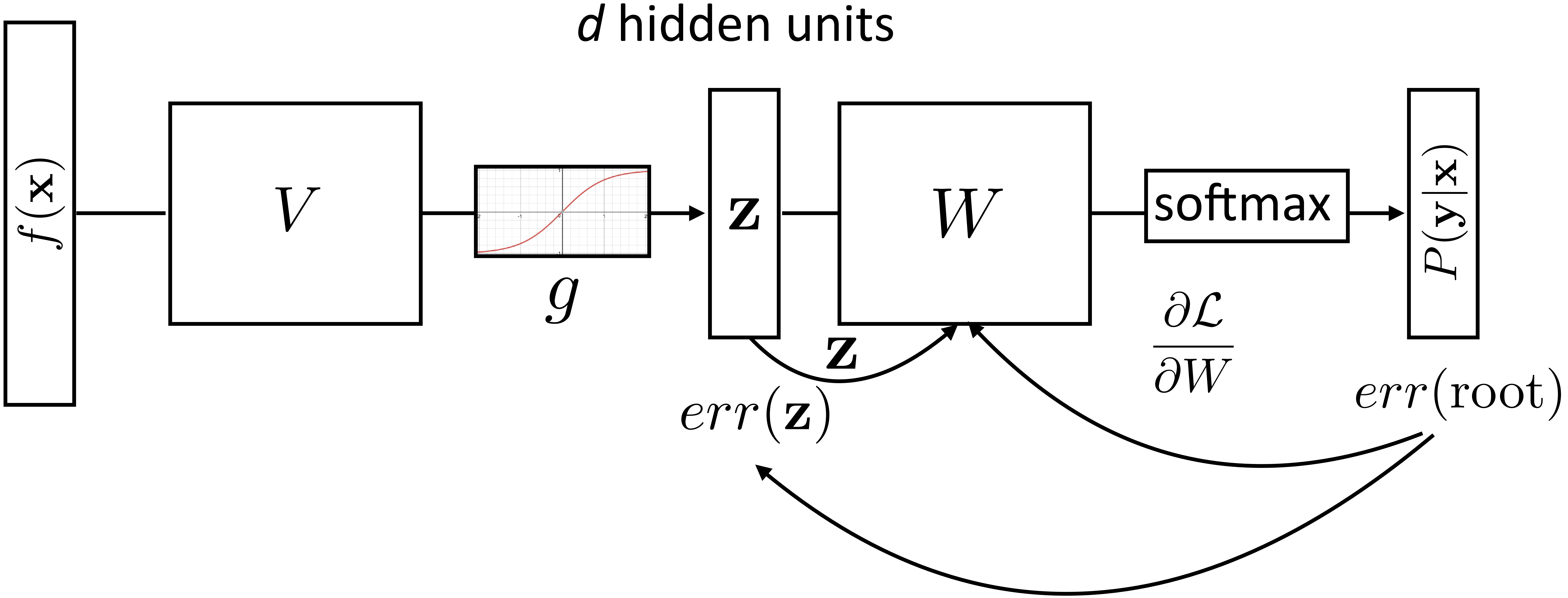

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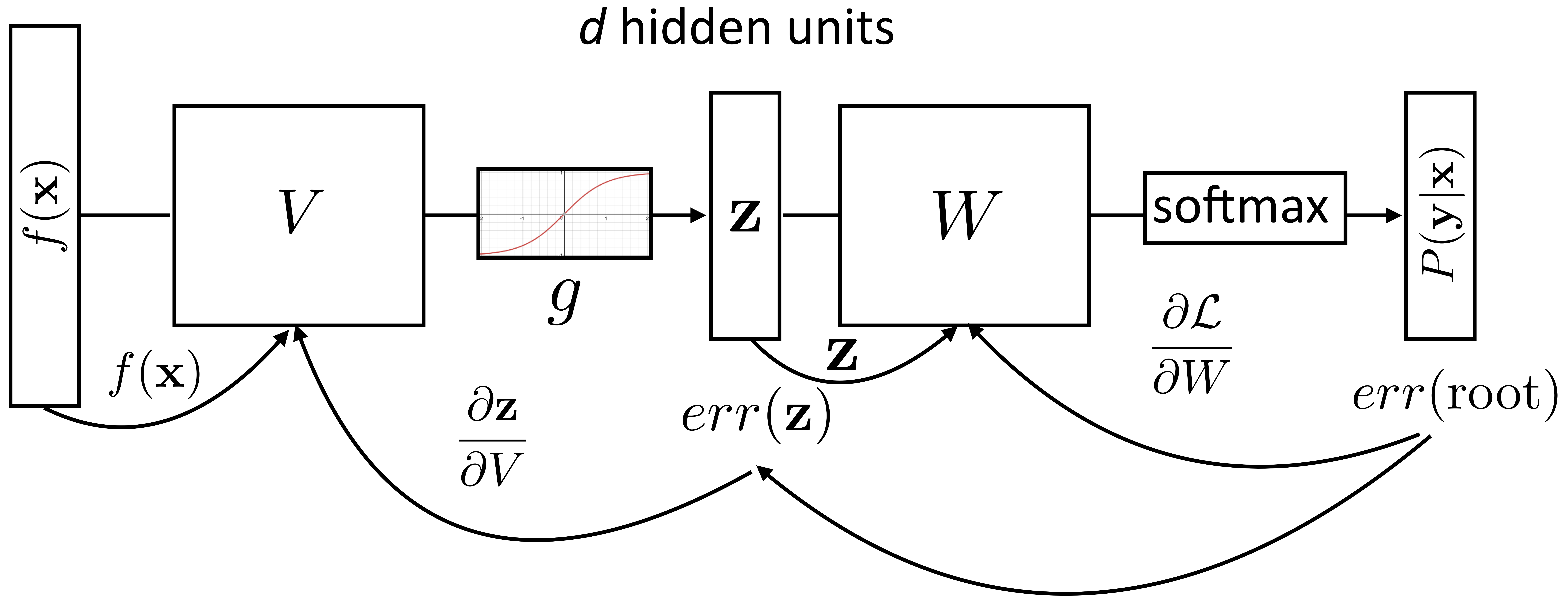

This Lecture

- Training
- Word representations
- word2vec/GloVe
- Evaluating word embeddings

Training Tips

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- How to initialize? How to regularize? What optimizer to use?
- This lecture: some practical tricks. Take deep learning or optimization courses to understand this further

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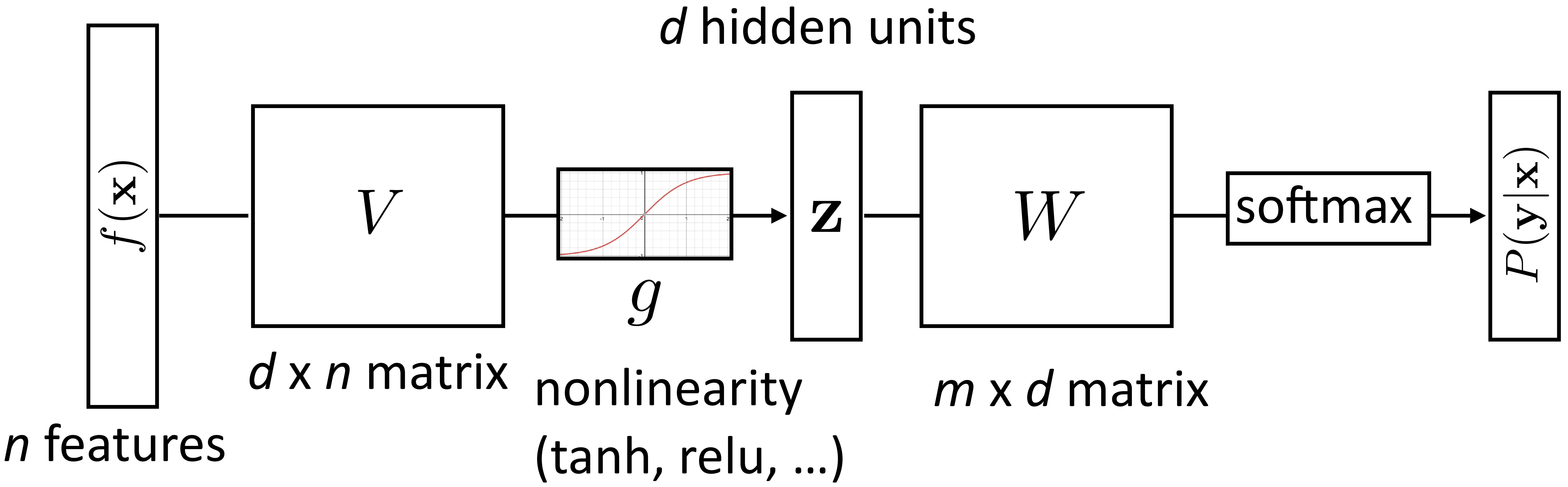

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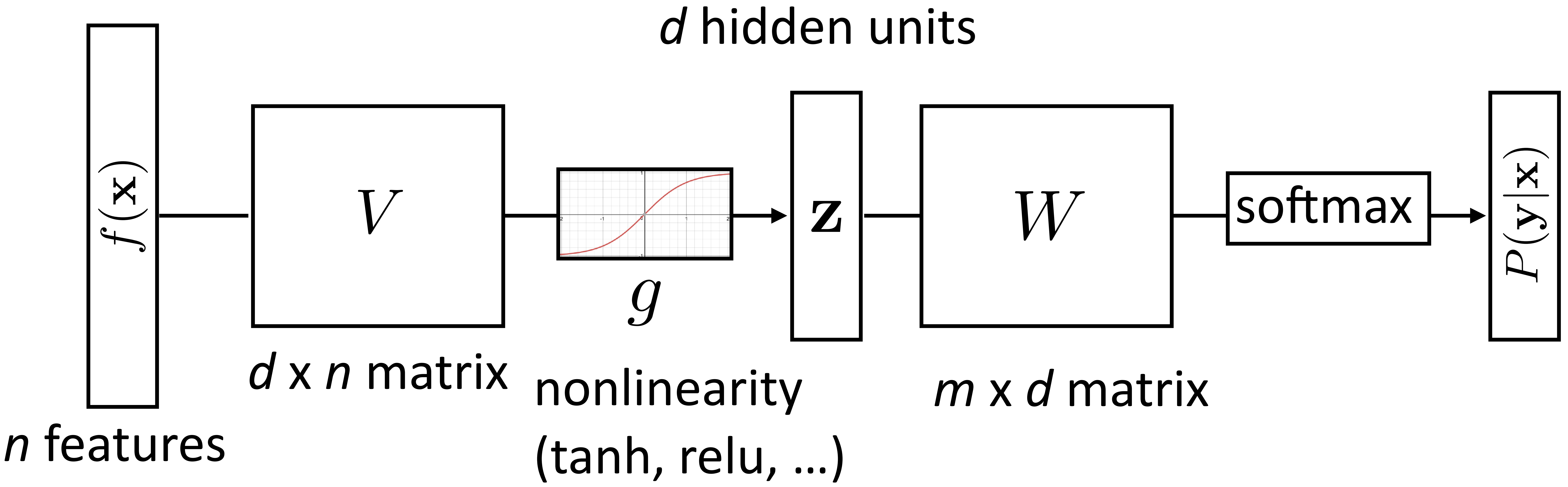

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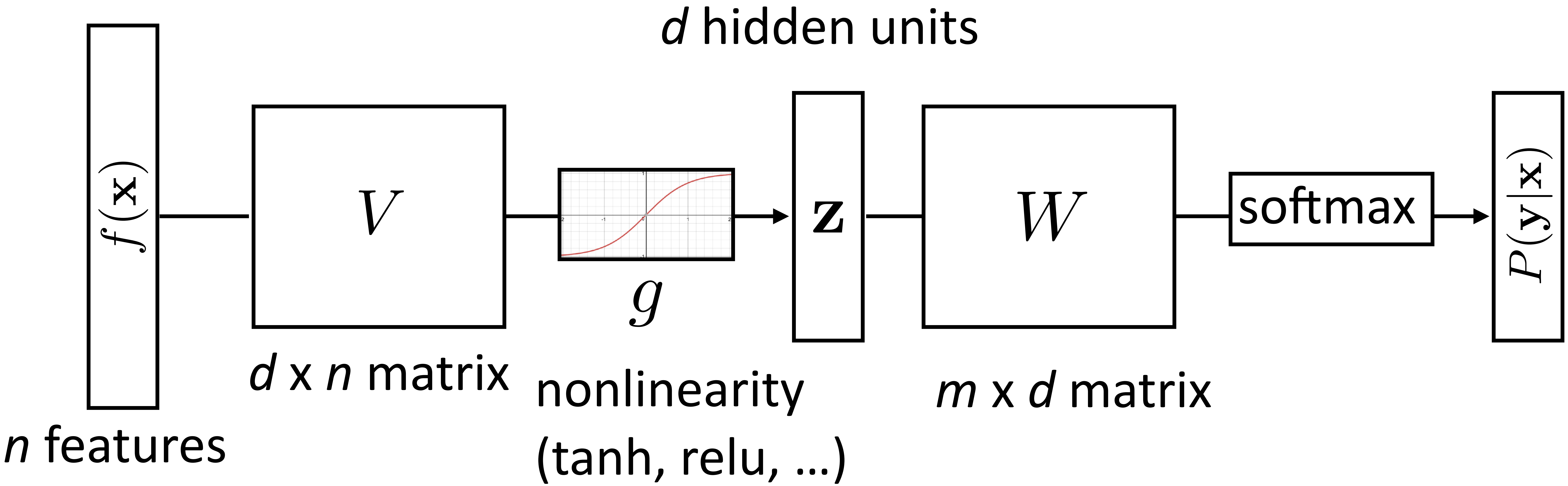

- How do we initialize V and W? What consequences does this have?
- *Nonconvex* problem, so initialization matters!

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- Nonlinear model…how does this affect things?

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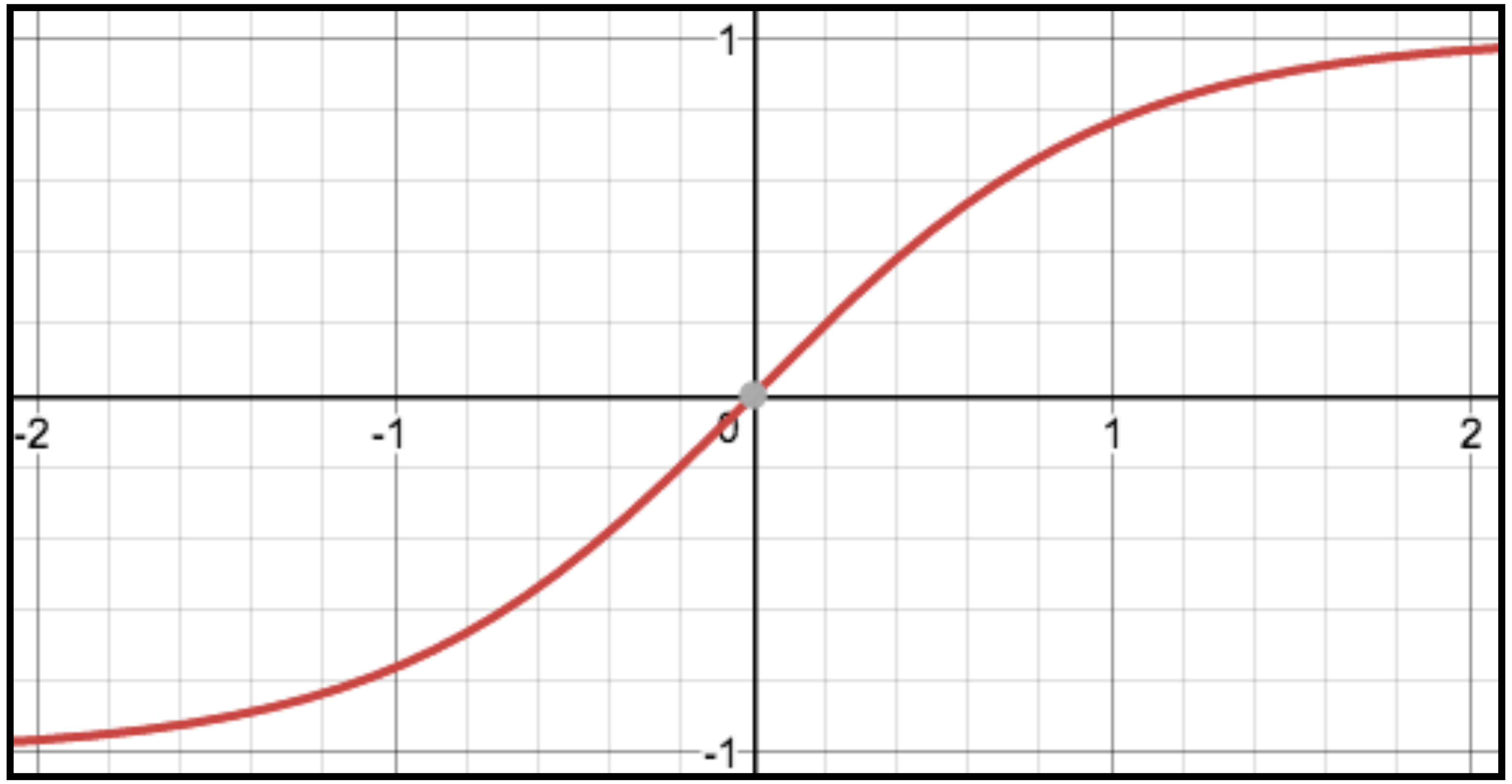

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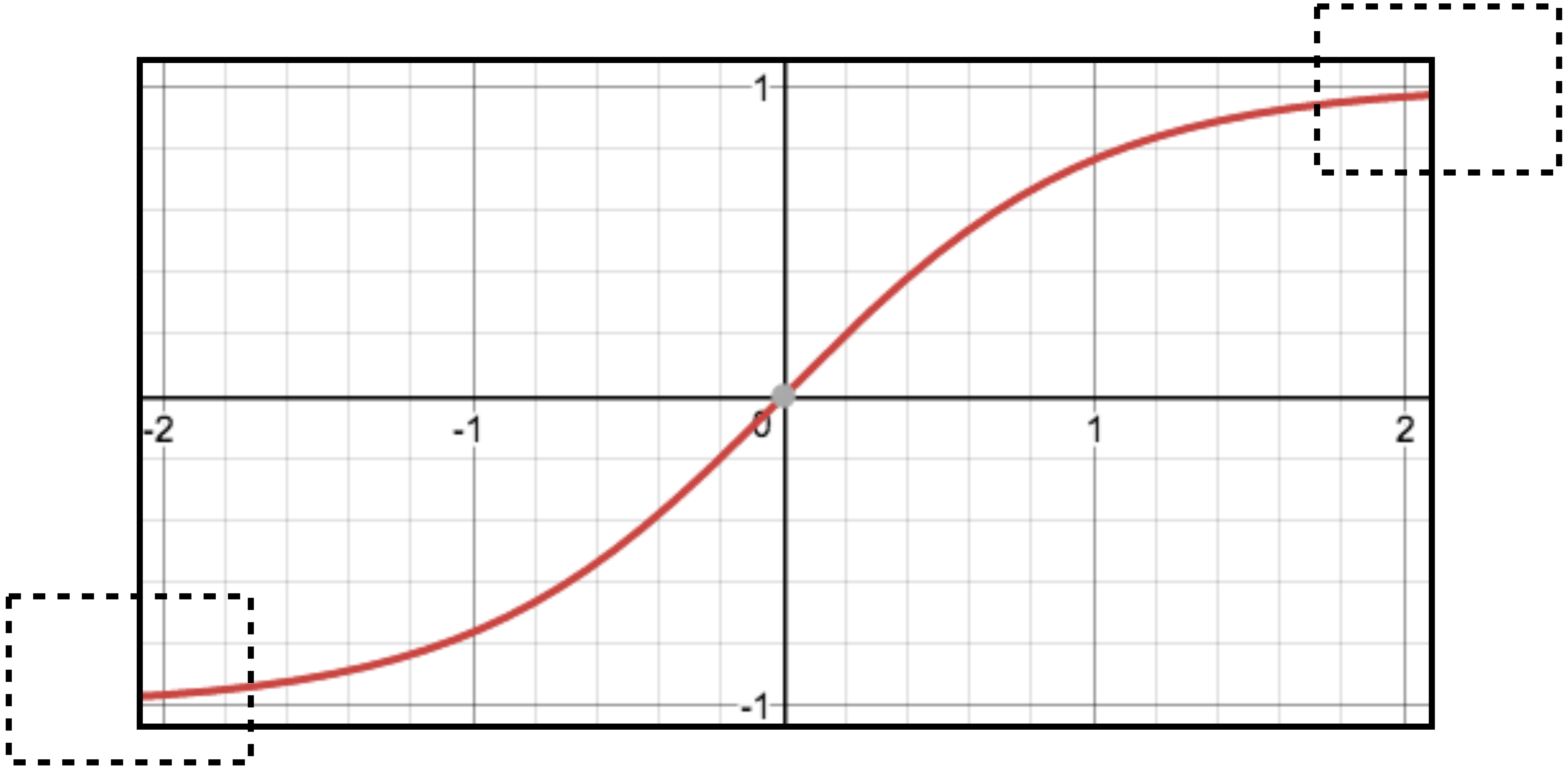

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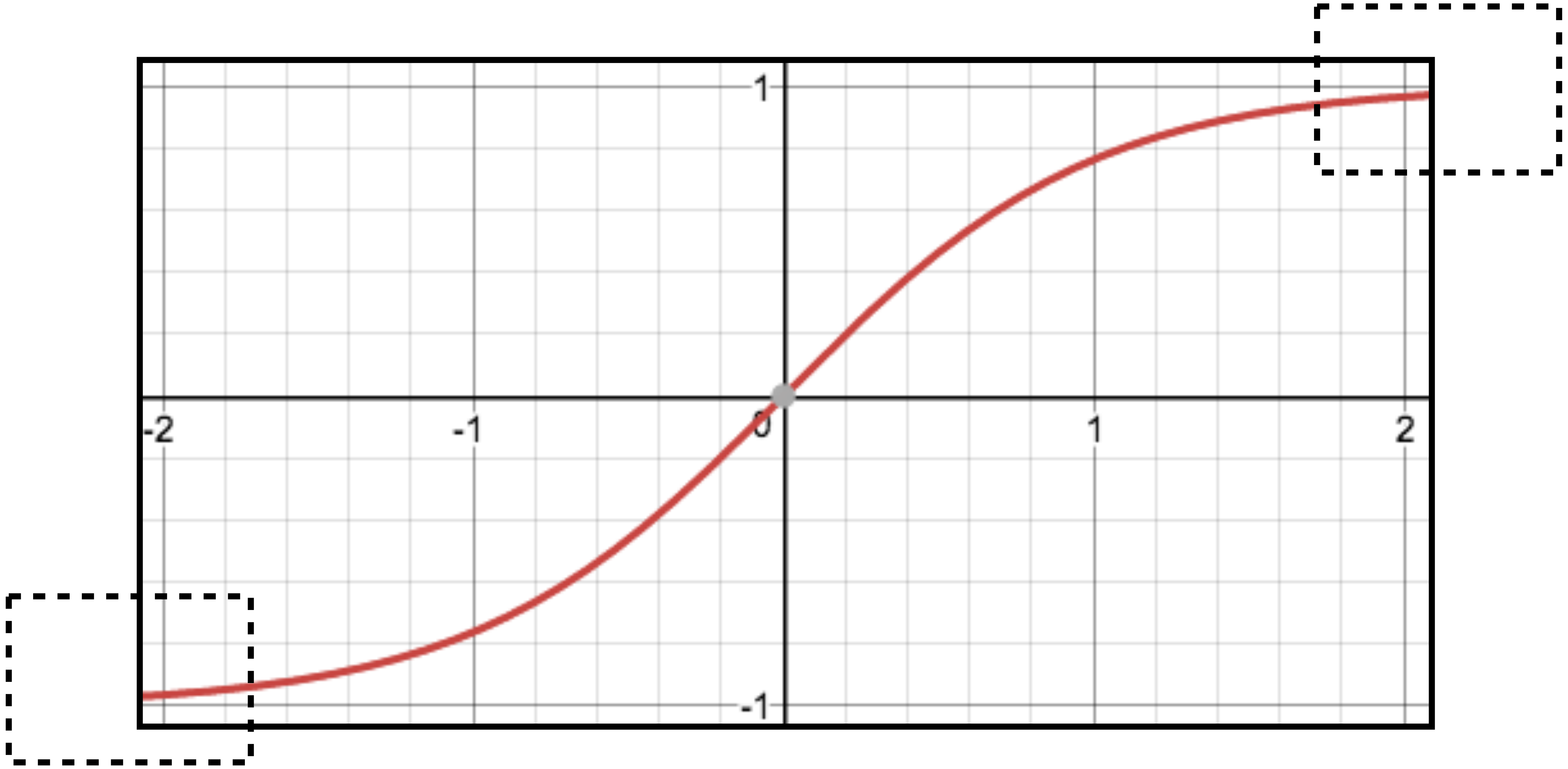

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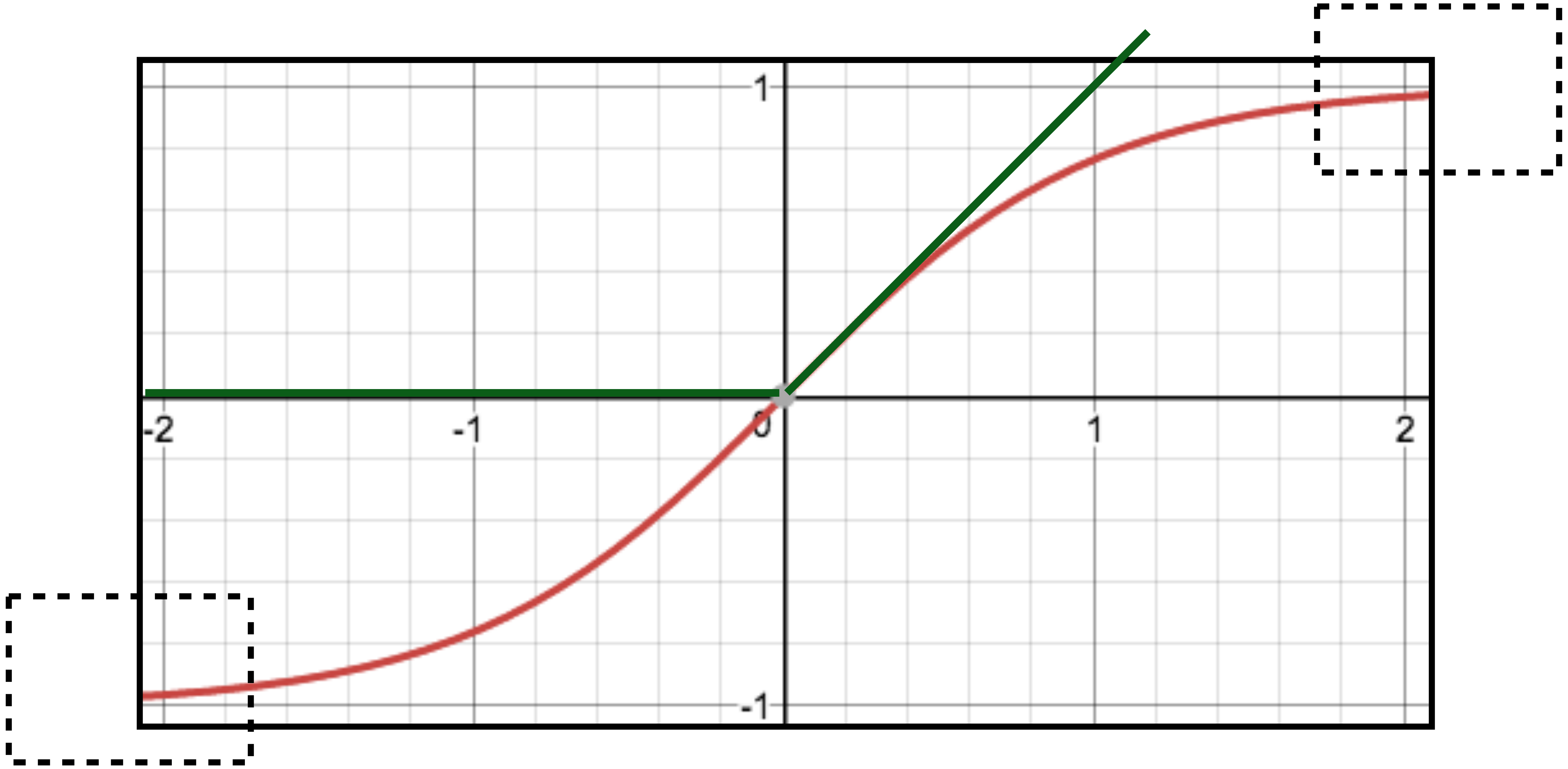

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- ReLU: larger dynamic range (all positive numbers), but can produce big values, can break down if everything is too negative

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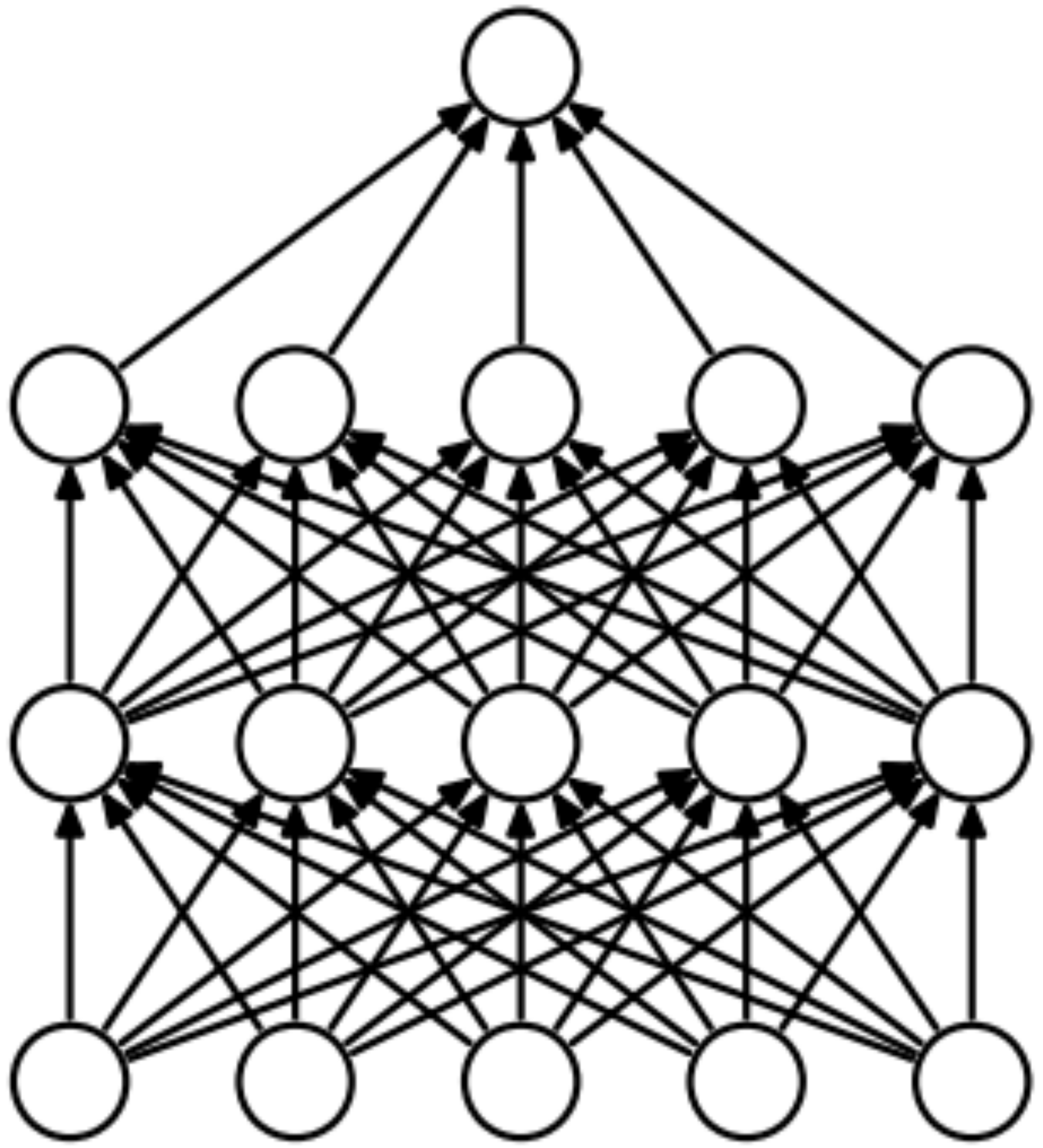
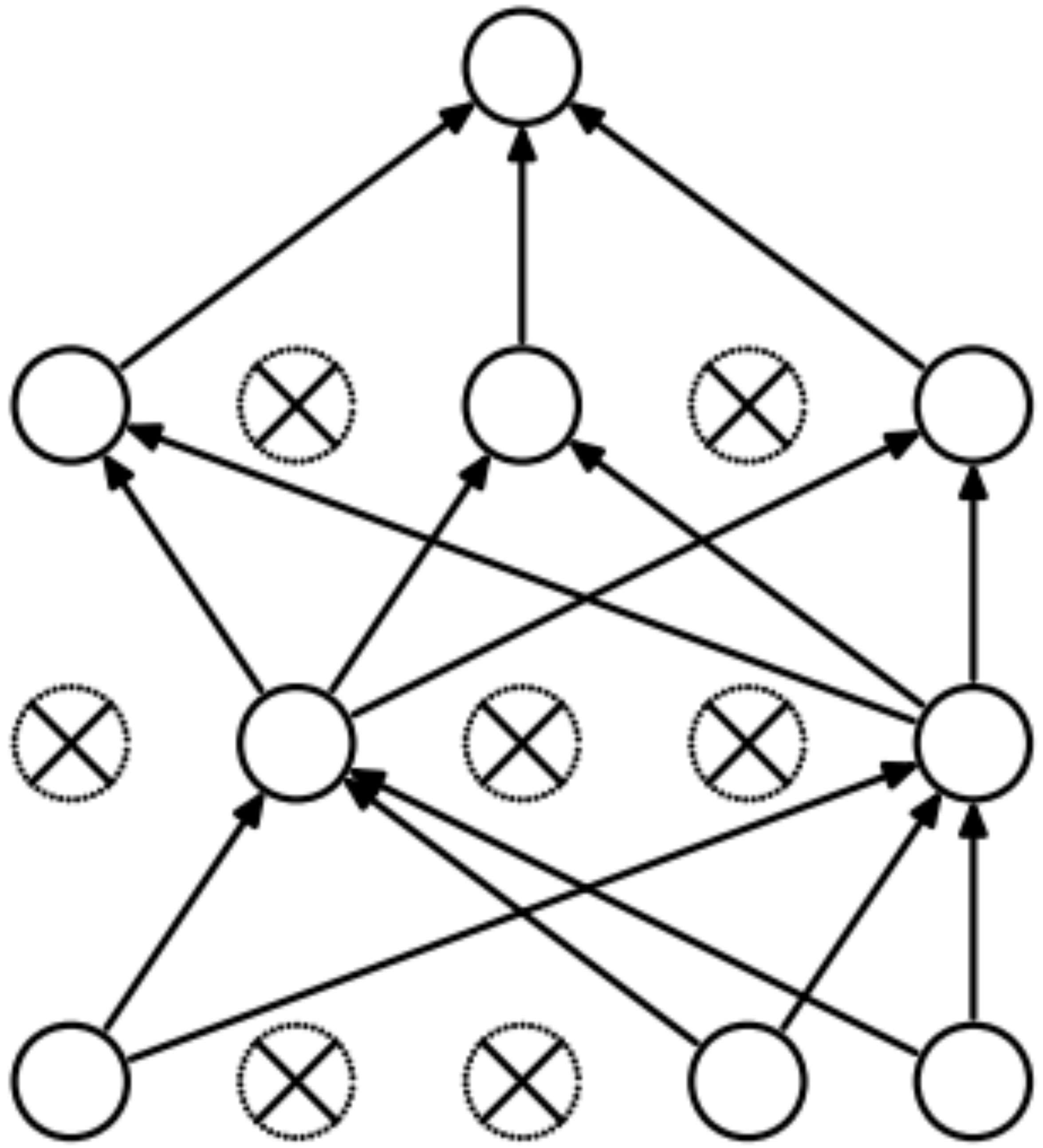
  - Want variance of inputs and gradients for each layer to be the same
- Batch normalization (Ioffe and Szegedy, 2015): periodically shift+rescale each layer to have mean 0 and variance 1 over a batch (useful if net is deep)

Dropout

- Probabilistically zero out parts of the network during training to prevent overfitting, use whole network at test time



(a) Standard Neural Net



(b) After applying dropout.

Srivastava et al. (2014)

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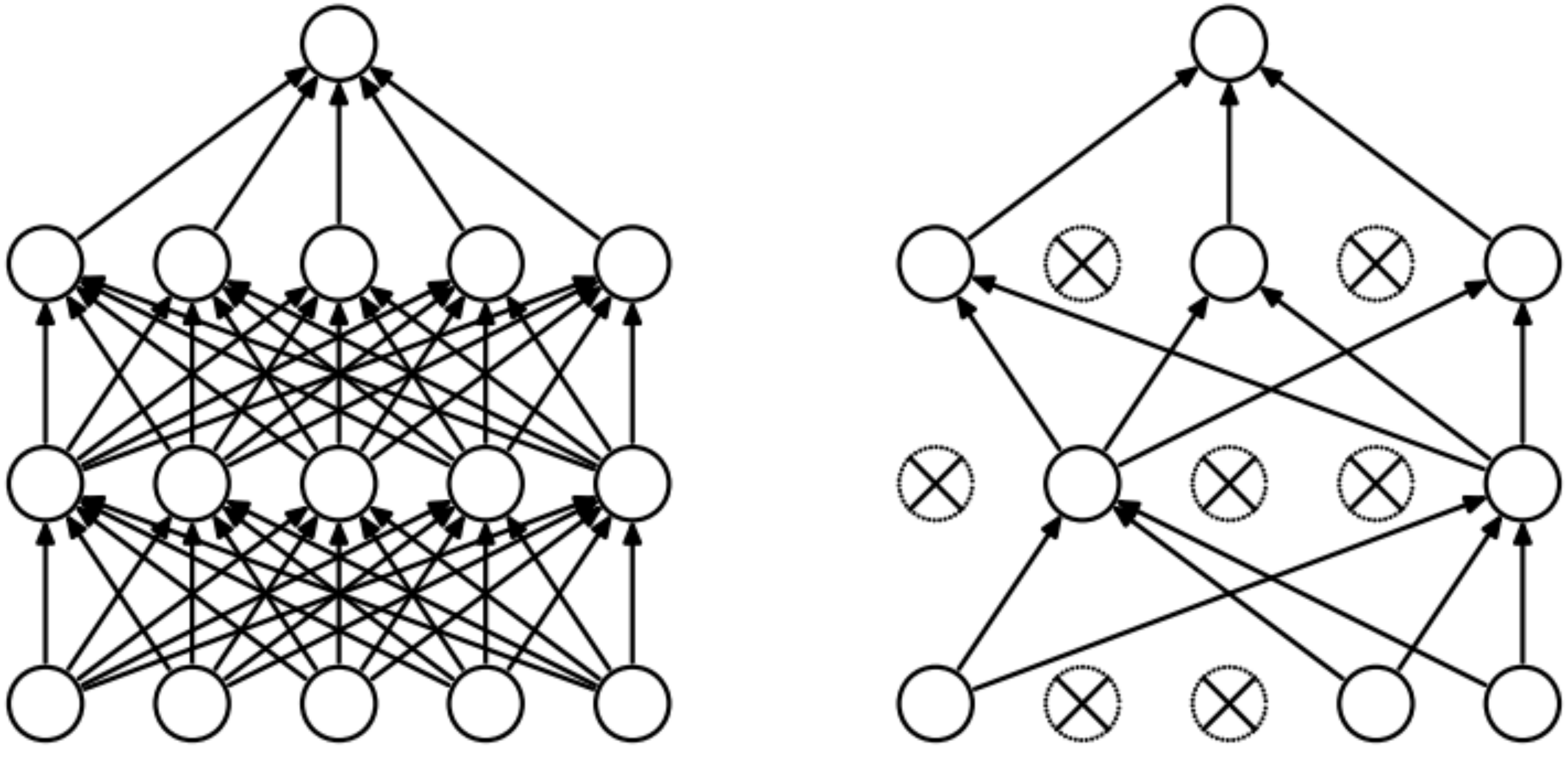

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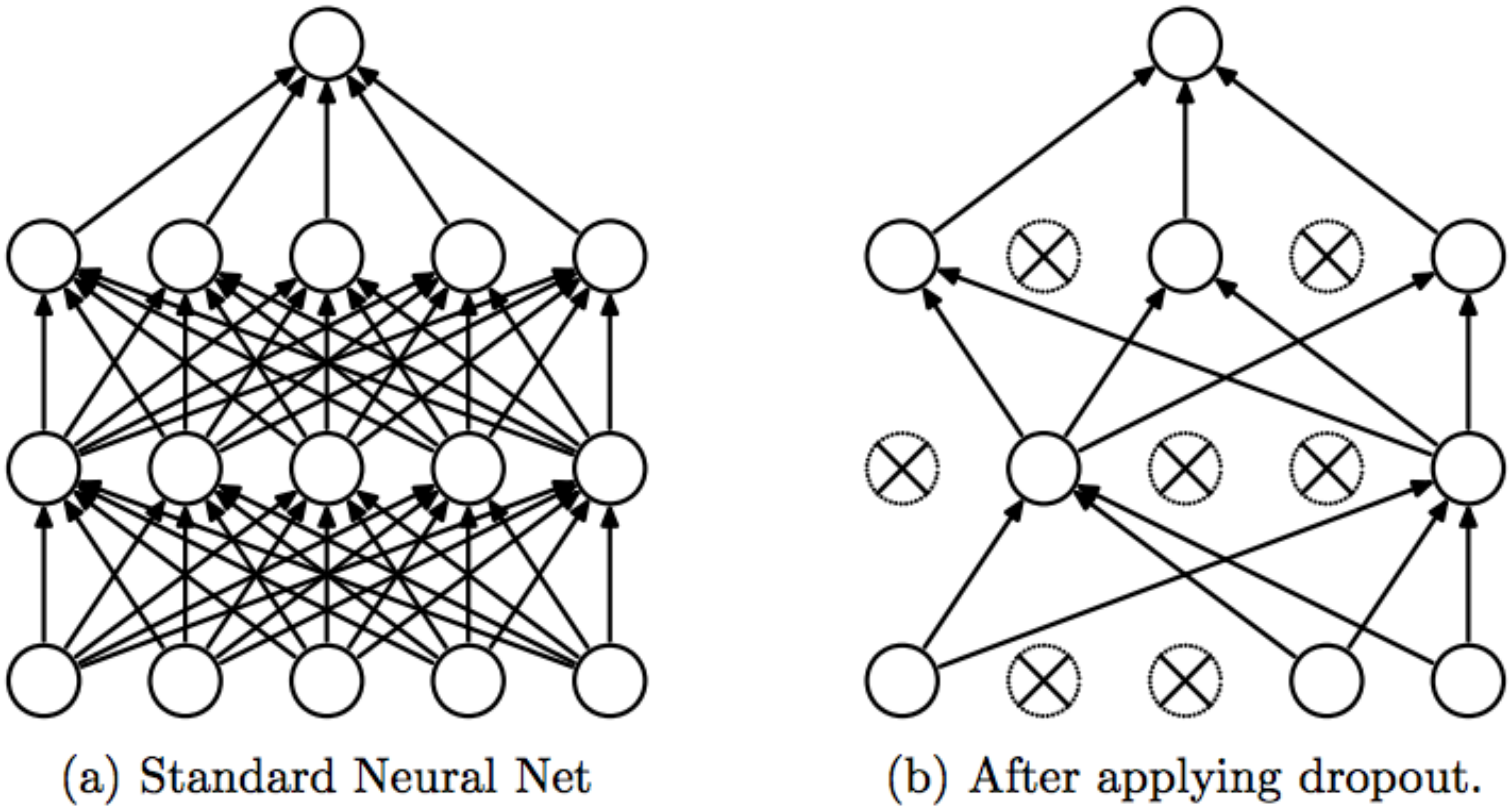

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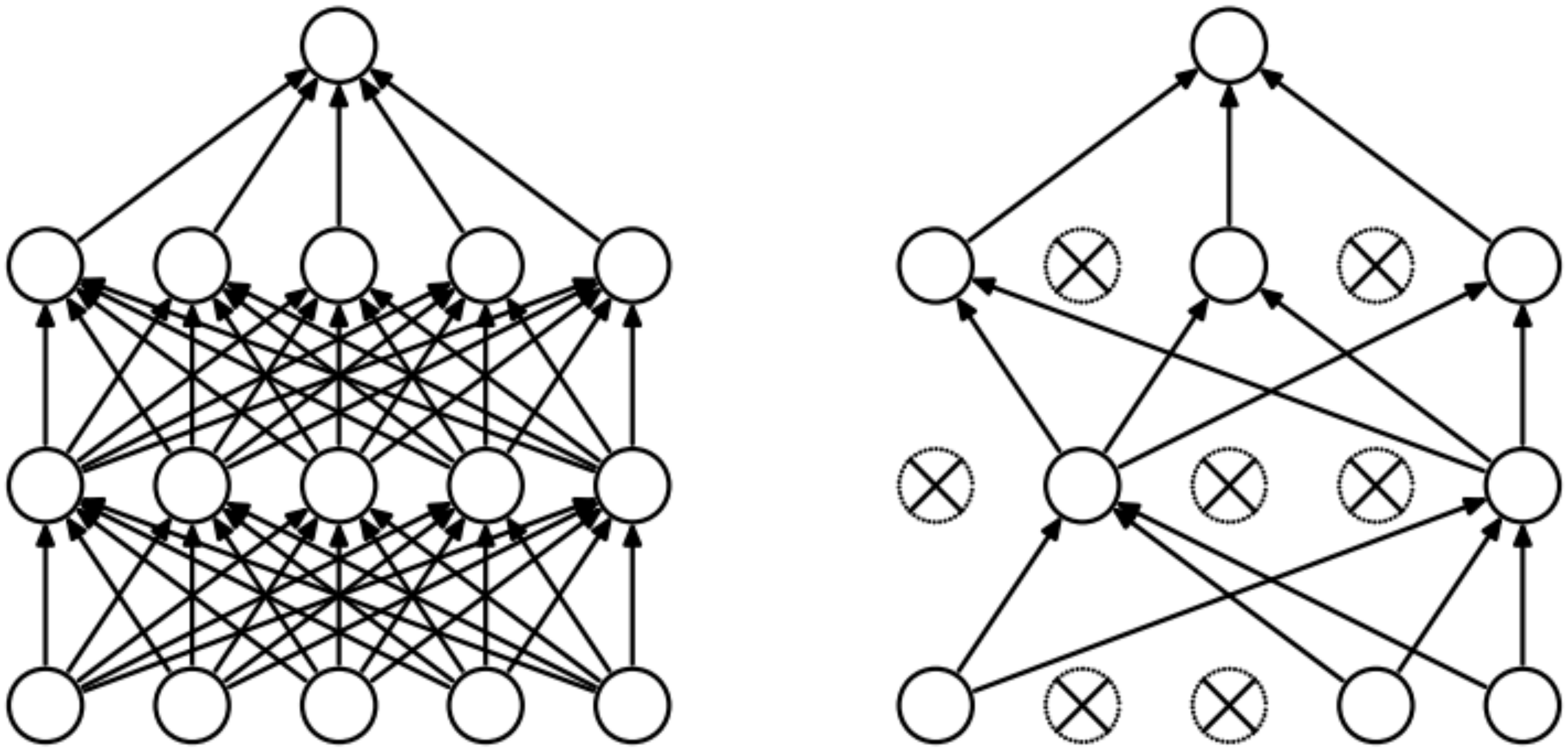

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- One line in Pytorch/Tensorflow

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Optimizer

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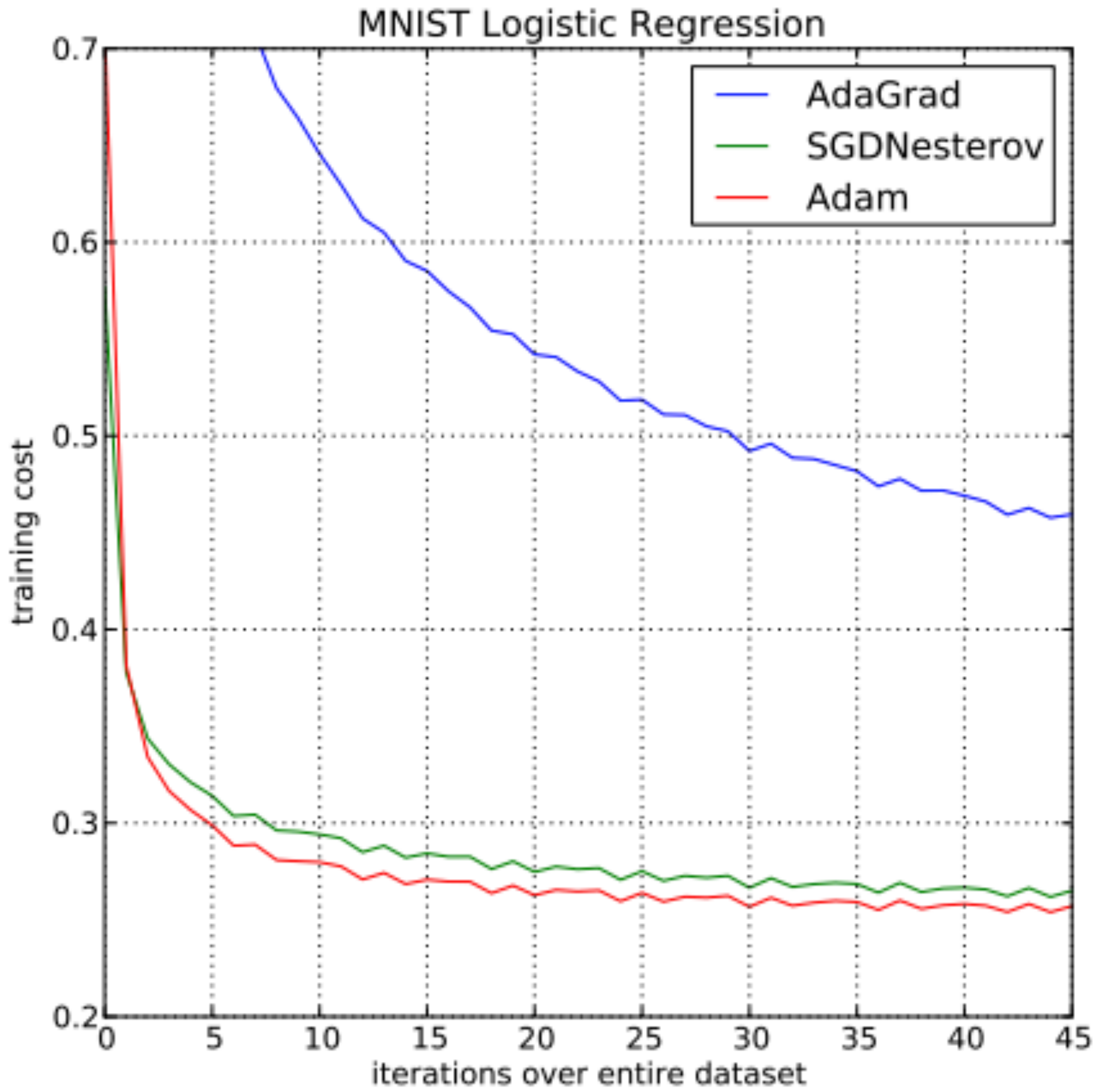

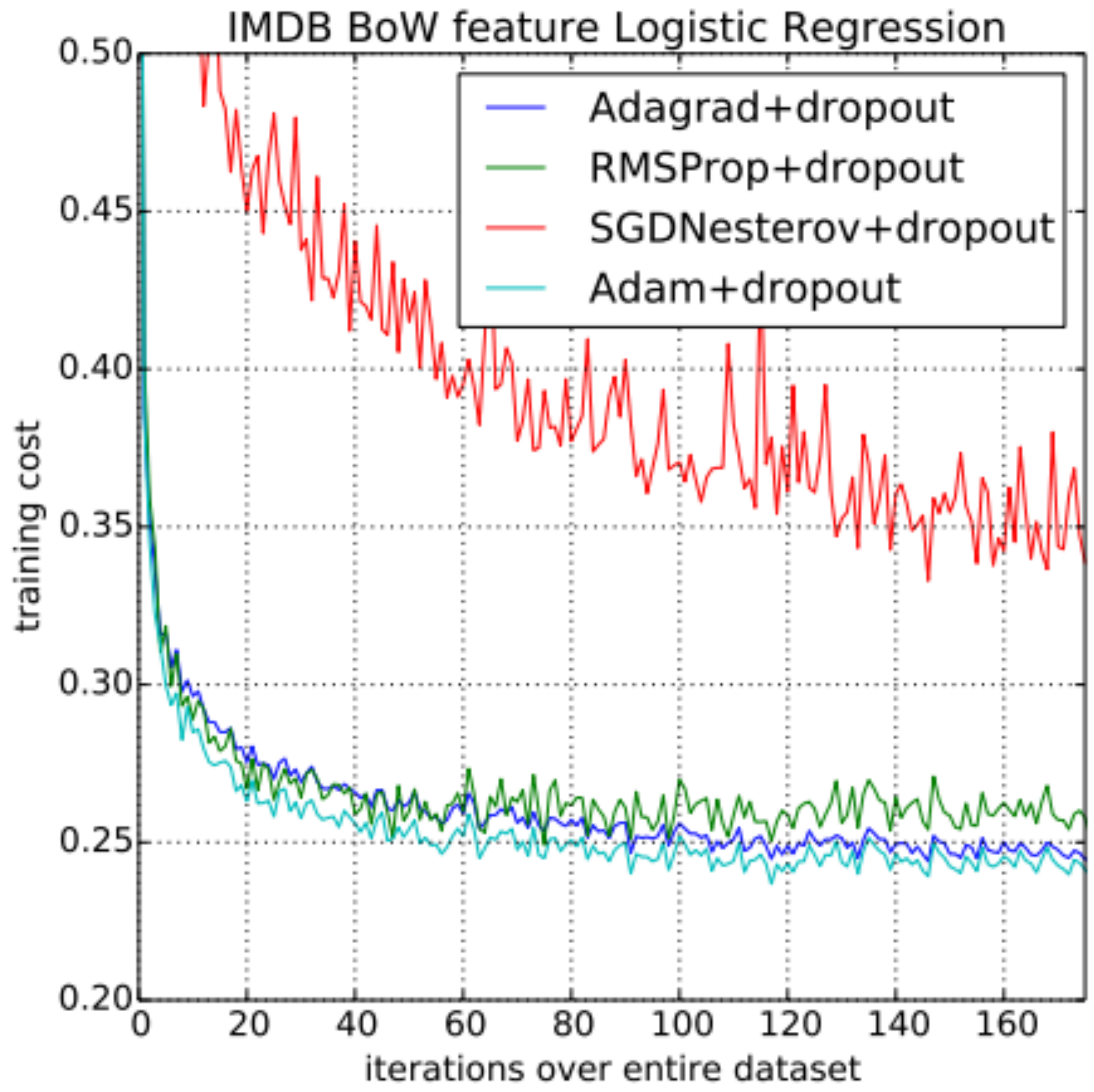

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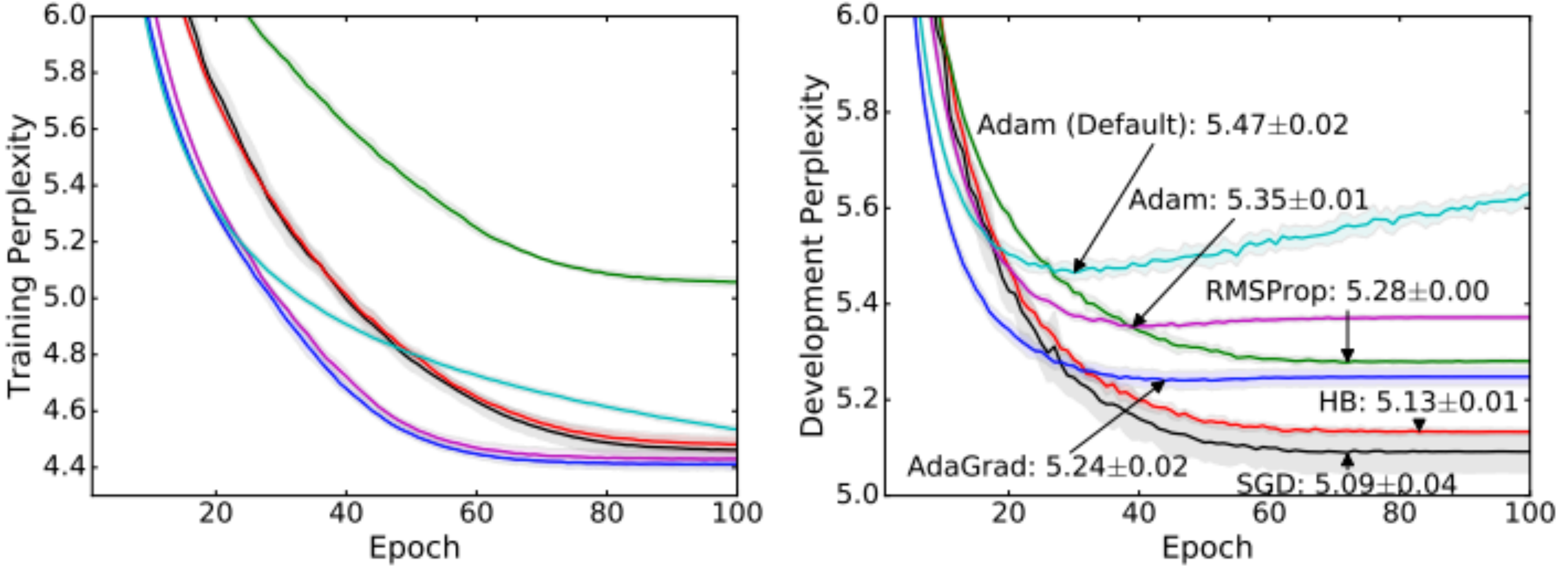

(e) Generative Parsing (Training Set) **(f)** Generative Parsing (Development Set)

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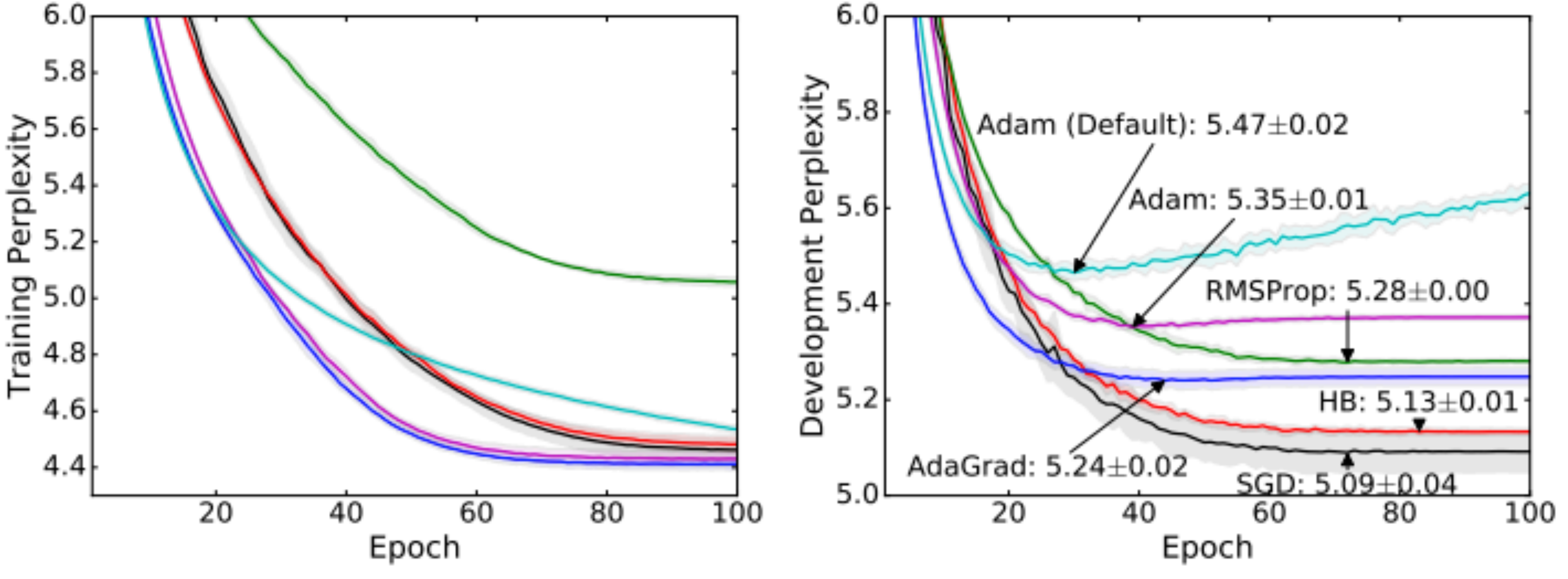
- Check dev set periodically, decrease learning rate if not making progress



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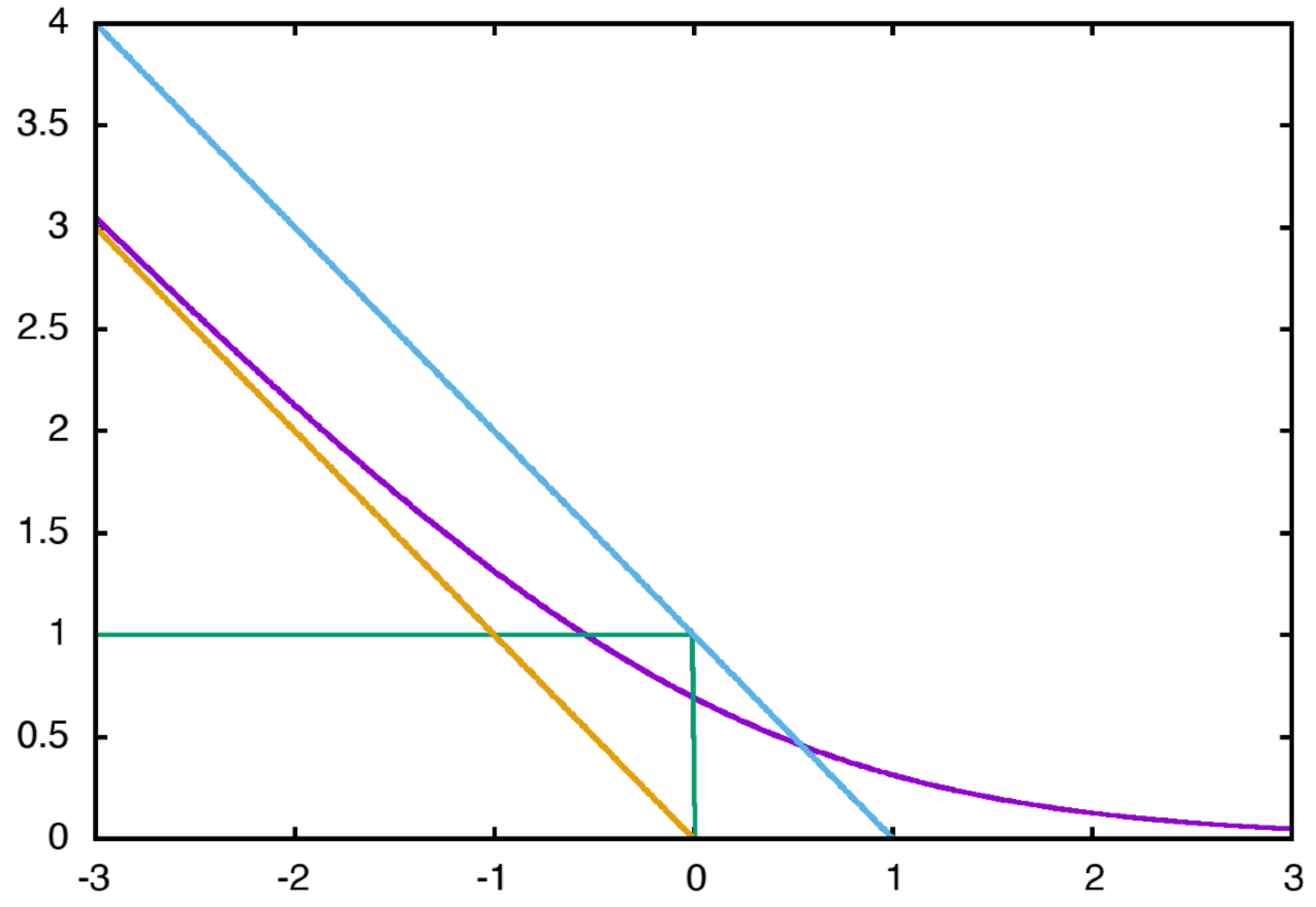

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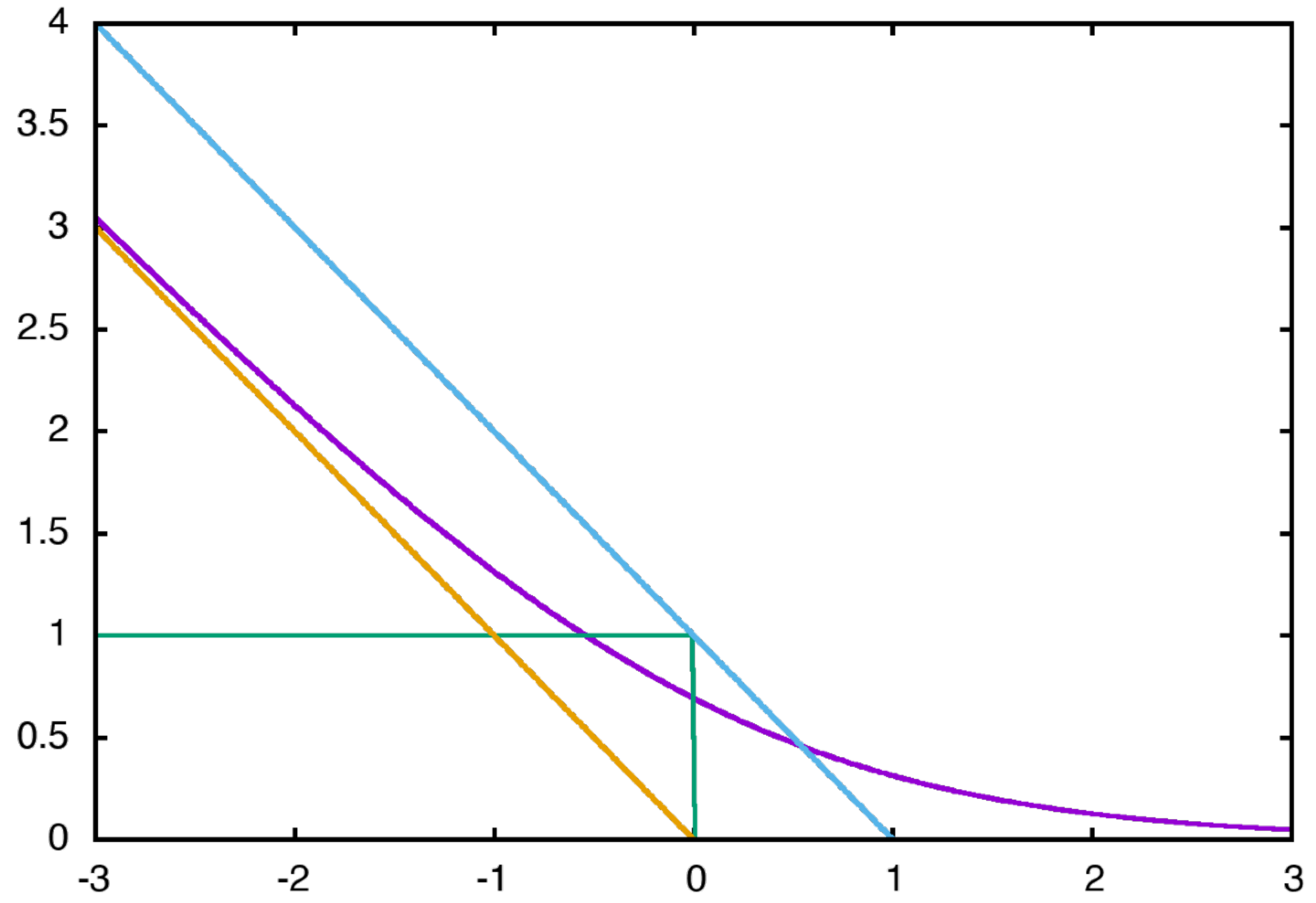

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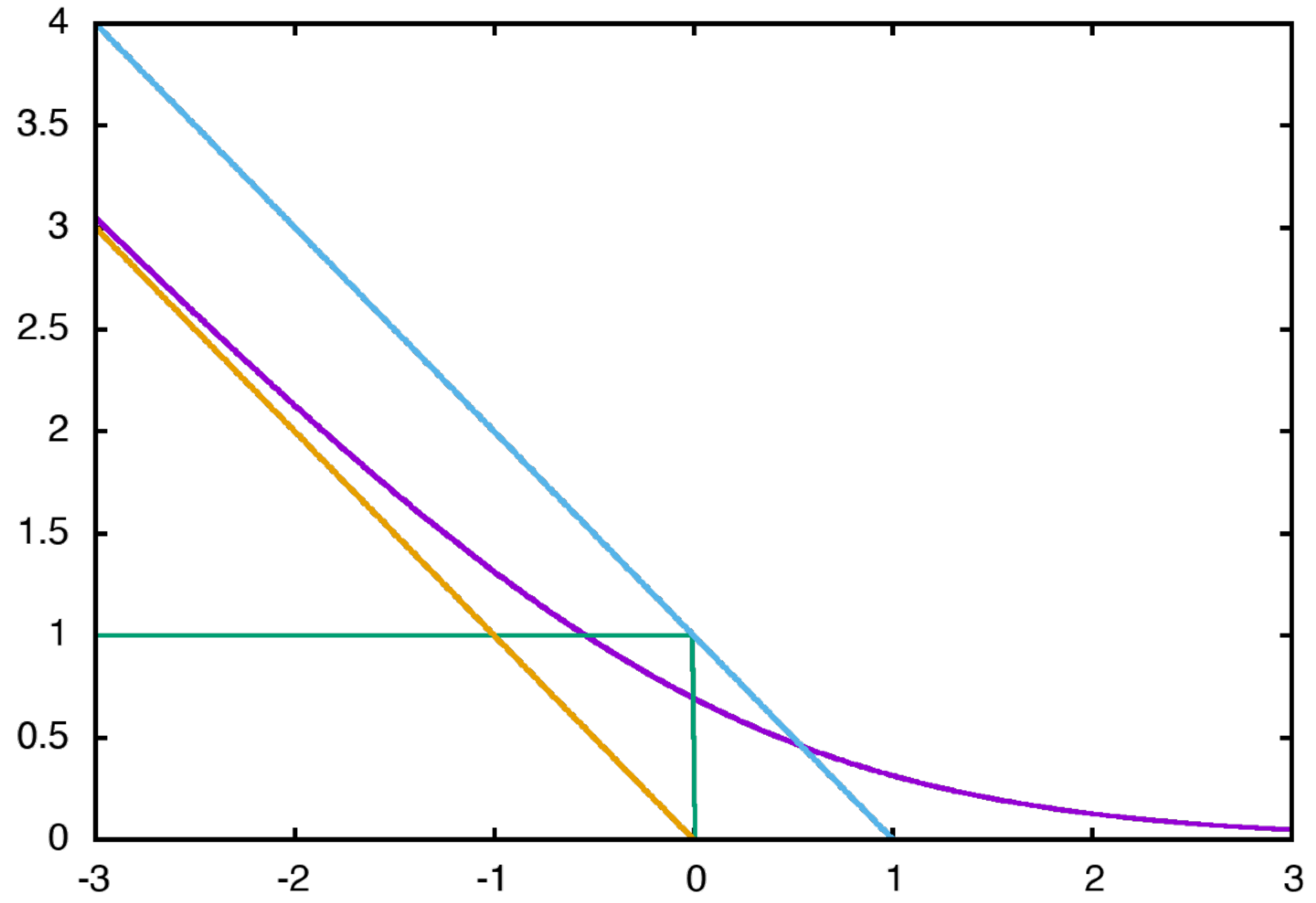

- Inference: define the network, your library of choice takes care of it (mostly…)
- Training: lots of choices for optimization/hyperparameters

Word Representations

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slide credit: Dan Klein

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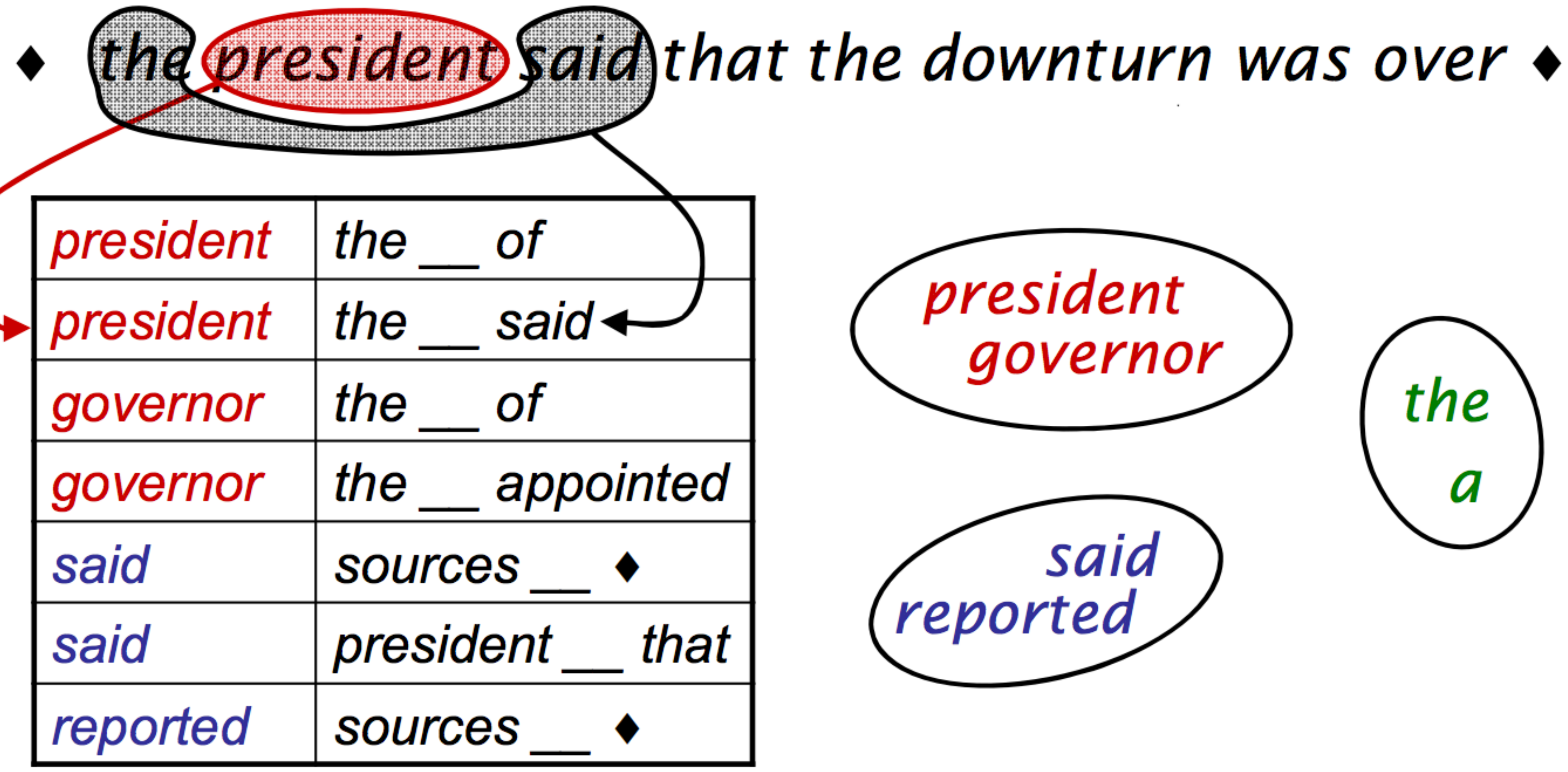
- Neural networks work very well at continuous data, but words are discrete
- Continuous model <-> expects continuous semantics from input
- “You shall know a word by the company it keeps” Firth (1957)



[Finch and Chater 92, Shuetze 93, many others]

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Discrete Word Representations

Brown et al. (1992)

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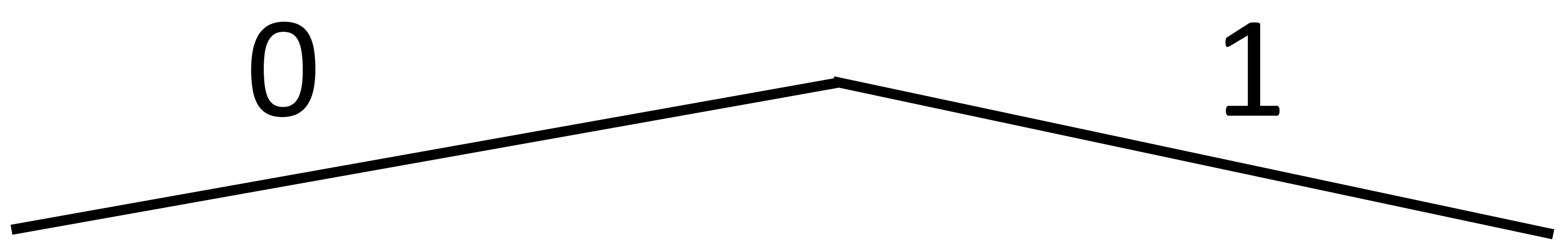

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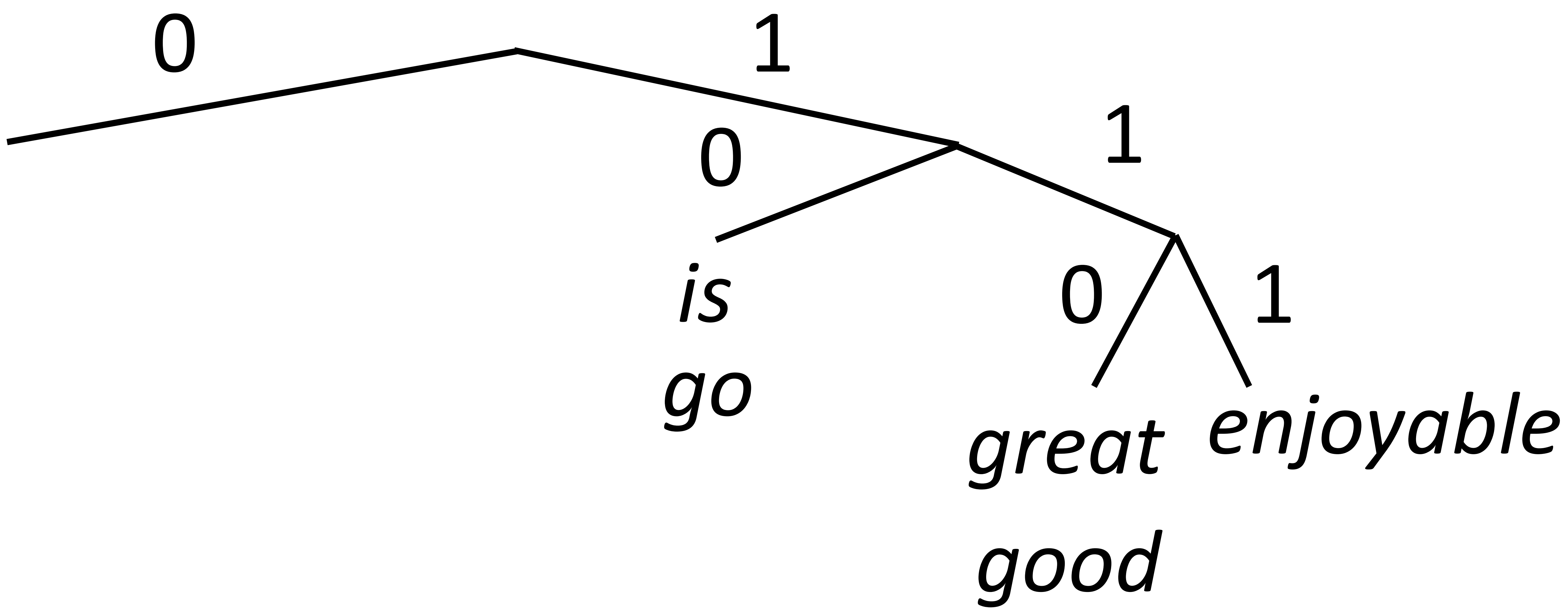

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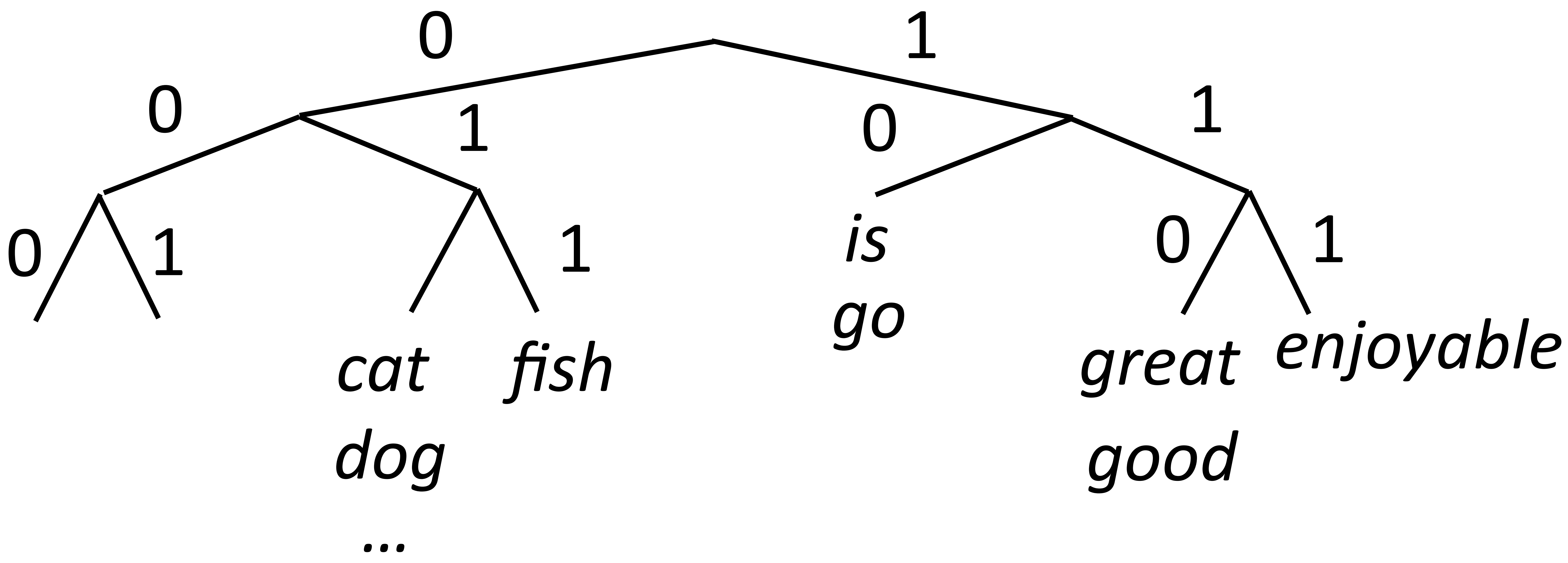

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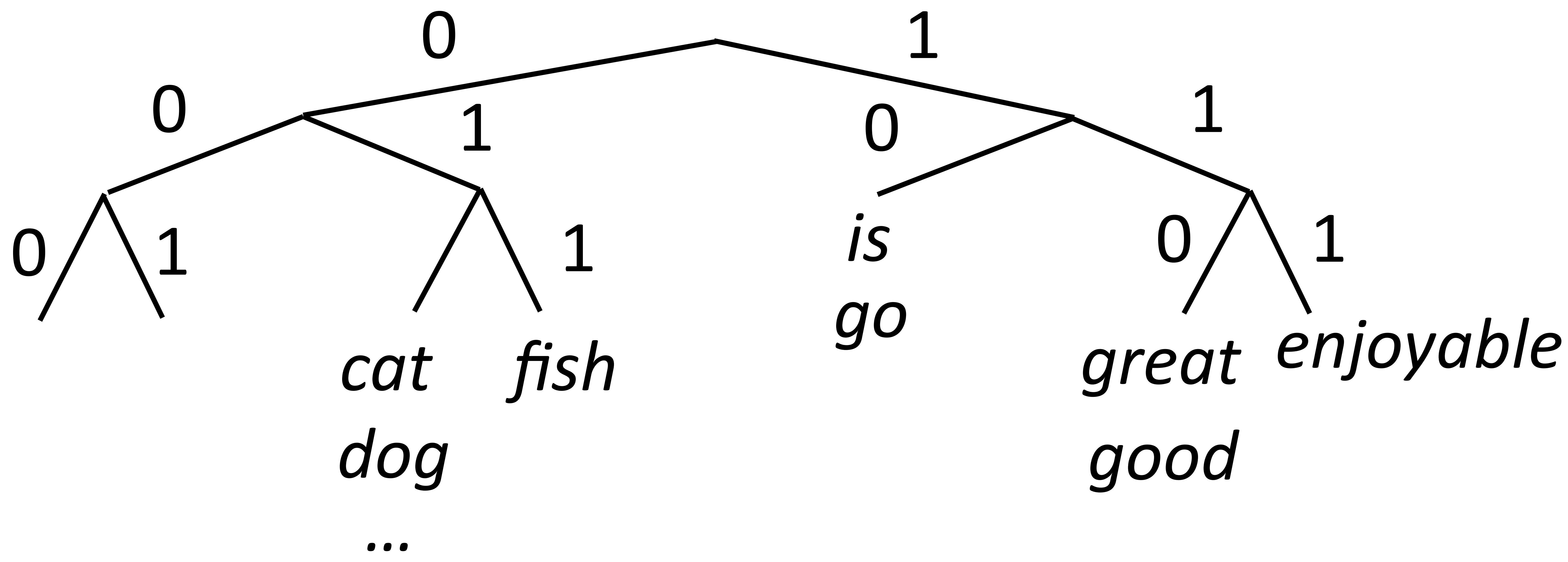

- Maximize $P(w_i|w_{i-1}) = P(c_i|c_{i-1})P(w_i|c_i)$

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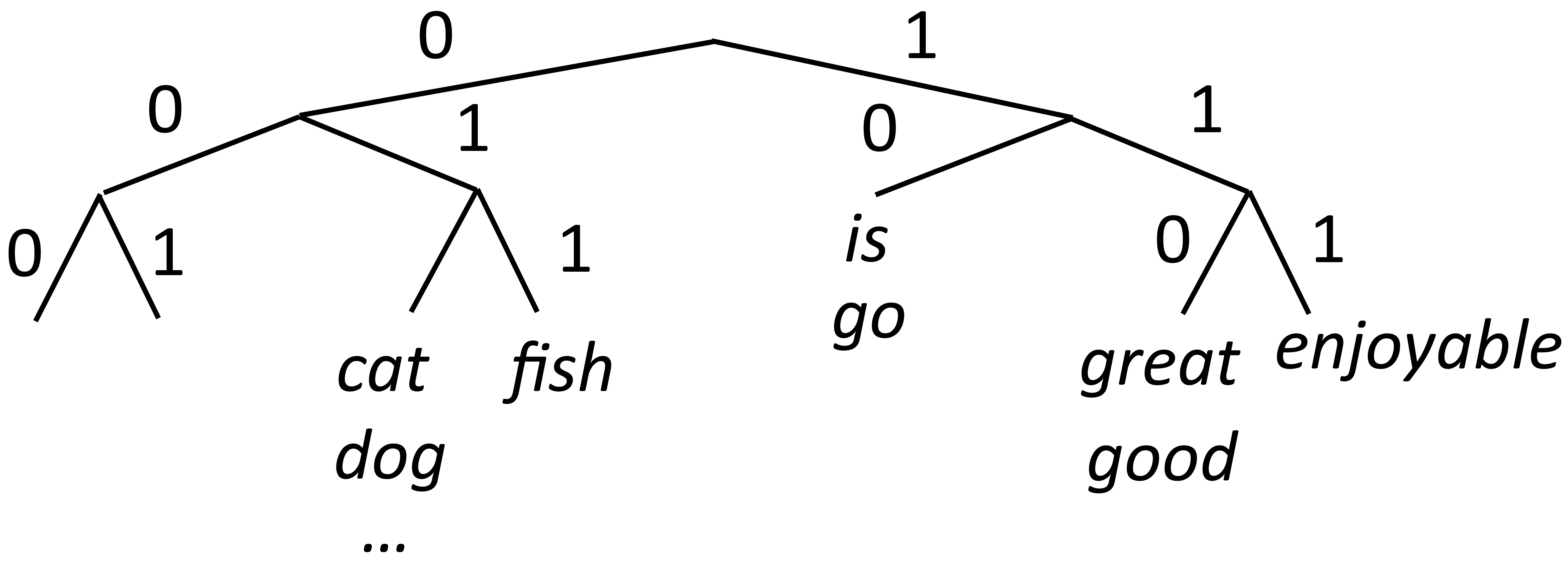

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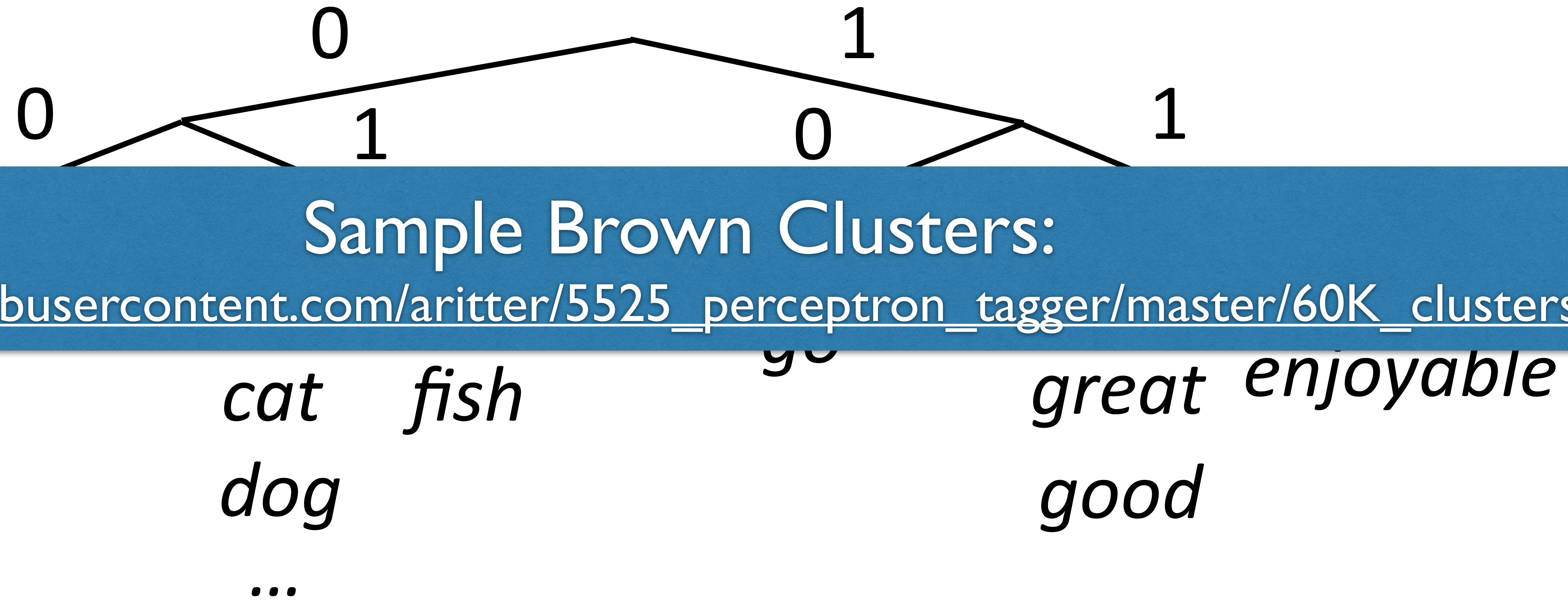

Sample Brown Clusters:

- https://raw.githubusercontent.com/aritter/5525_perceptron_tagger/master/60K_clusters.bits.txt

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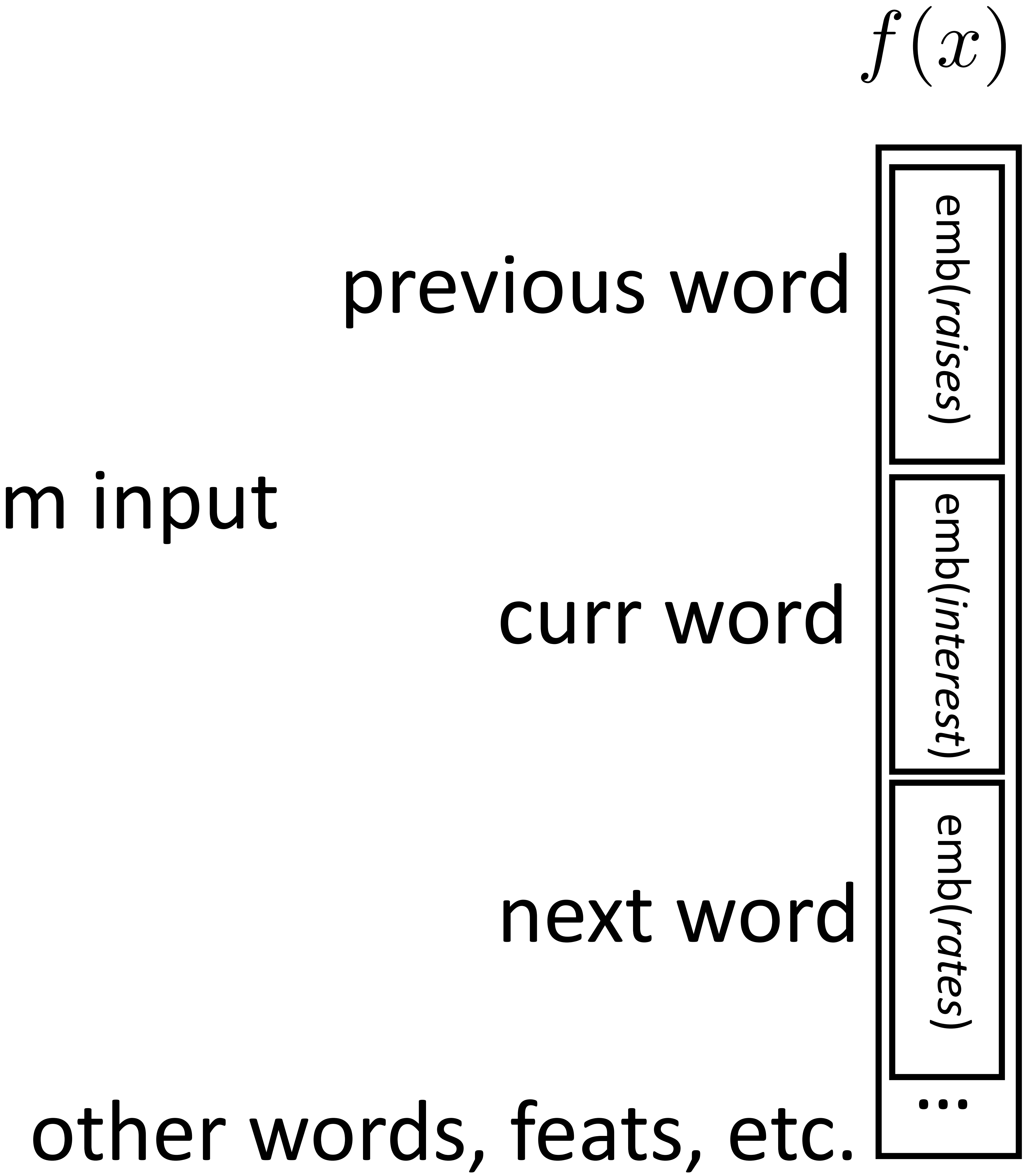
Word Embeddings

- Part-of-speech tagging with FFNNs

??

Fed raises ***interest*** *rates in order to …*

- Word embeddings for each word form input



Botha et al. (2017)

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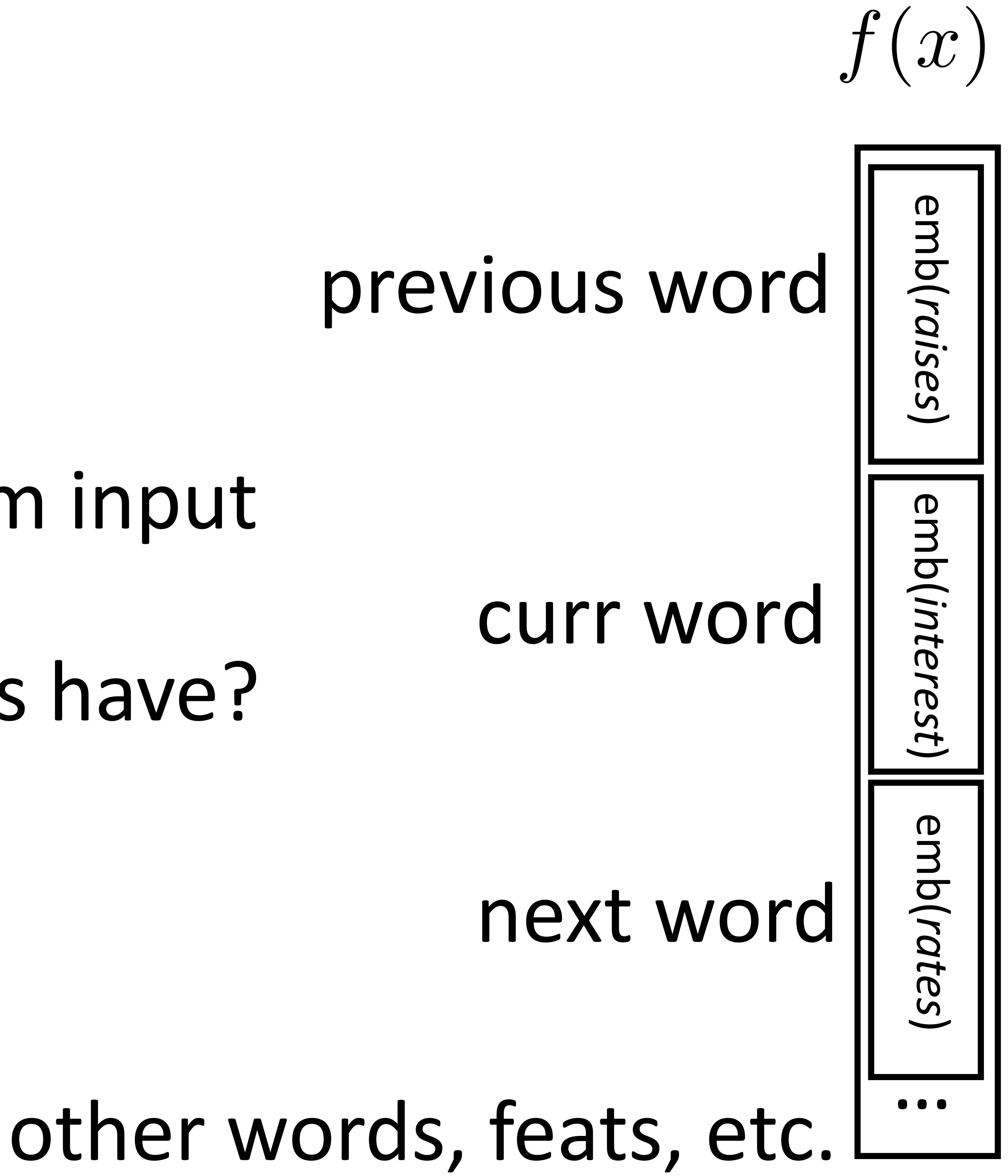

- Word embeddings for each word form input

- What properties should these vectors have?

Botha et al. (2017)

Word Embeddings

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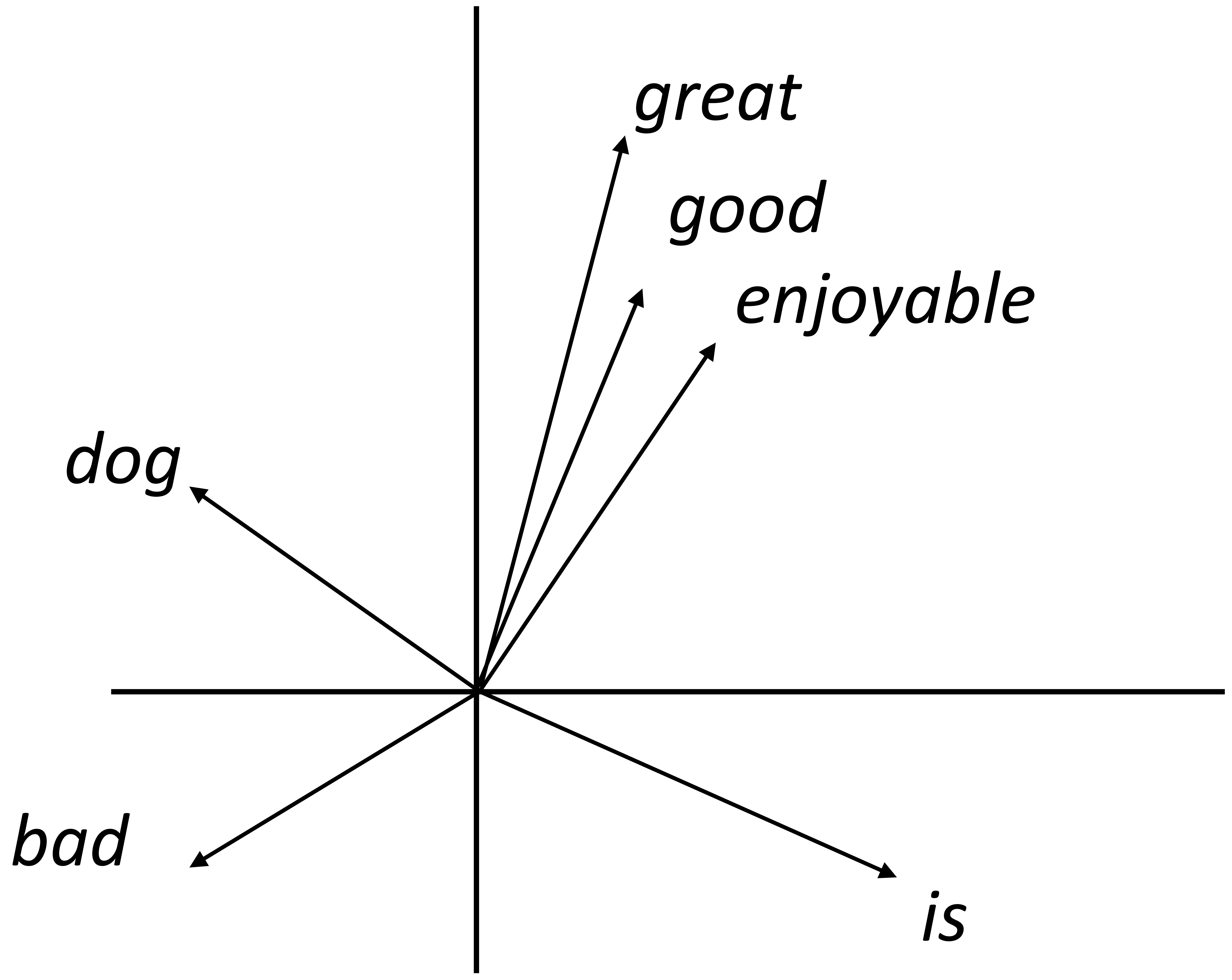
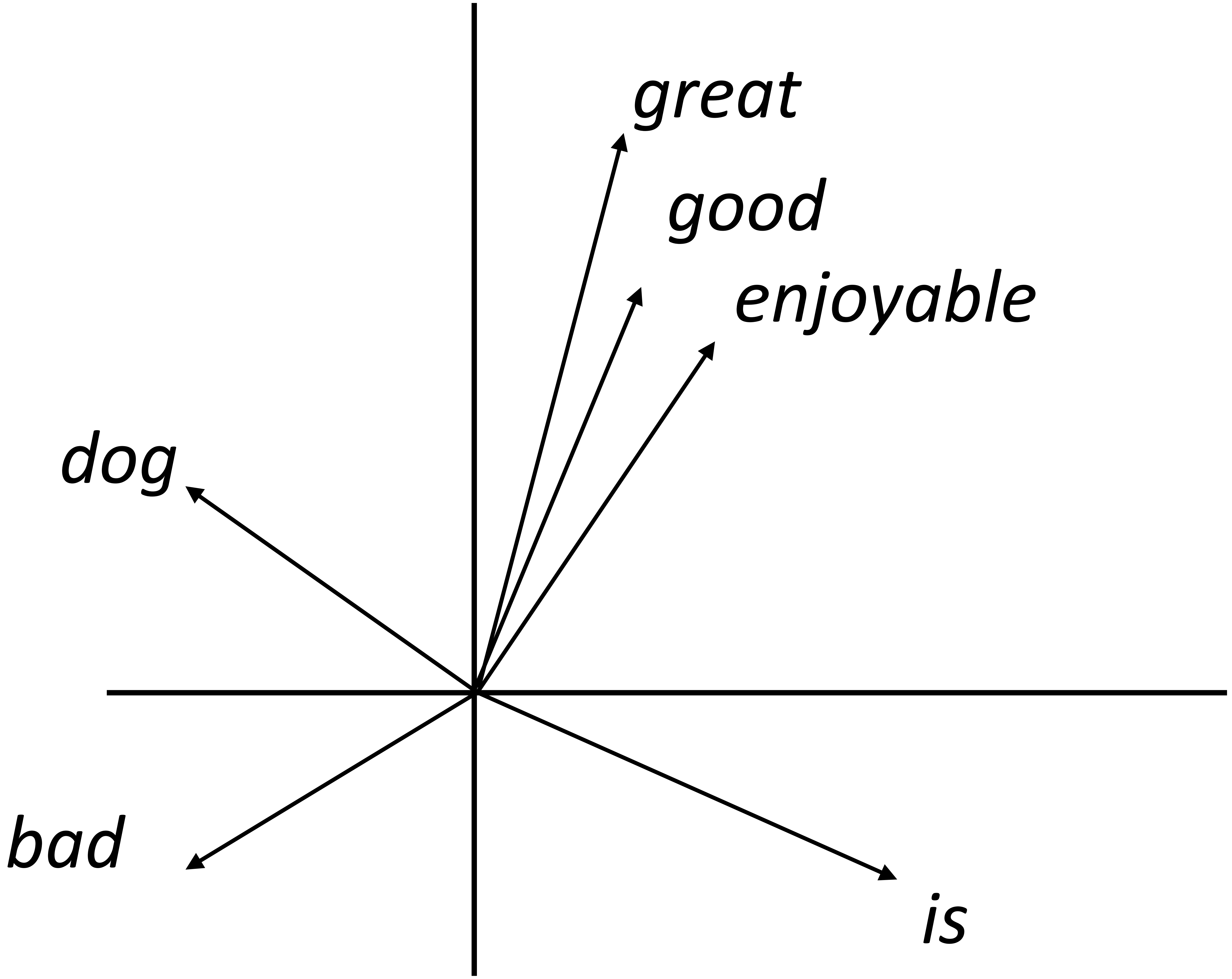


Word Embeddings

- Want a vector space where similar words have similar embeddings



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the movie was great

≈

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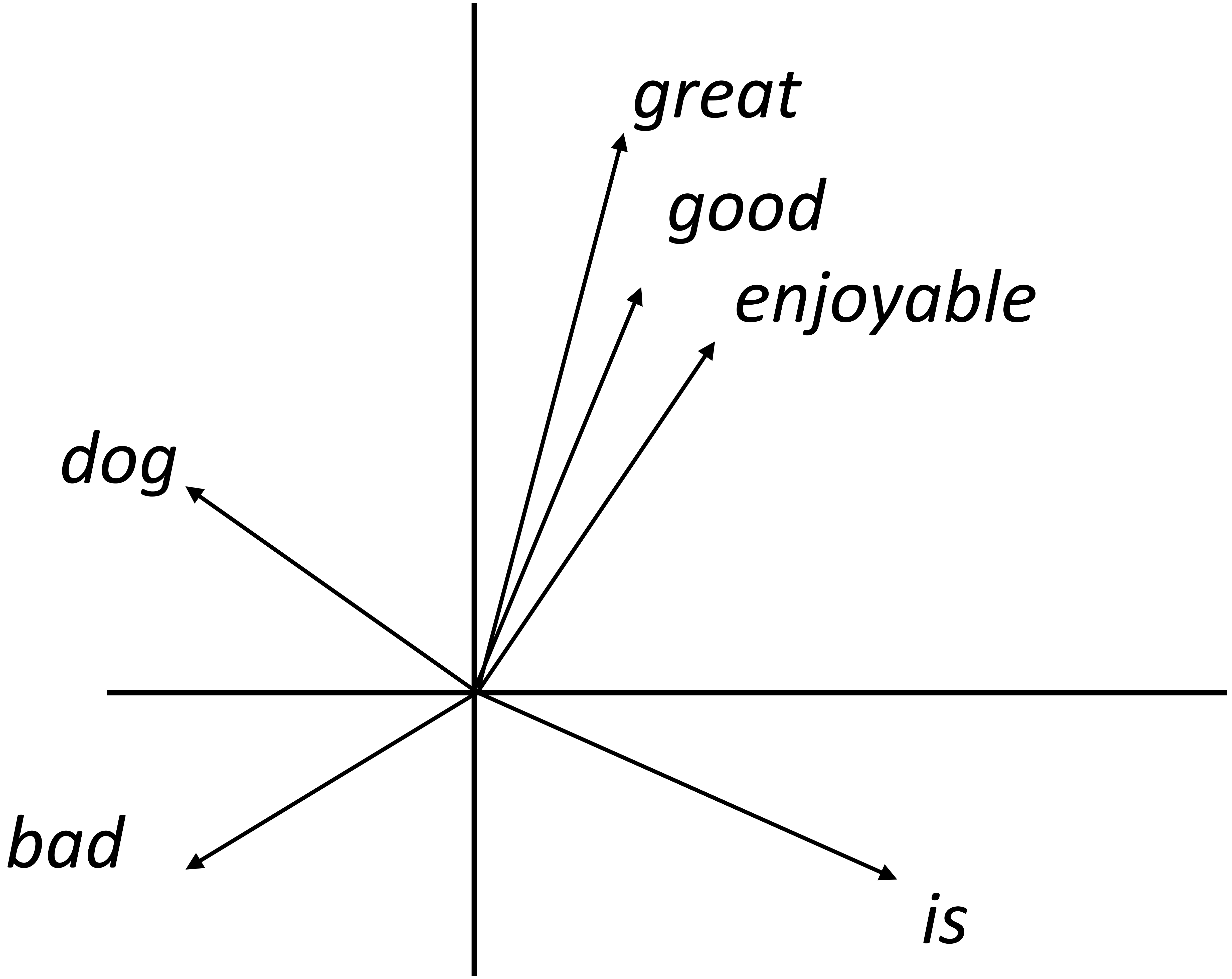

Word Embeddings

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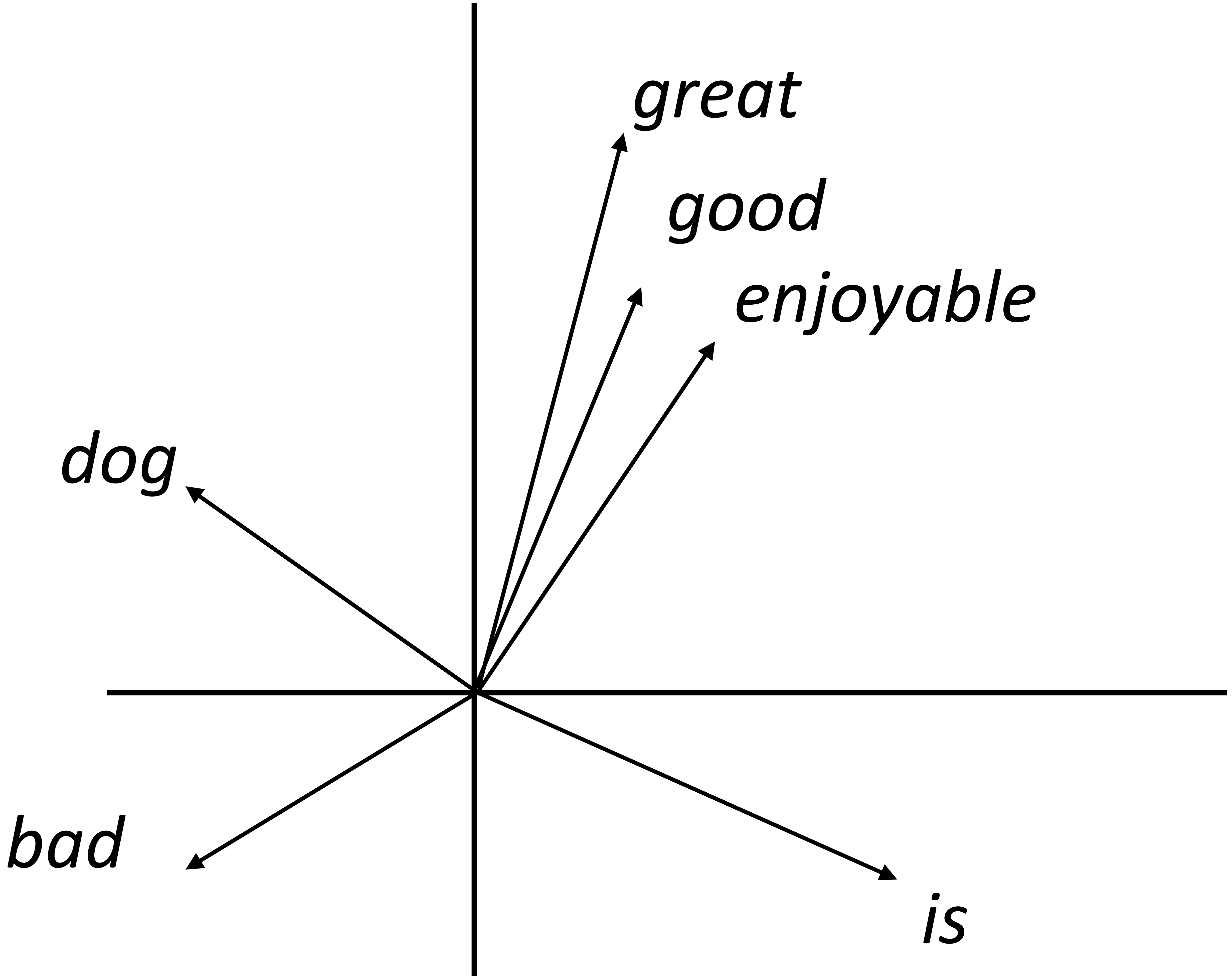
- Goal: come up with a way to produce these embeddings



word2vec/GloVe

Continuous Bag-of-Words

- Predict word from context

*the dog **bit** the man*

Mikolov et al. (2013)

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d-dimensional word embeddings

dog

the

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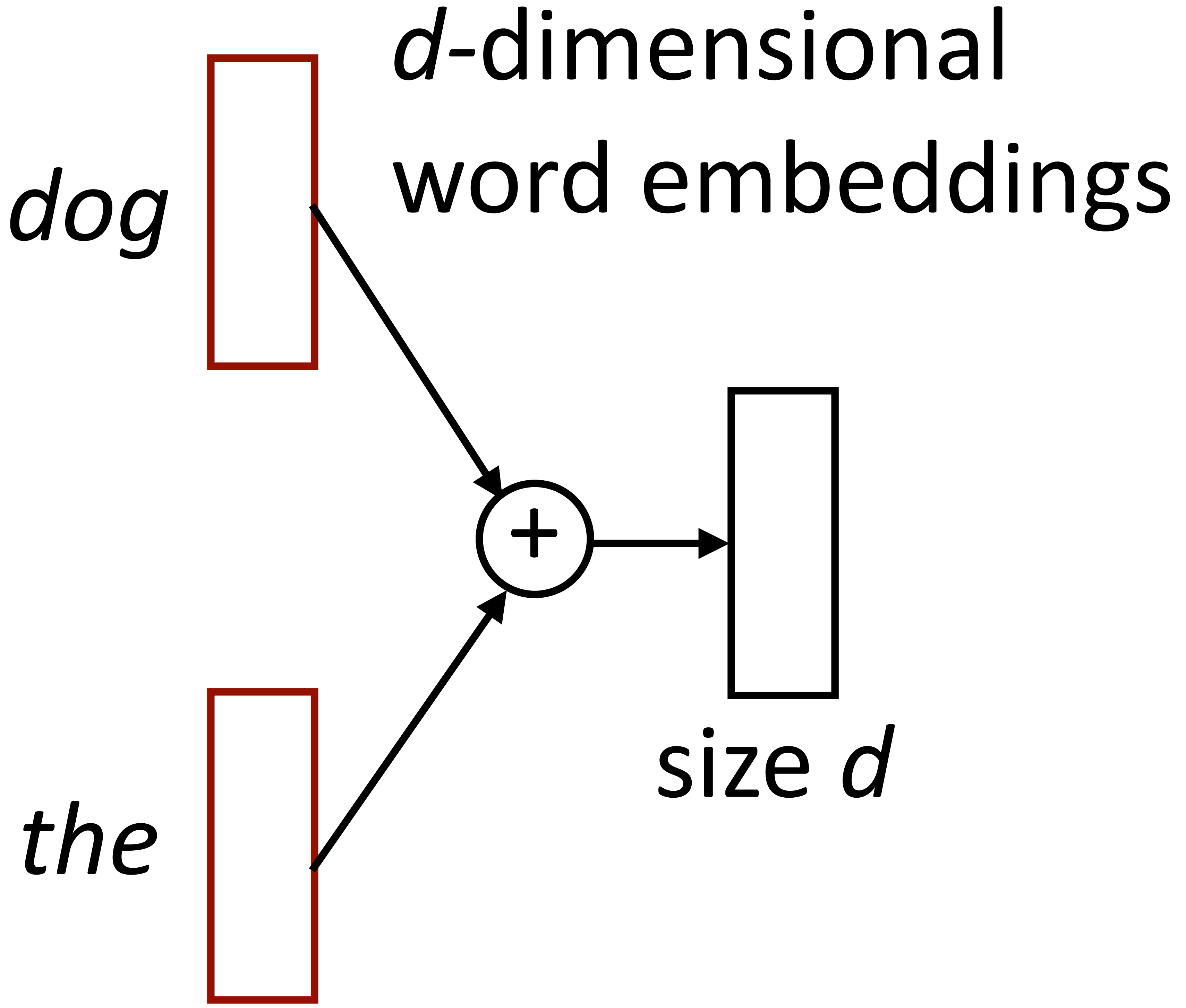

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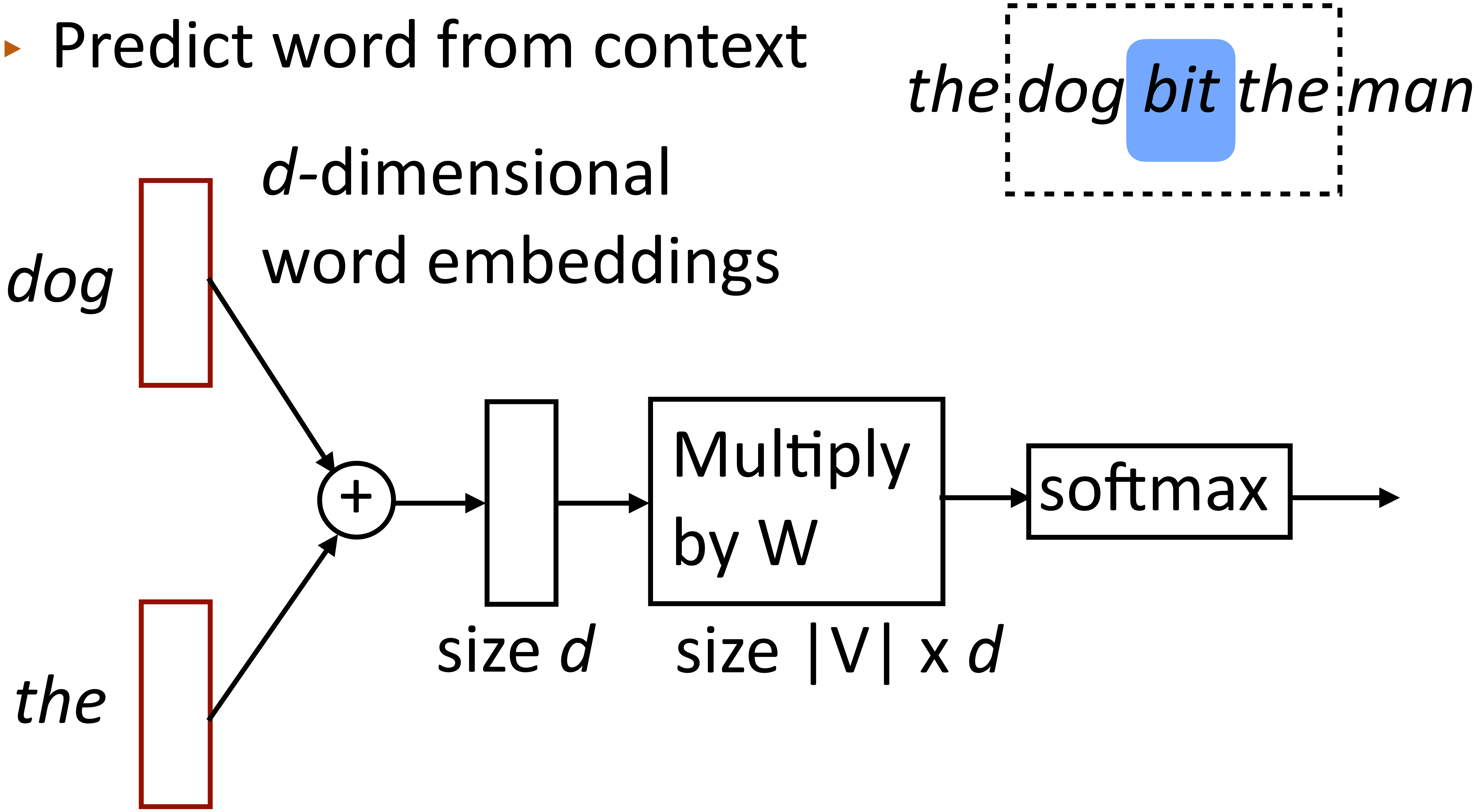

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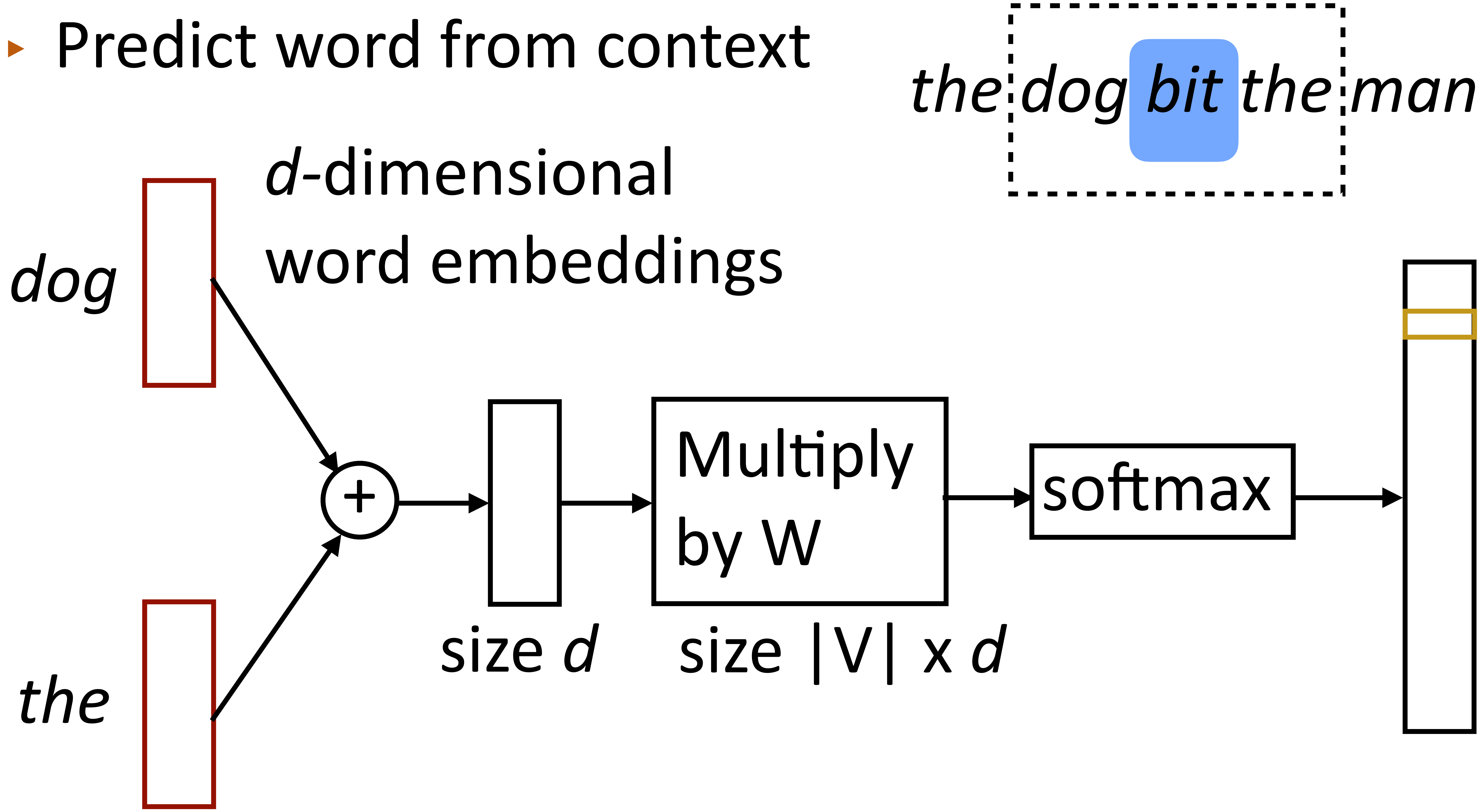
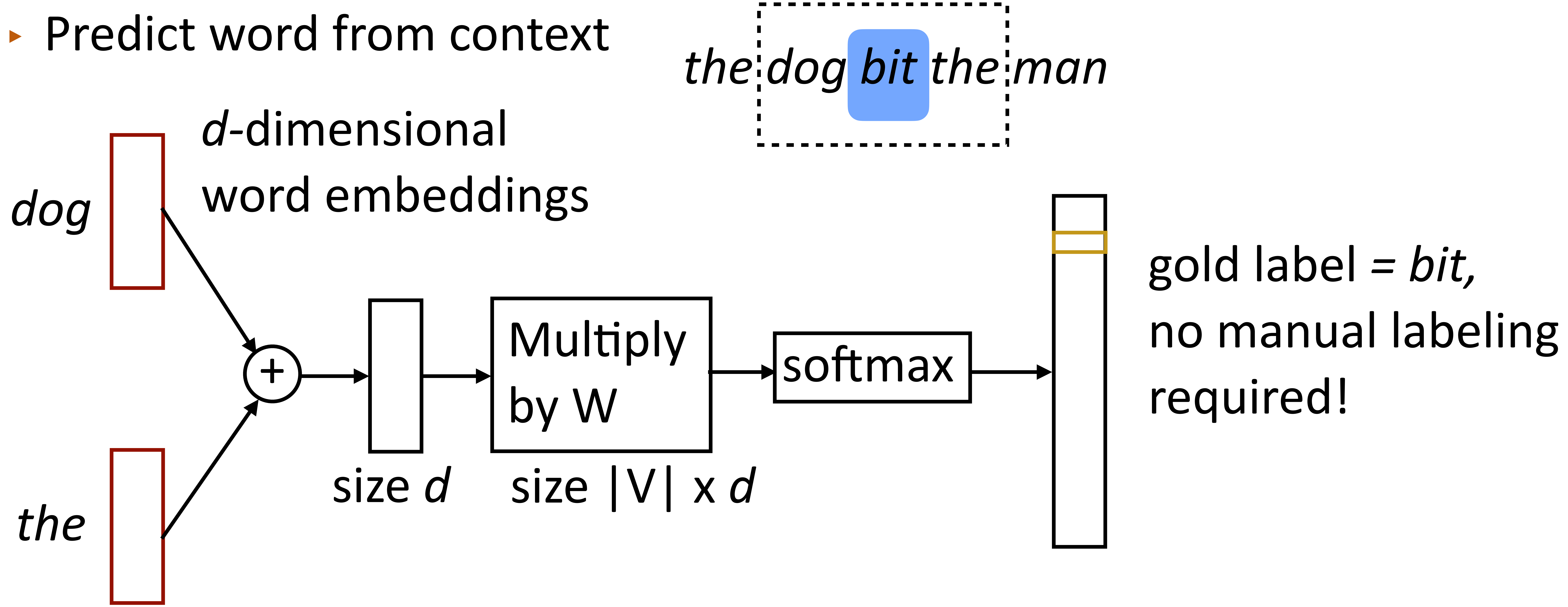


Mikolov et al. (2013)

Continuous Bag-of-Words

- Predict word from context

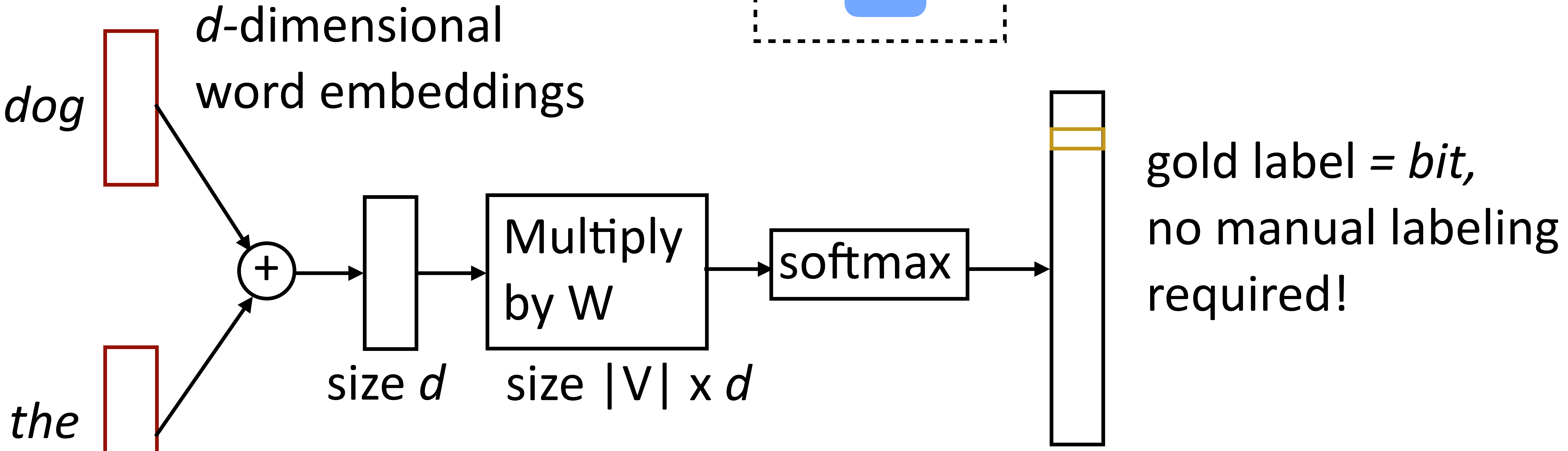


Mikolov et al. (2013)

Continuous Bag-of-Words

- Predict word from context

the dog ***bit*** *the man*



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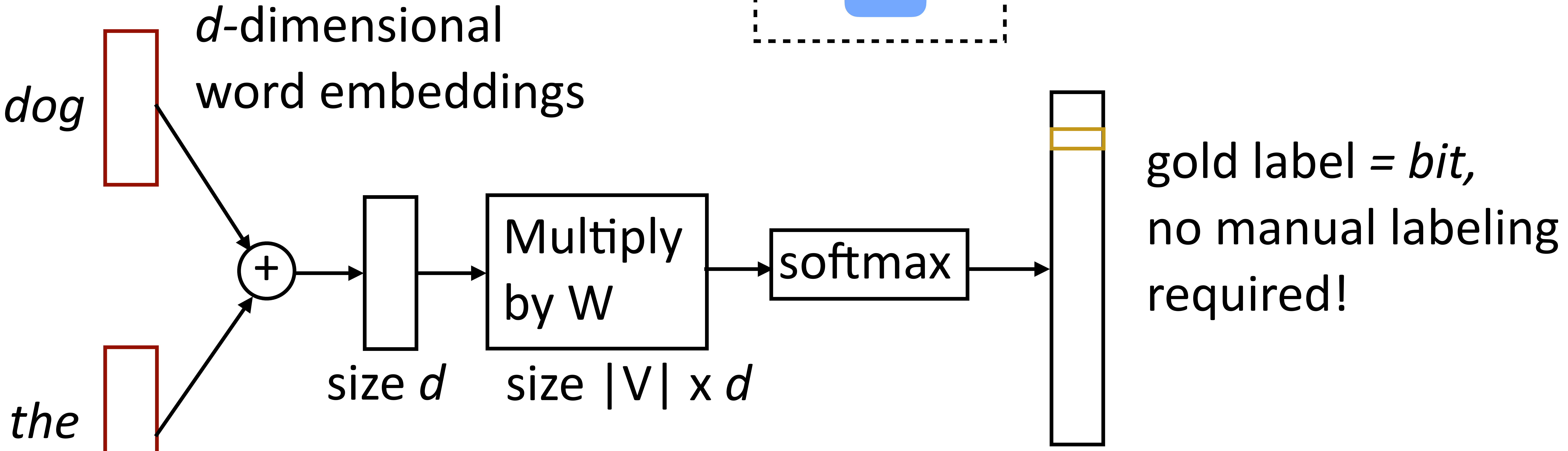

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- Parameters: *d* x |V| (one *d*-length vector per voc word),
  |V| x *d* output parameters (W)

Mikolov et al. (2013)

Skip-Gram

- Predict one word of context from word

the dog bit the man

Mikolov et al. (2013)

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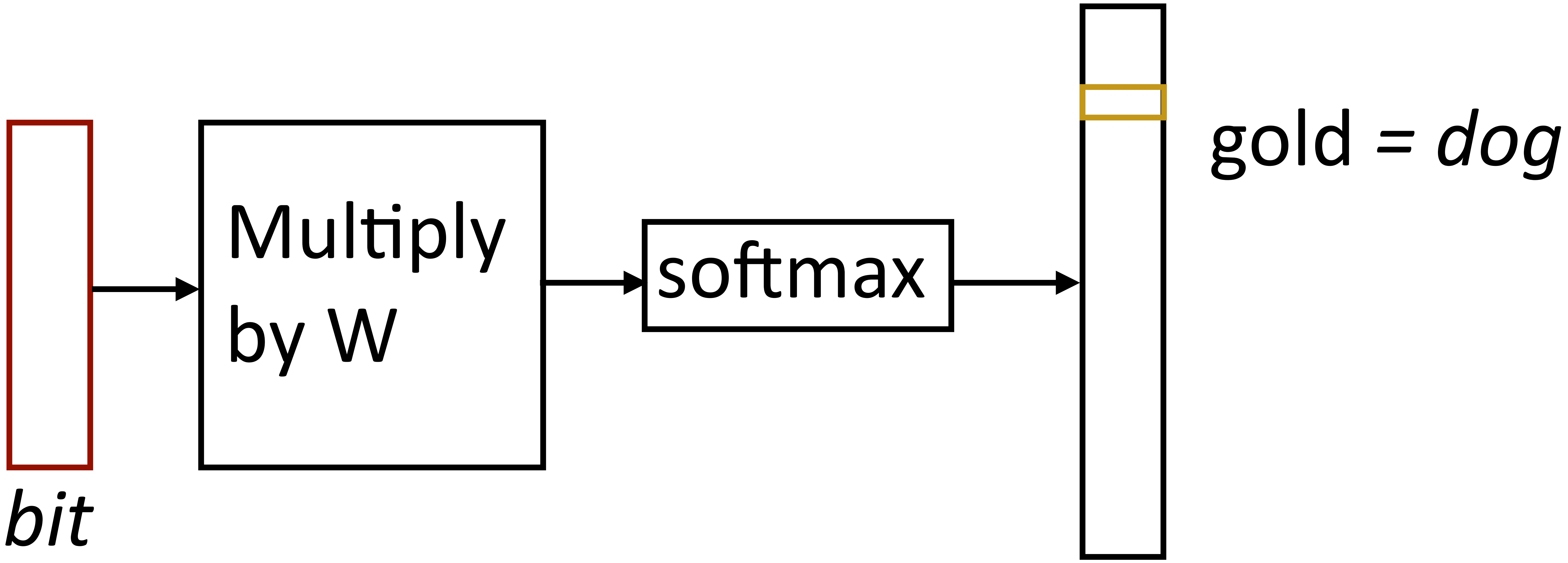

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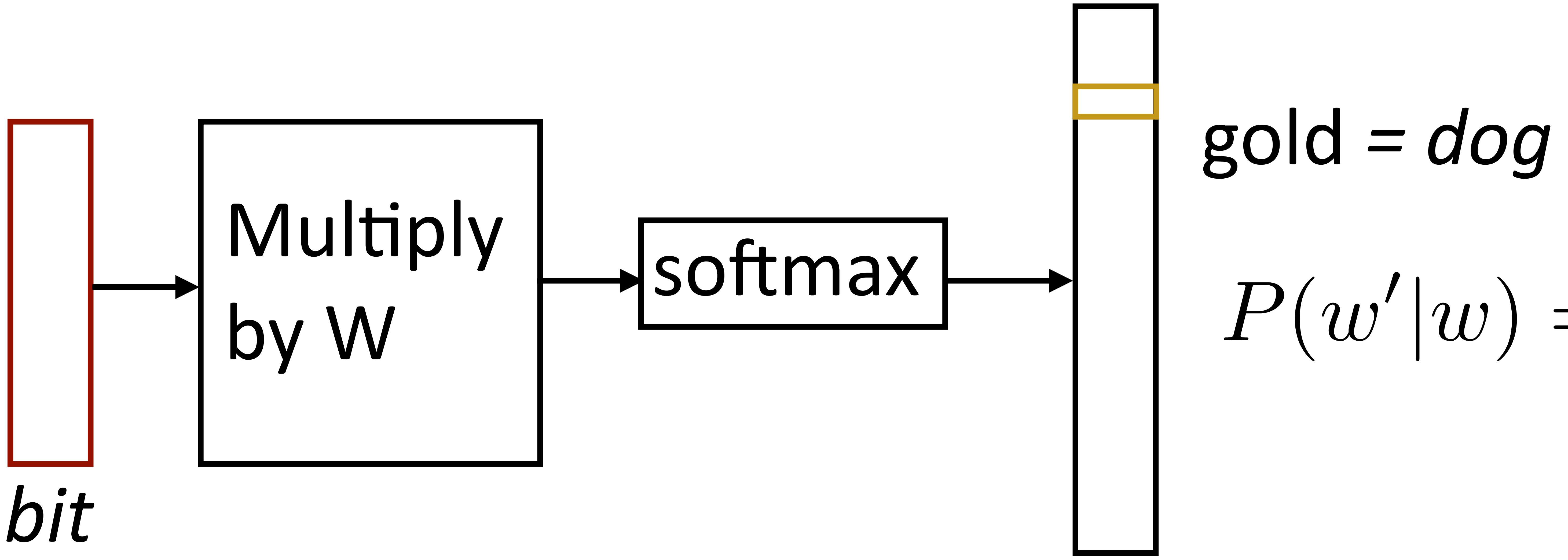

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Mikolov et al. (2013)

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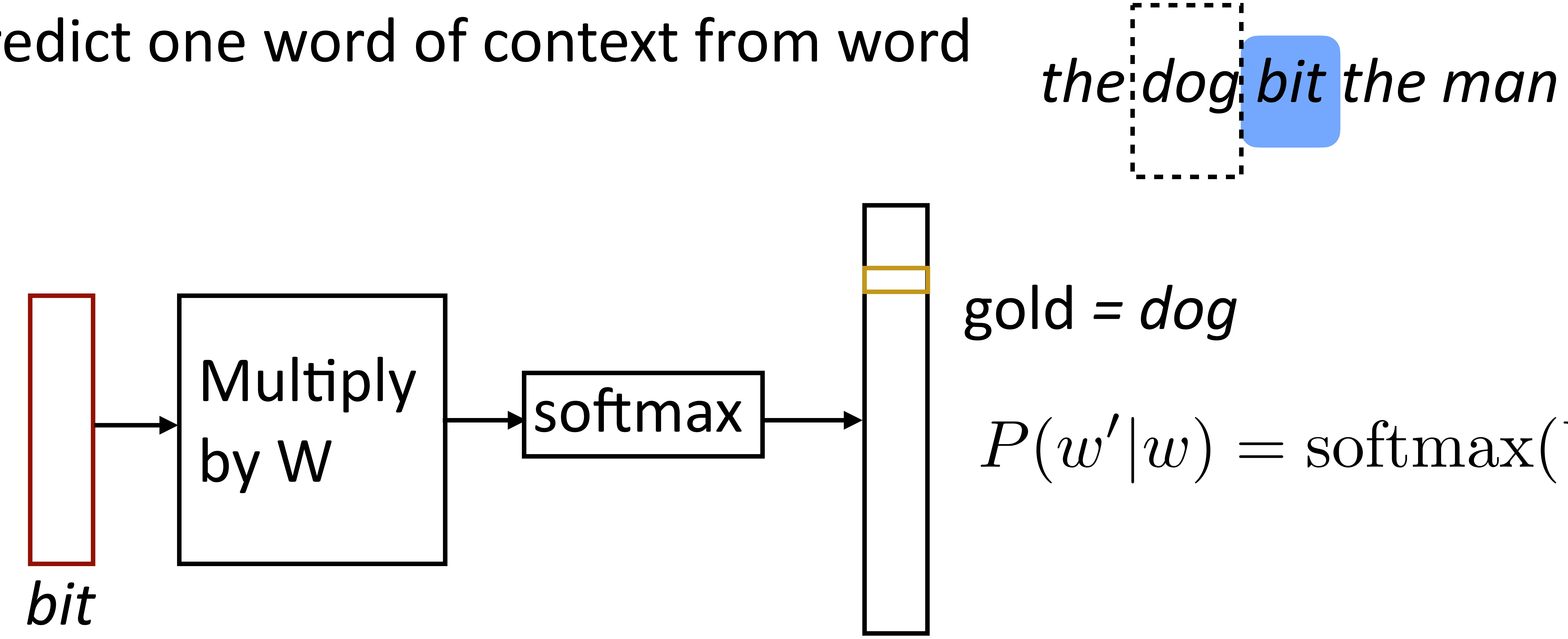

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- Another training example: *bit -> the*

Mikolov et al. (2013)

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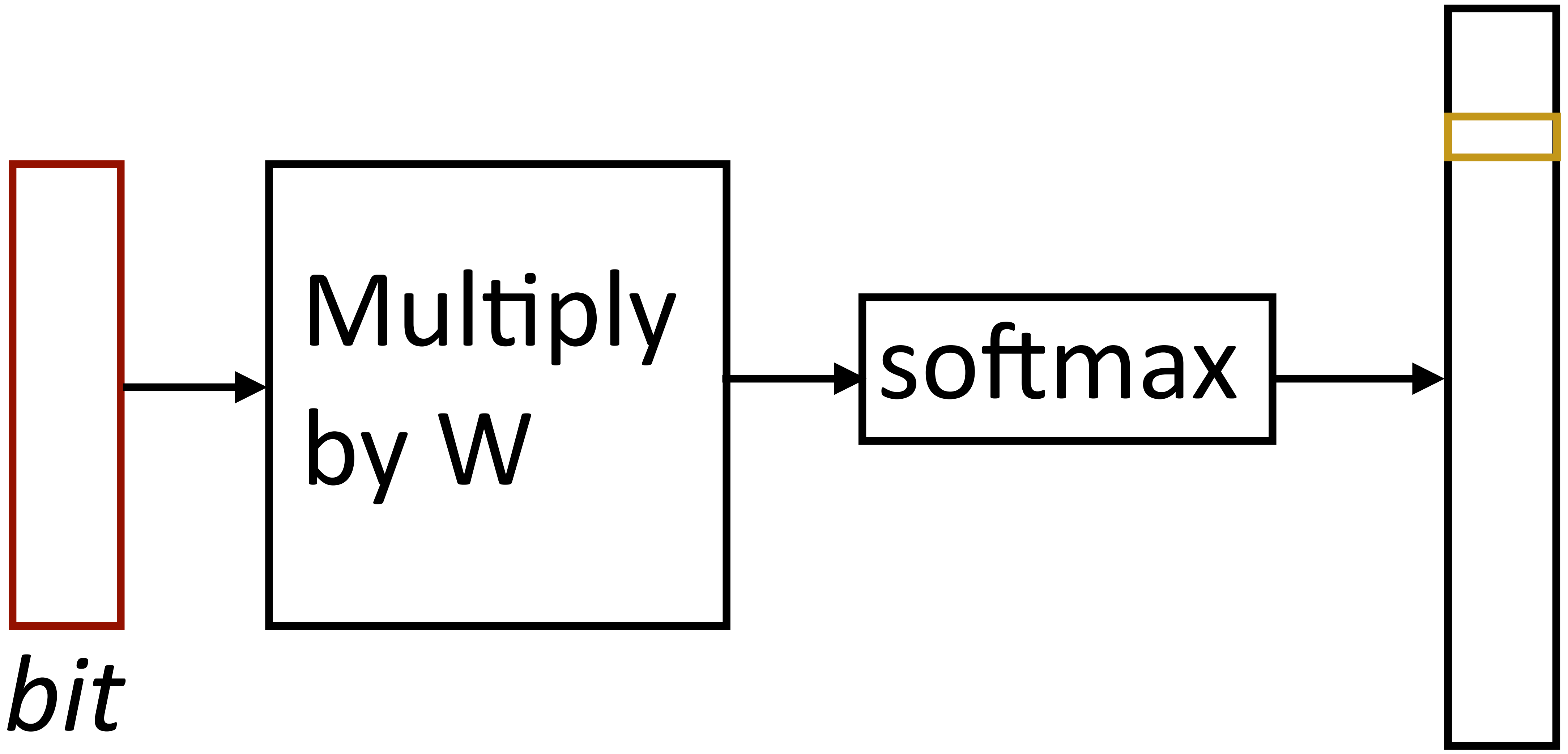

gold = *dog*

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- Another training example: *bit* -> *the*
- Parameters: *d* x |V| vectors, |V| x *d* output parameters (W) (also usable as vectors!)

Mikolov et al. (2013)

Hierarchical Softmax

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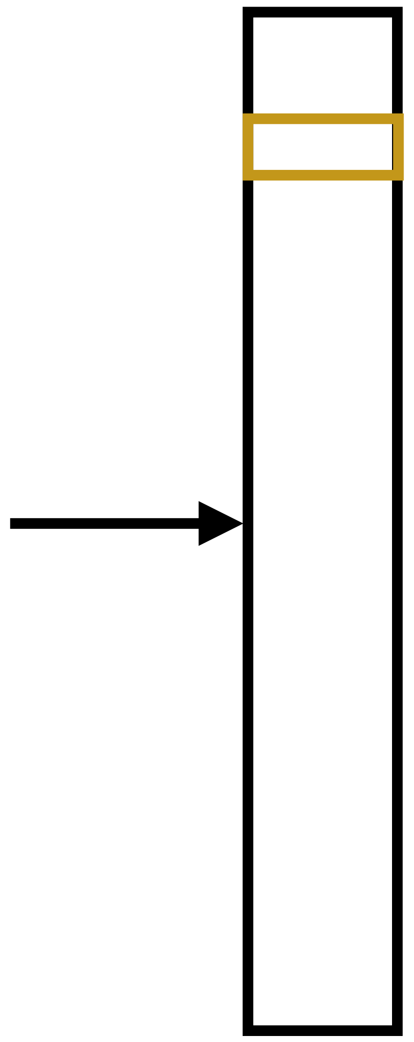

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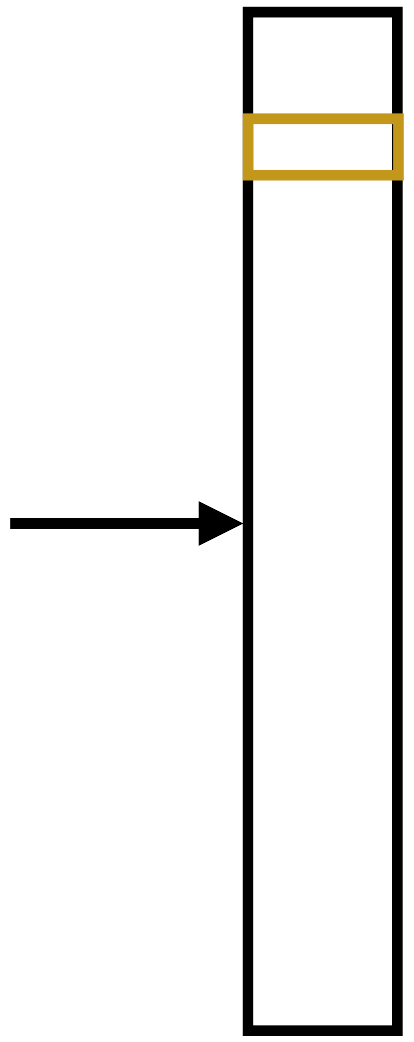

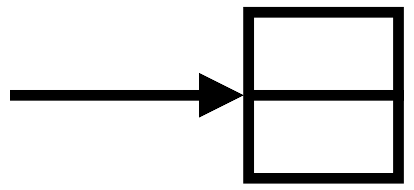

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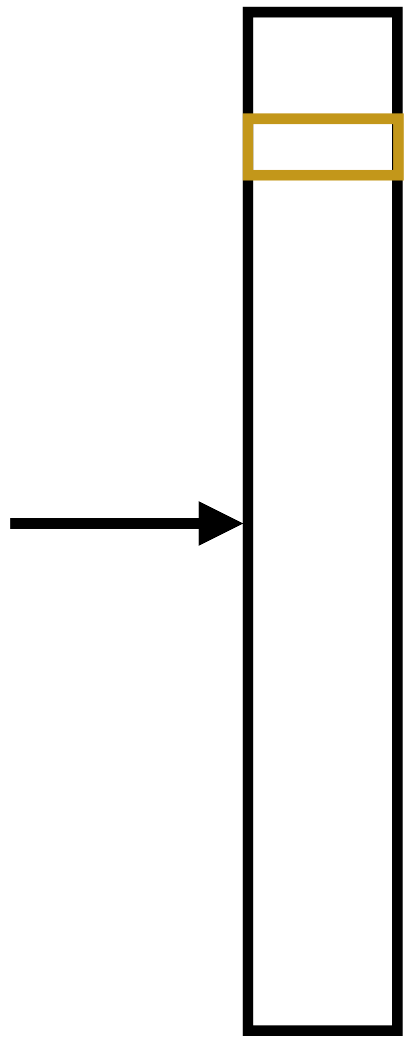

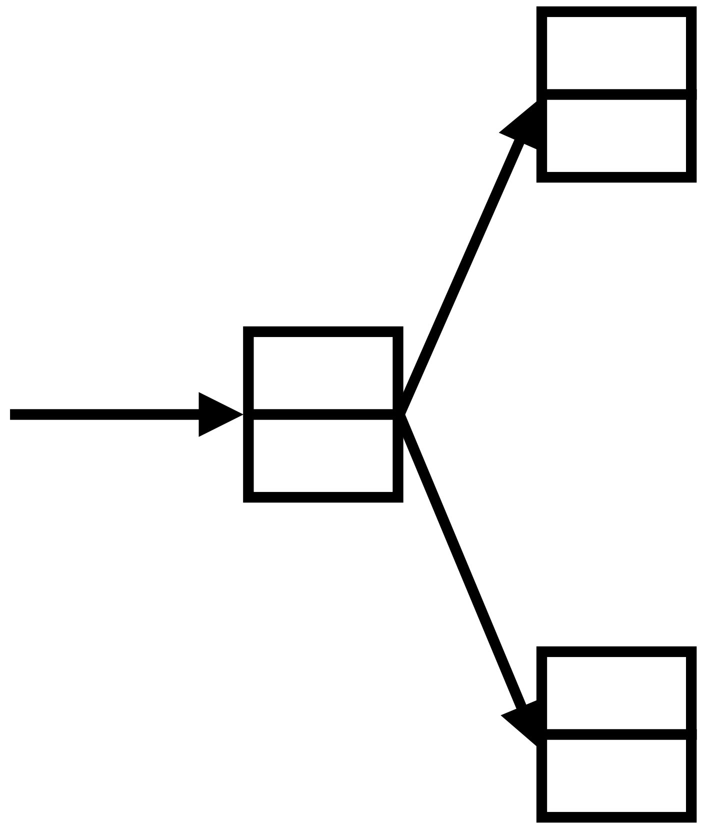

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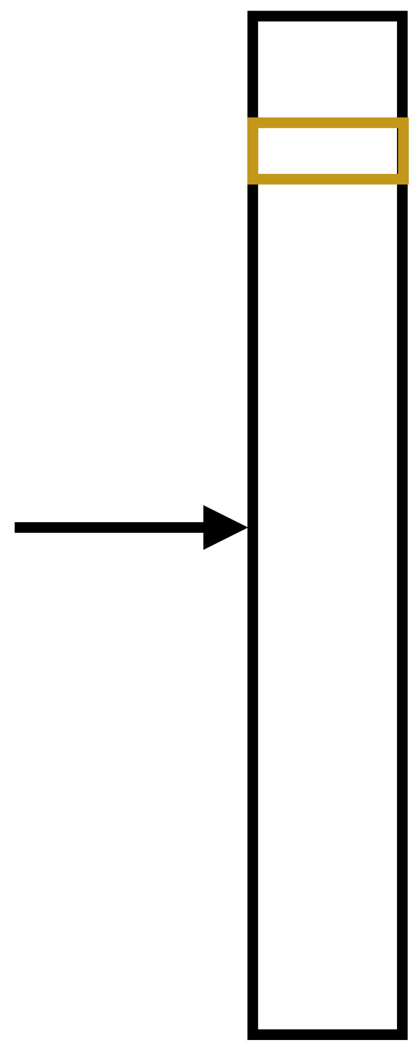

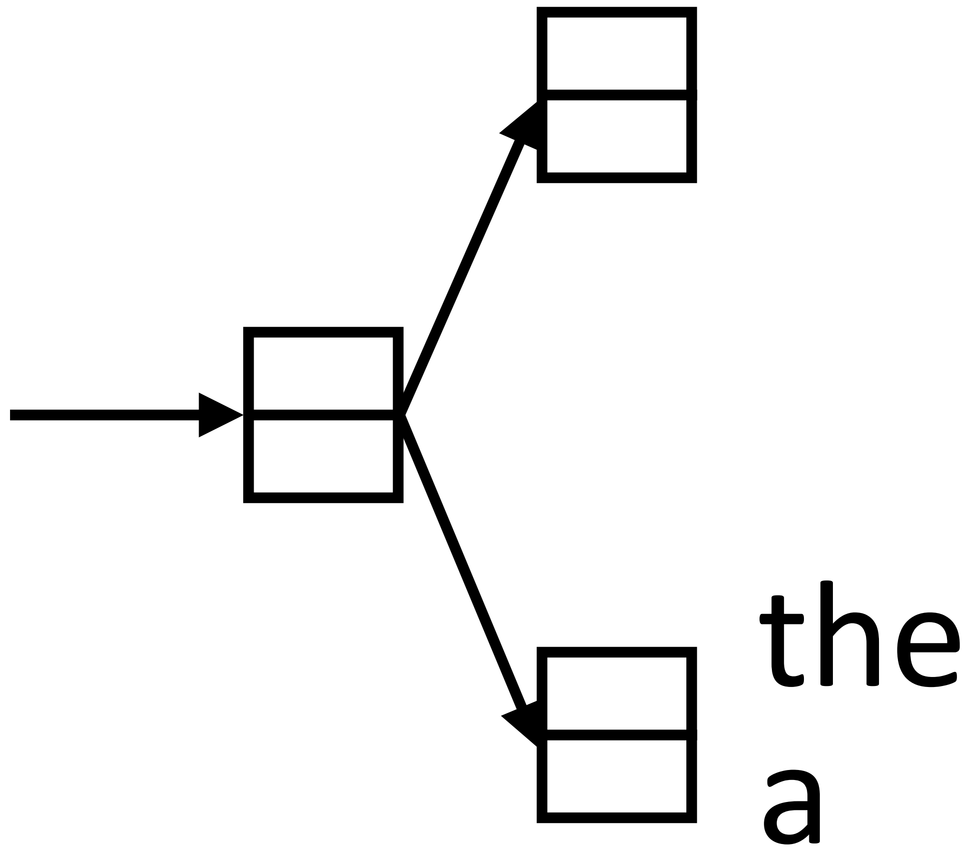

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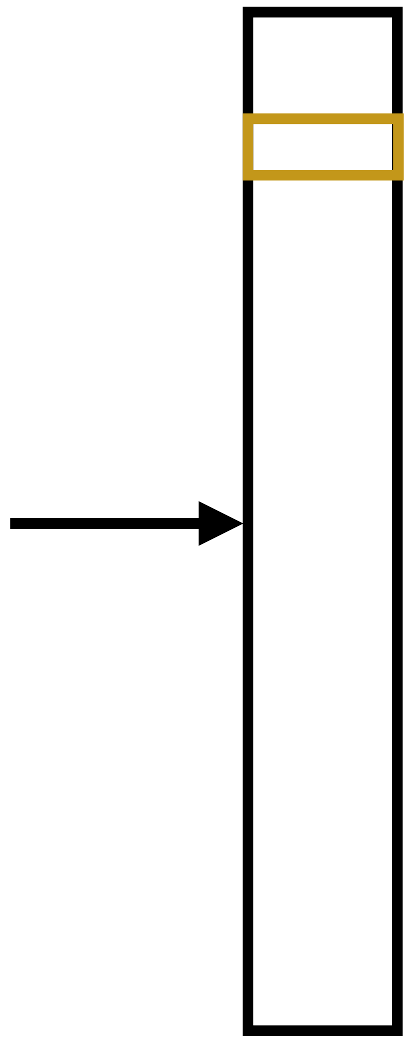

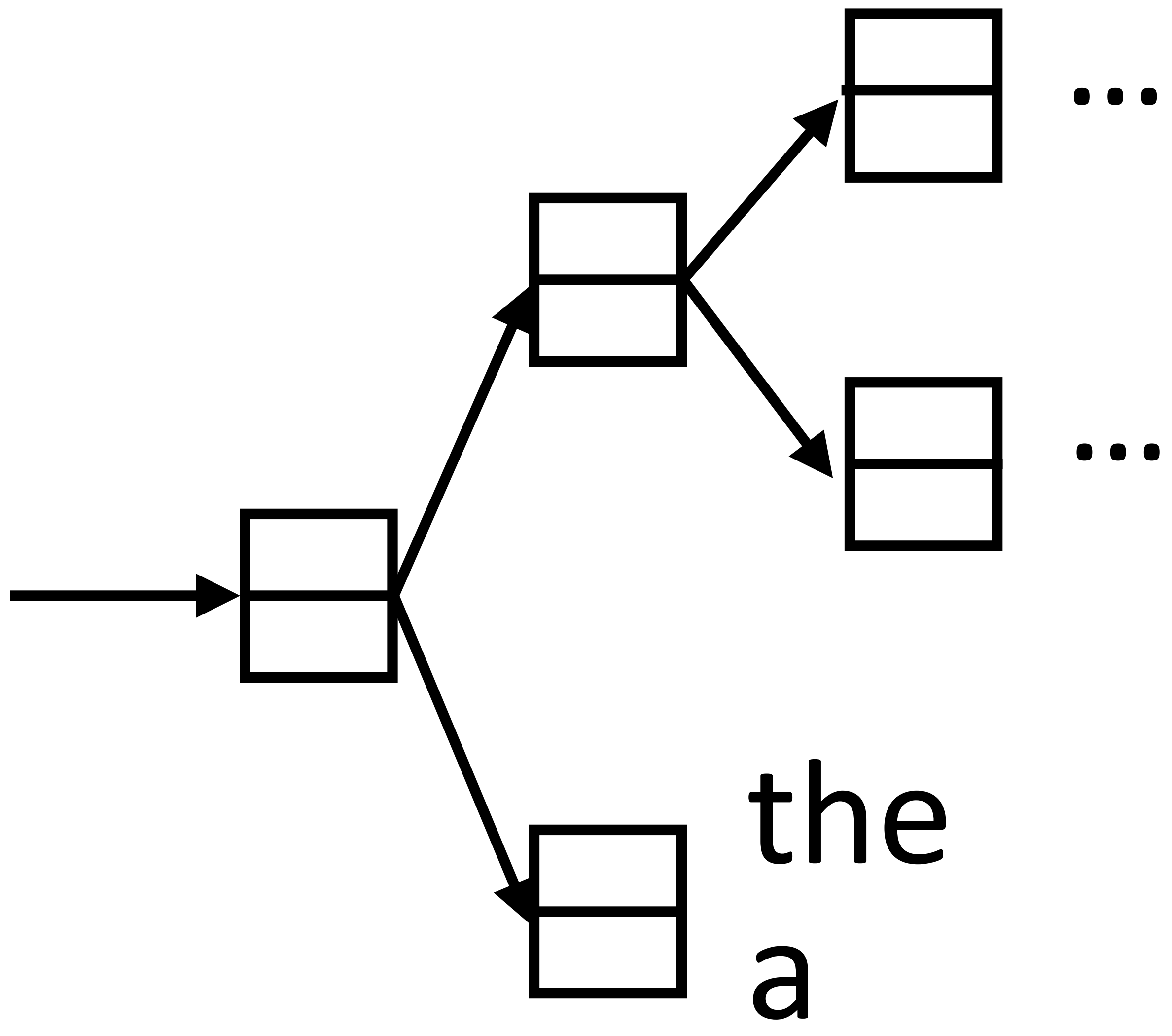

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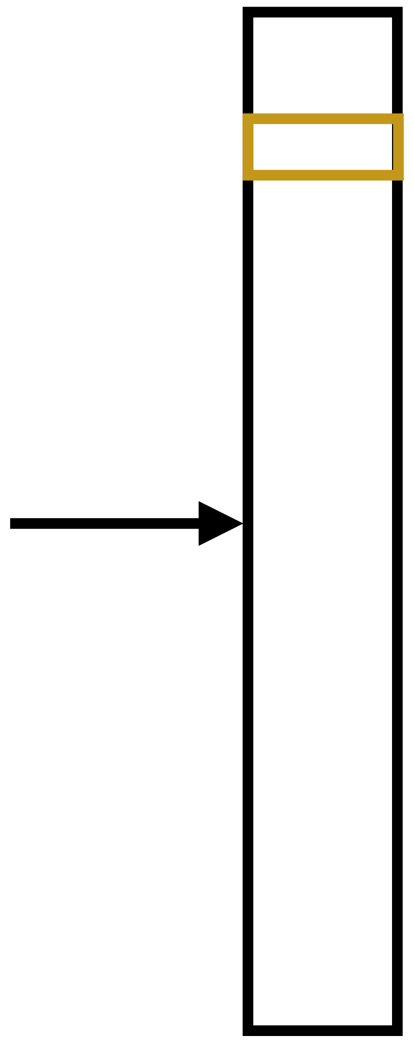

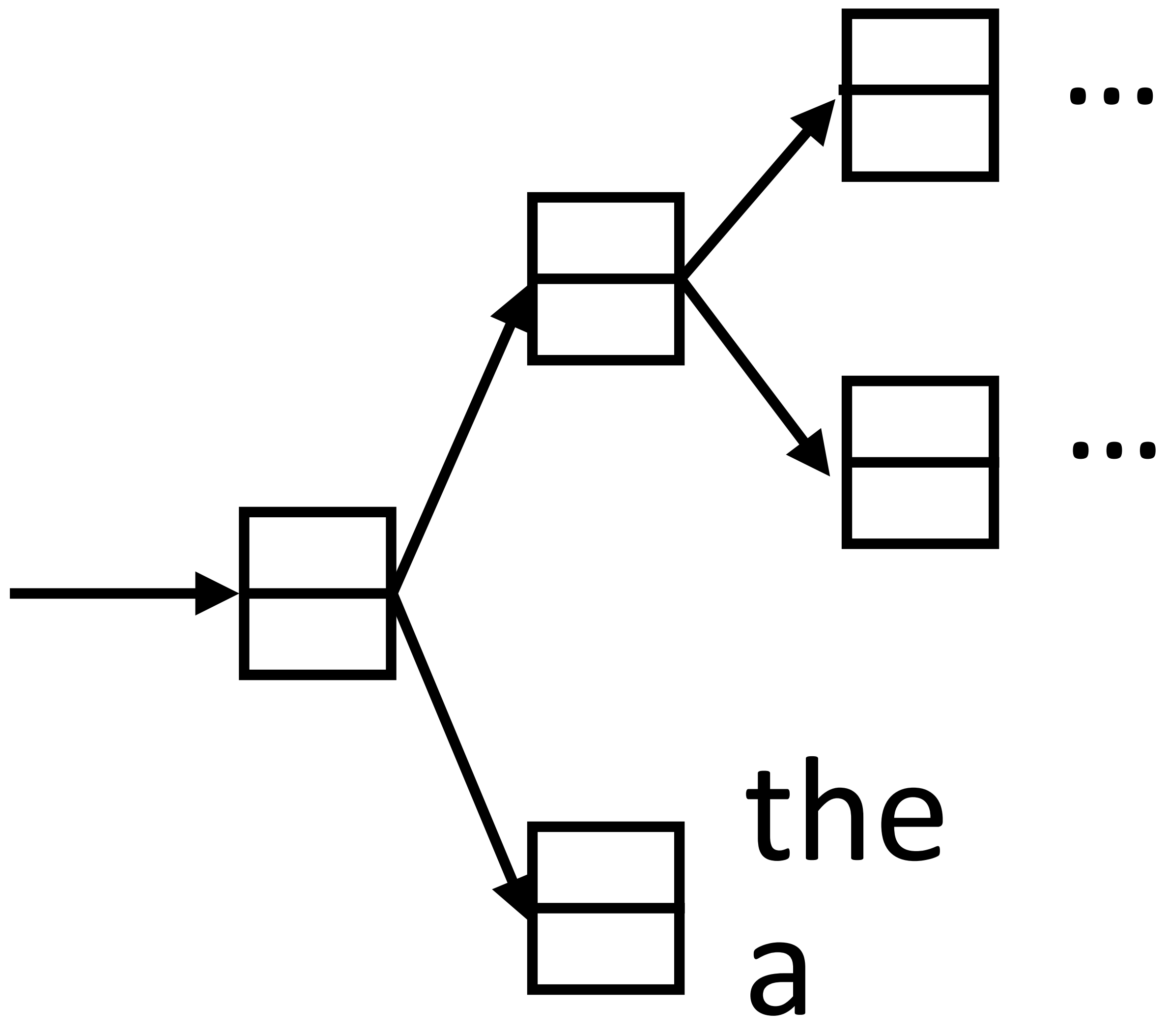

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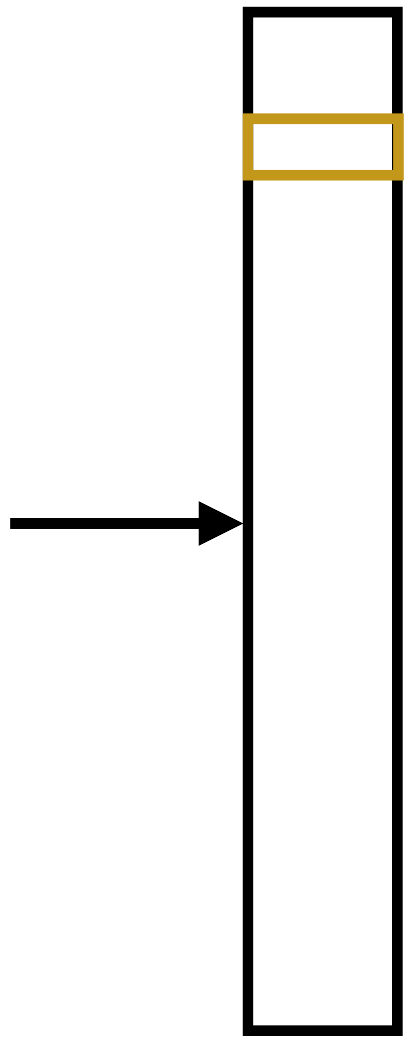

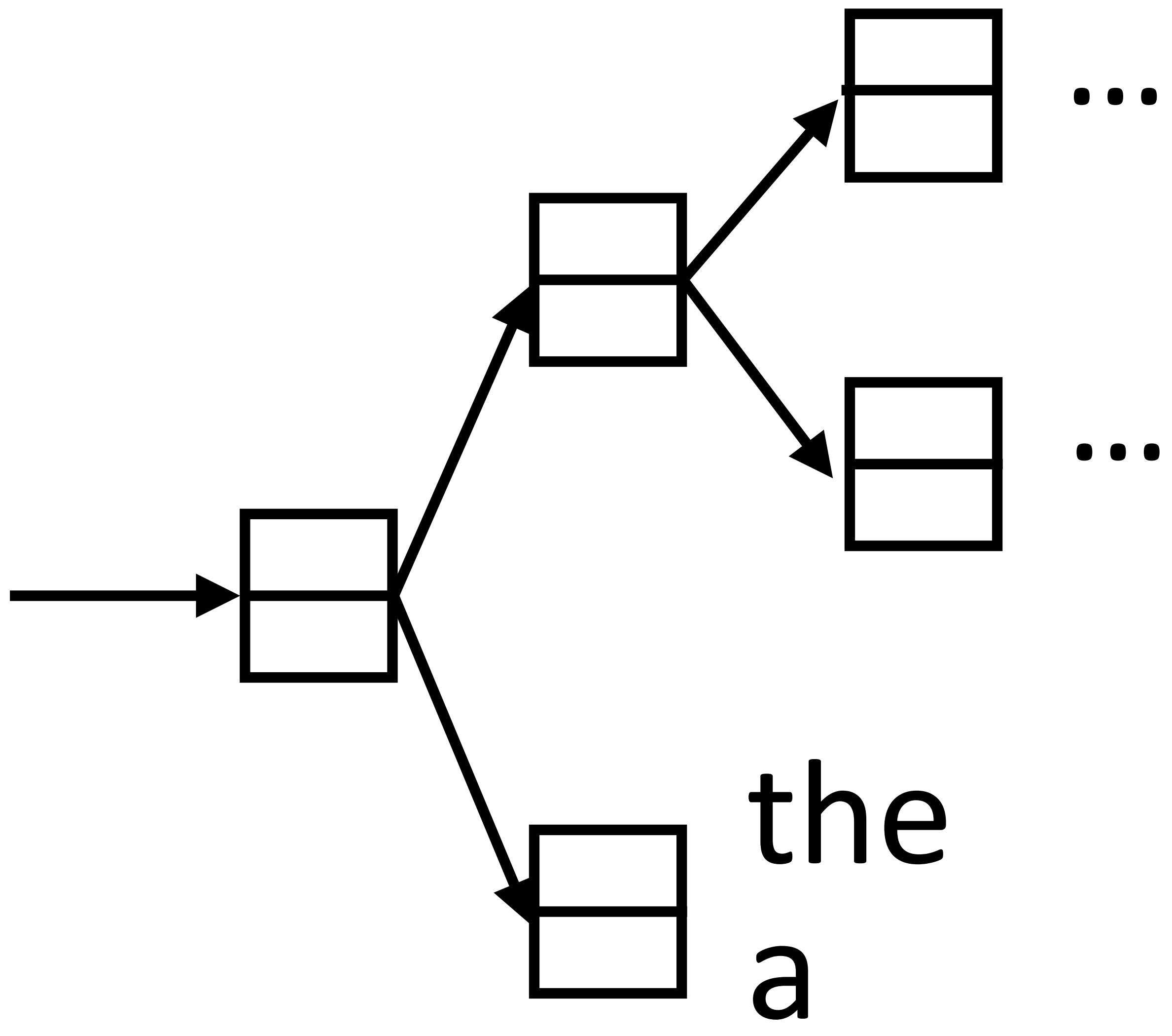

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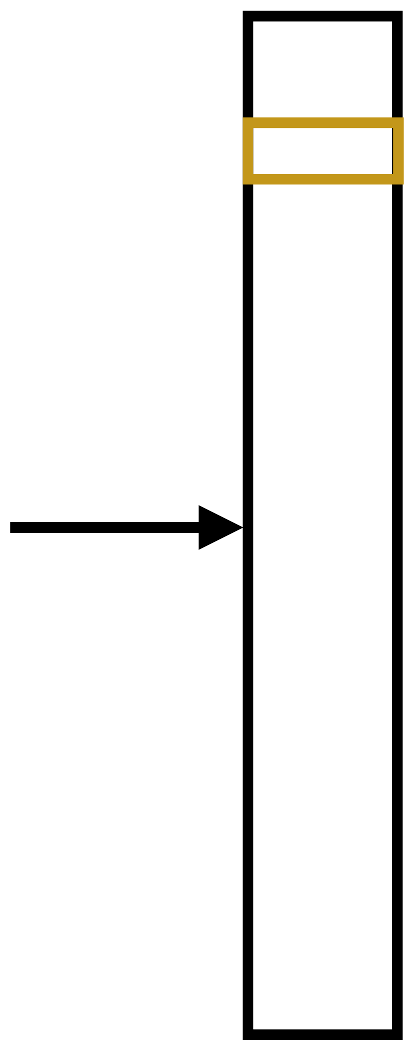

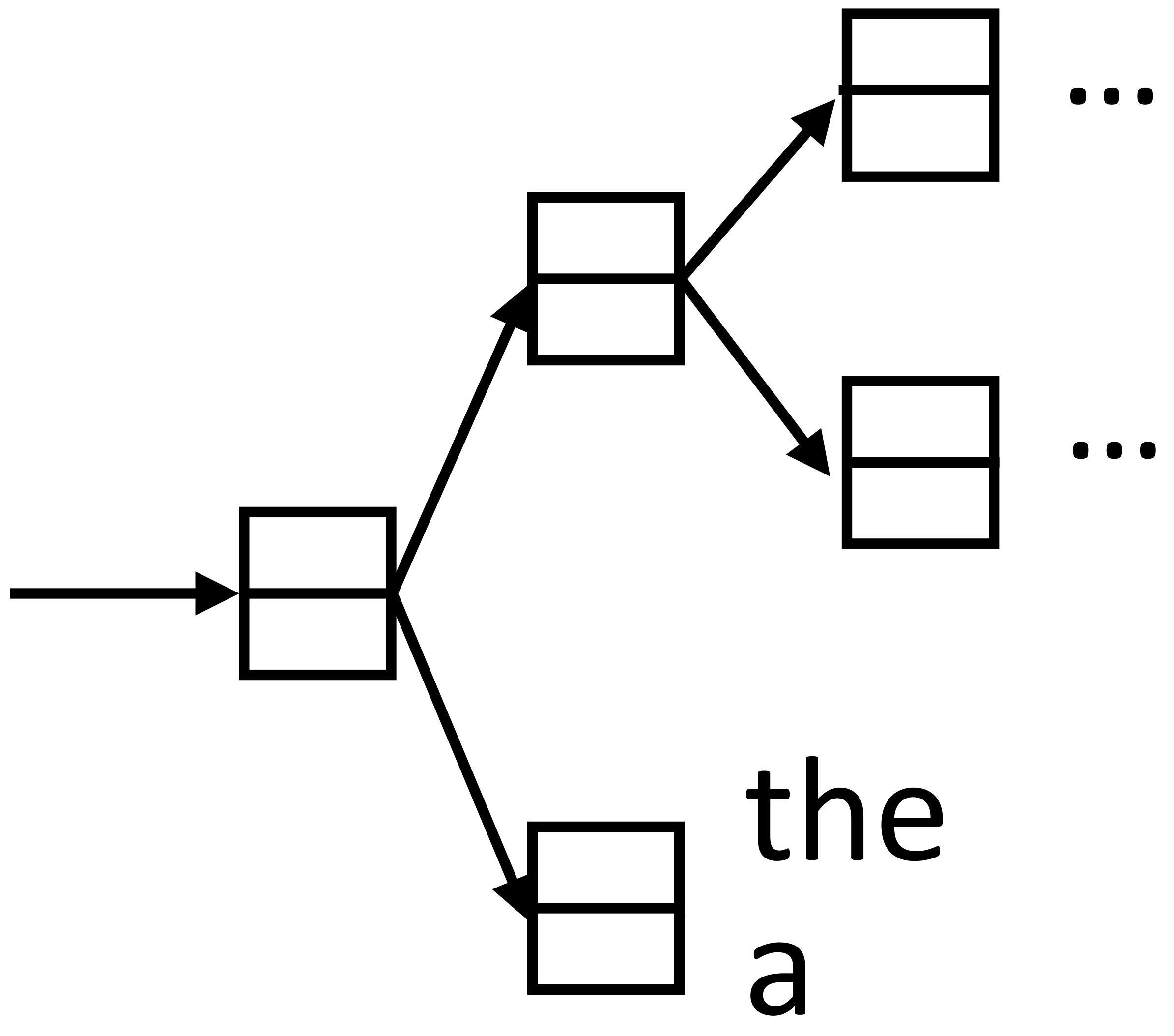

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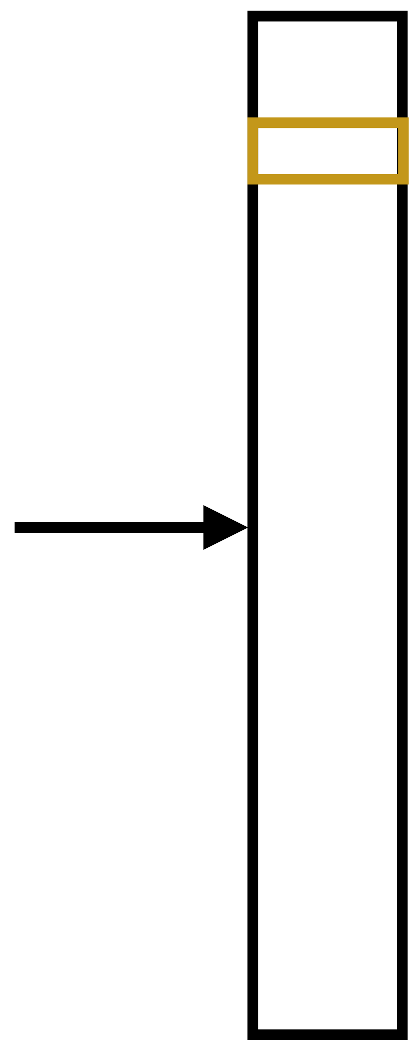

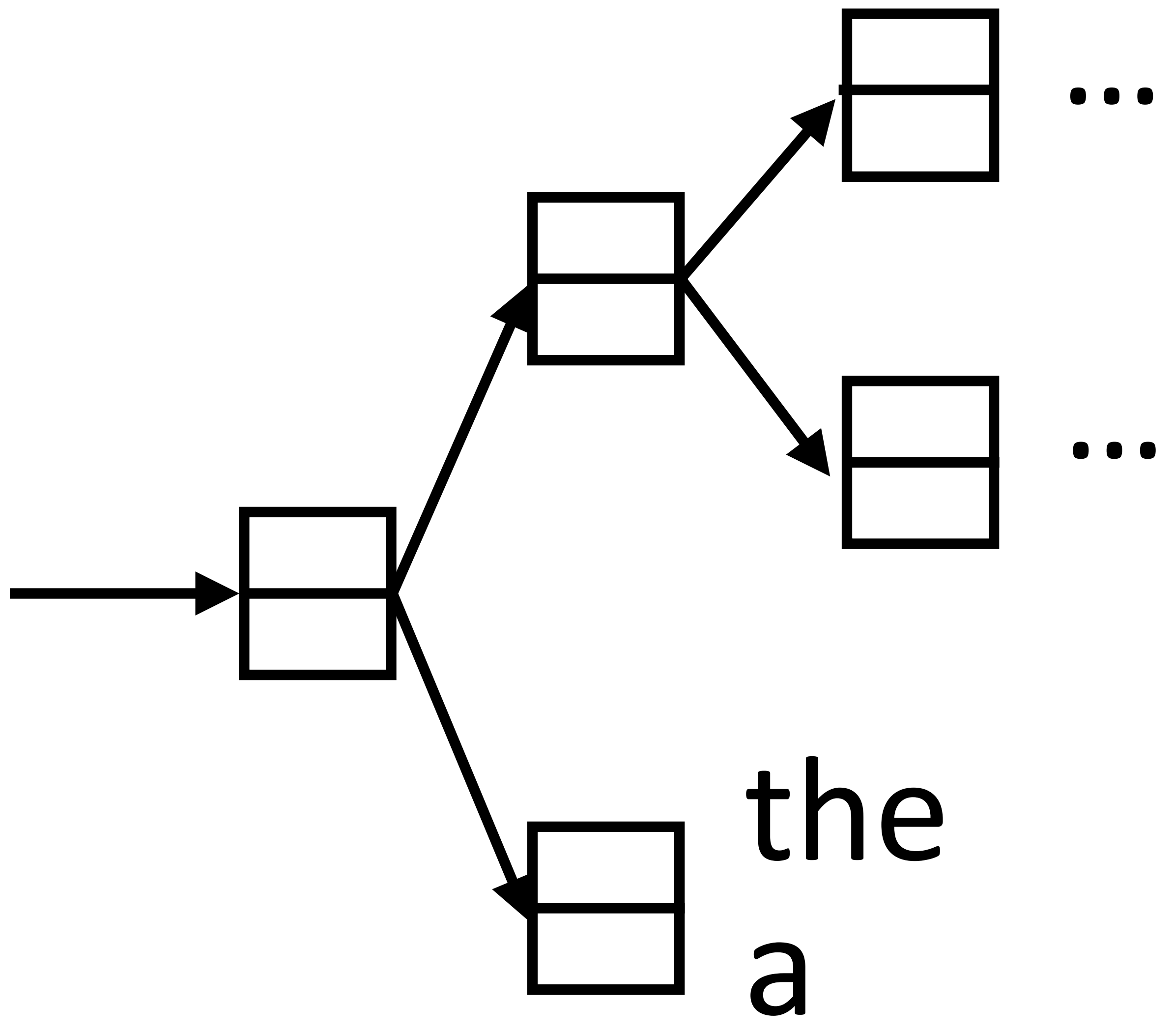

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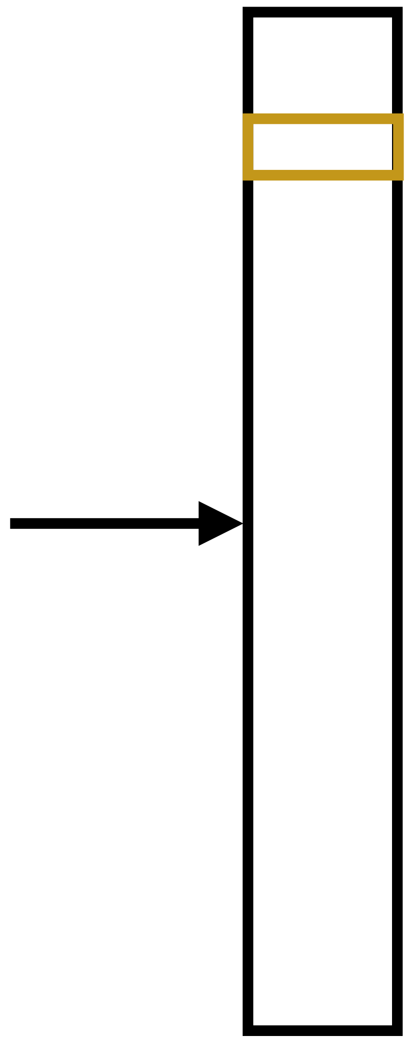

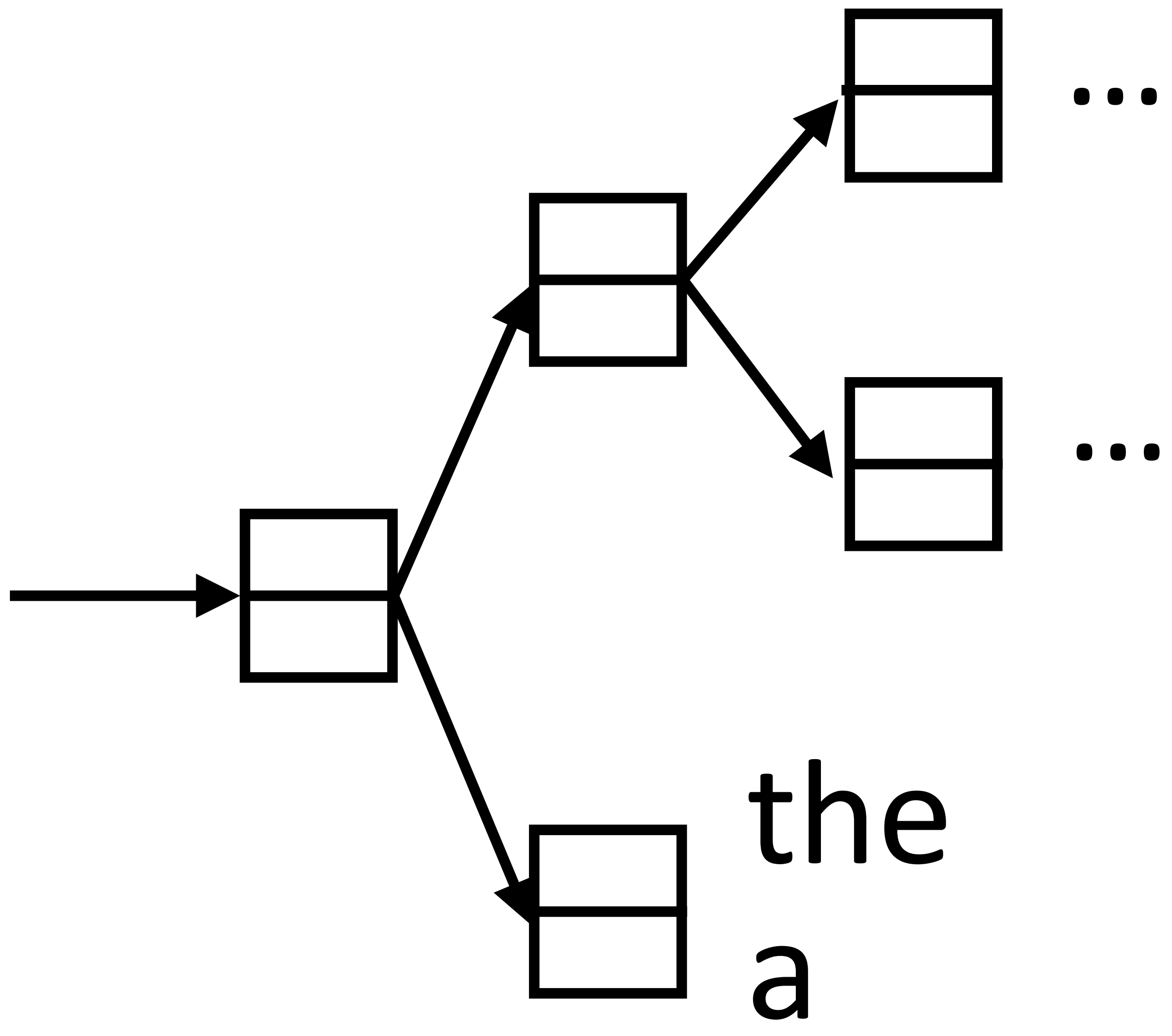

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Mikolov et al. (2013)

Skip-Gram with Negative Sampling

Mikolov et al. (2013)

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- Take (word, context) pairs and classify them as “real” or not. Create random negative examples by sampling from unigram distribution

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words in similar contexts select for similar *c* vectors

Mikolov et al. (2013)

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sampled

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Mikolov et al. (2013)

Connections with Matrix Factorization

- Skip-gram model looks at word-word co-occurrences and produces two types of vectors

Levy et al. (2014)

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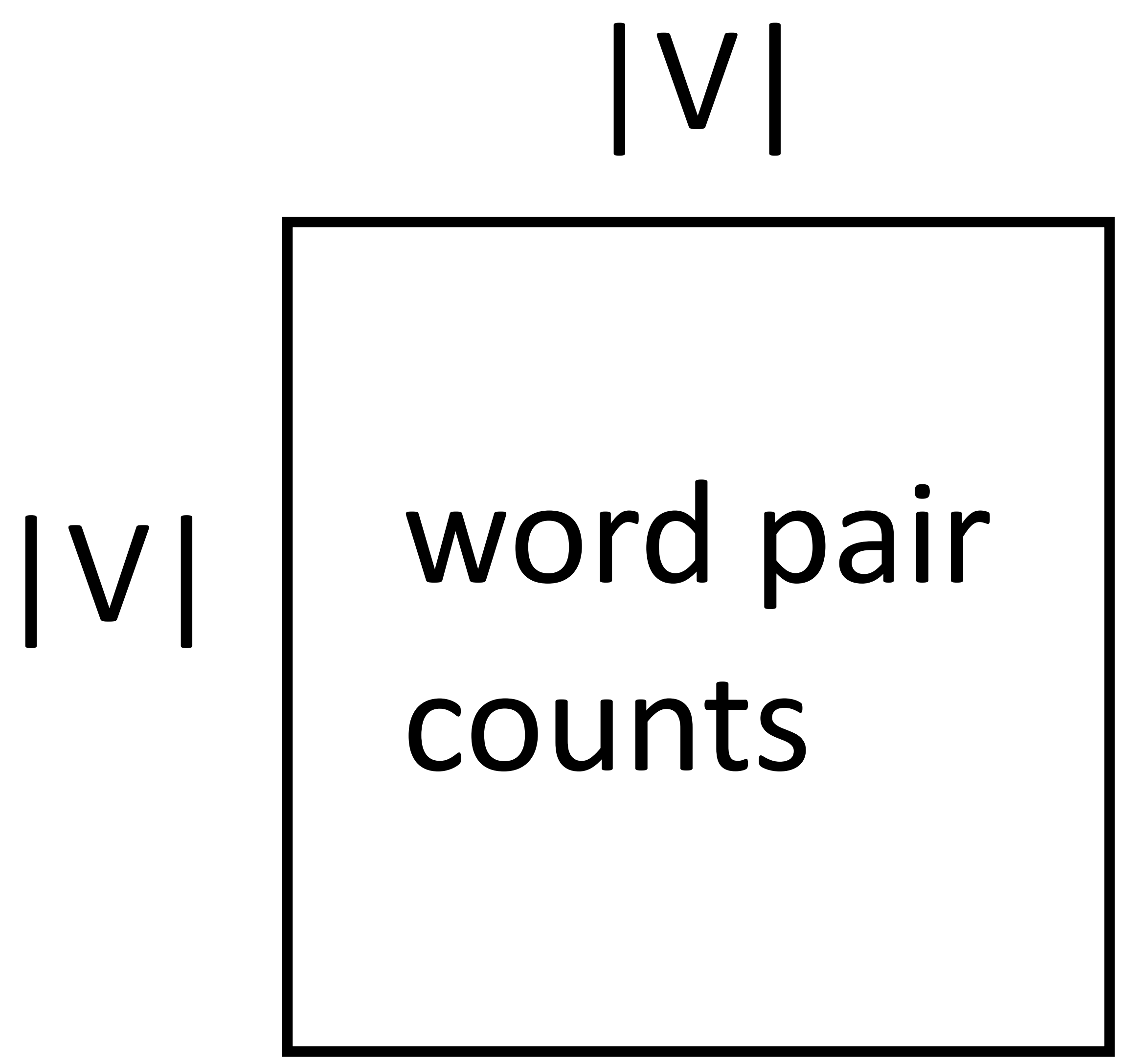

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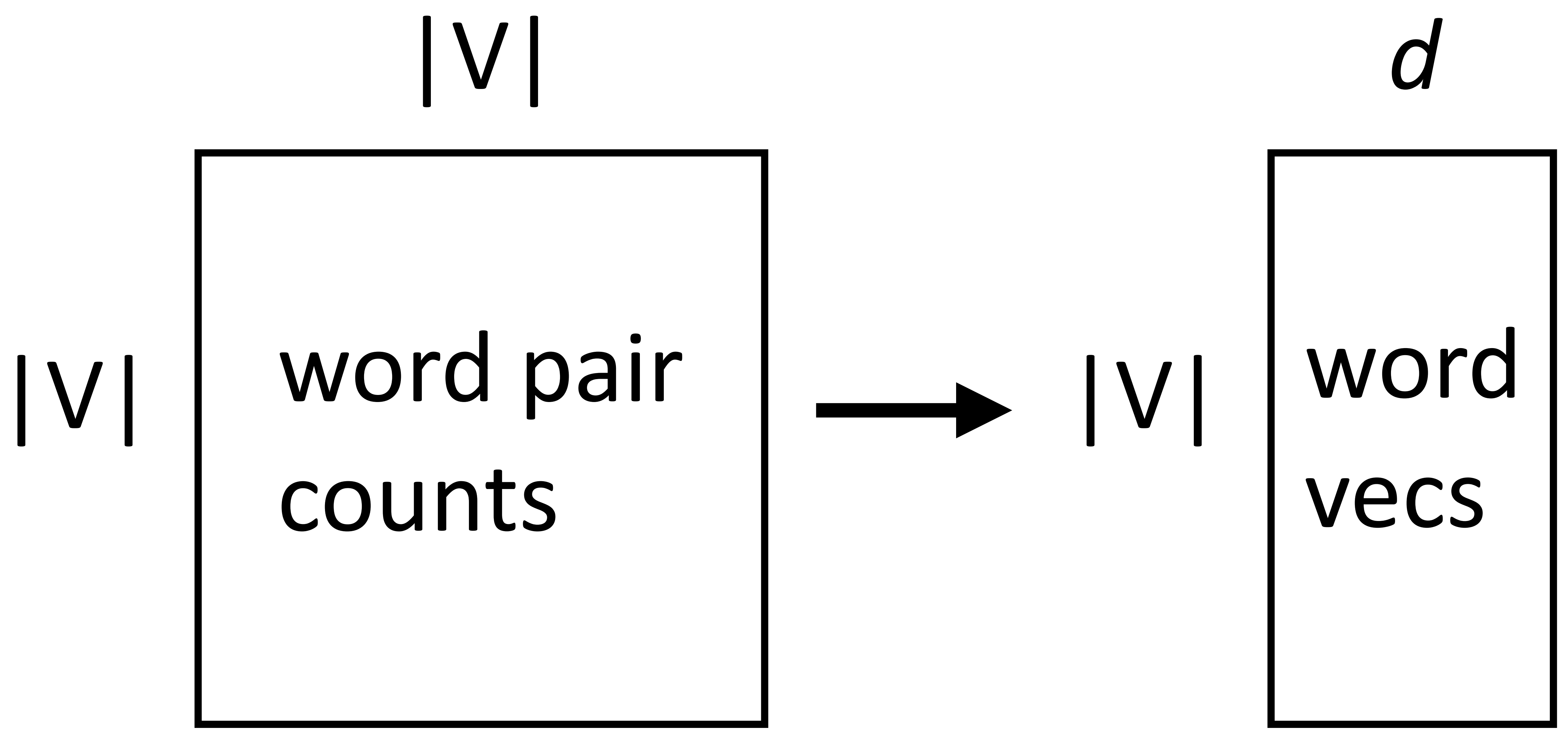

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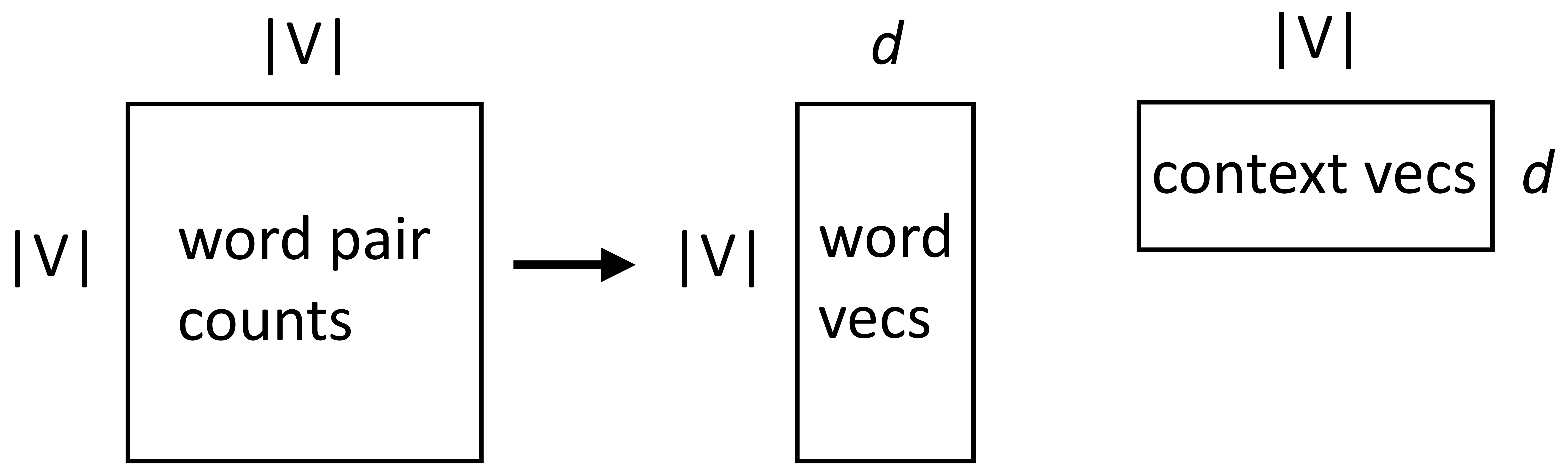

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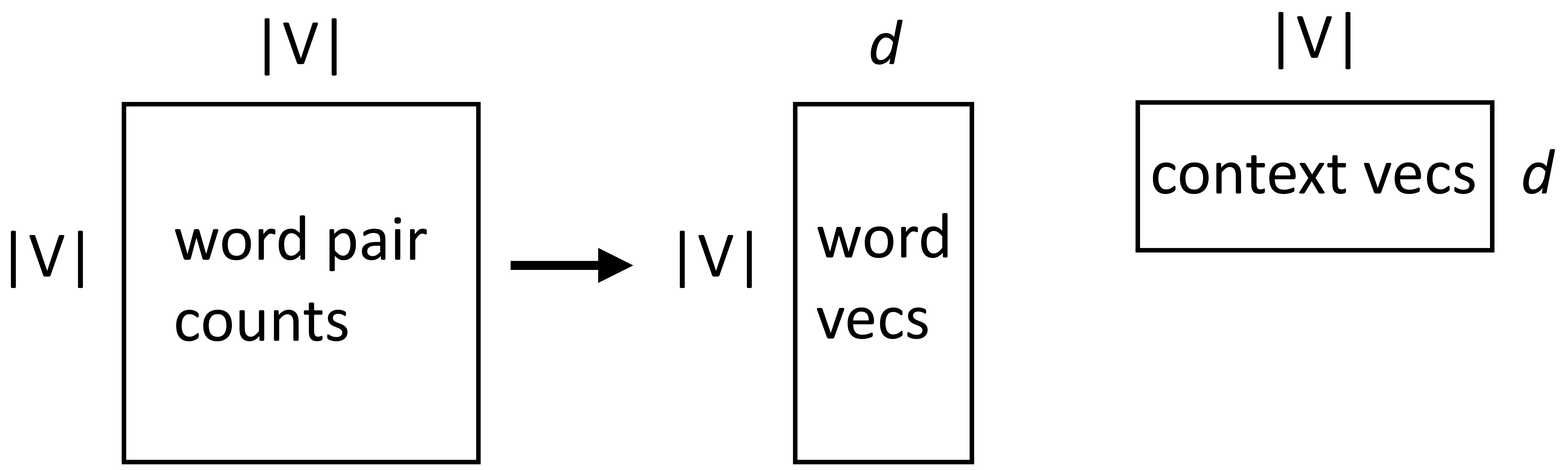
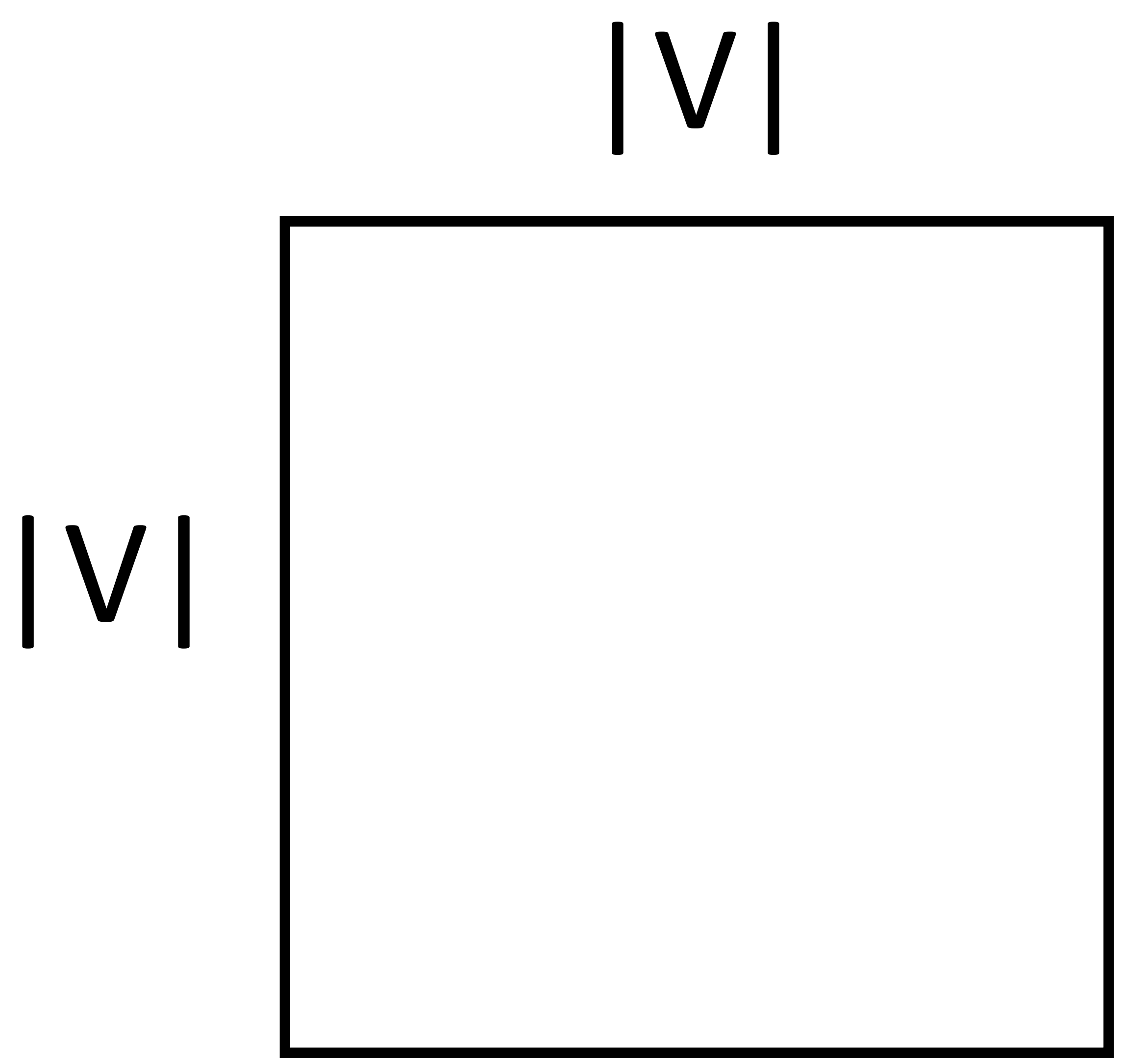


- Looks almost like a matrix factorization…can we interpret it this way?

Levy et al. (2014)

Skip-Gram as Matrix Factorization



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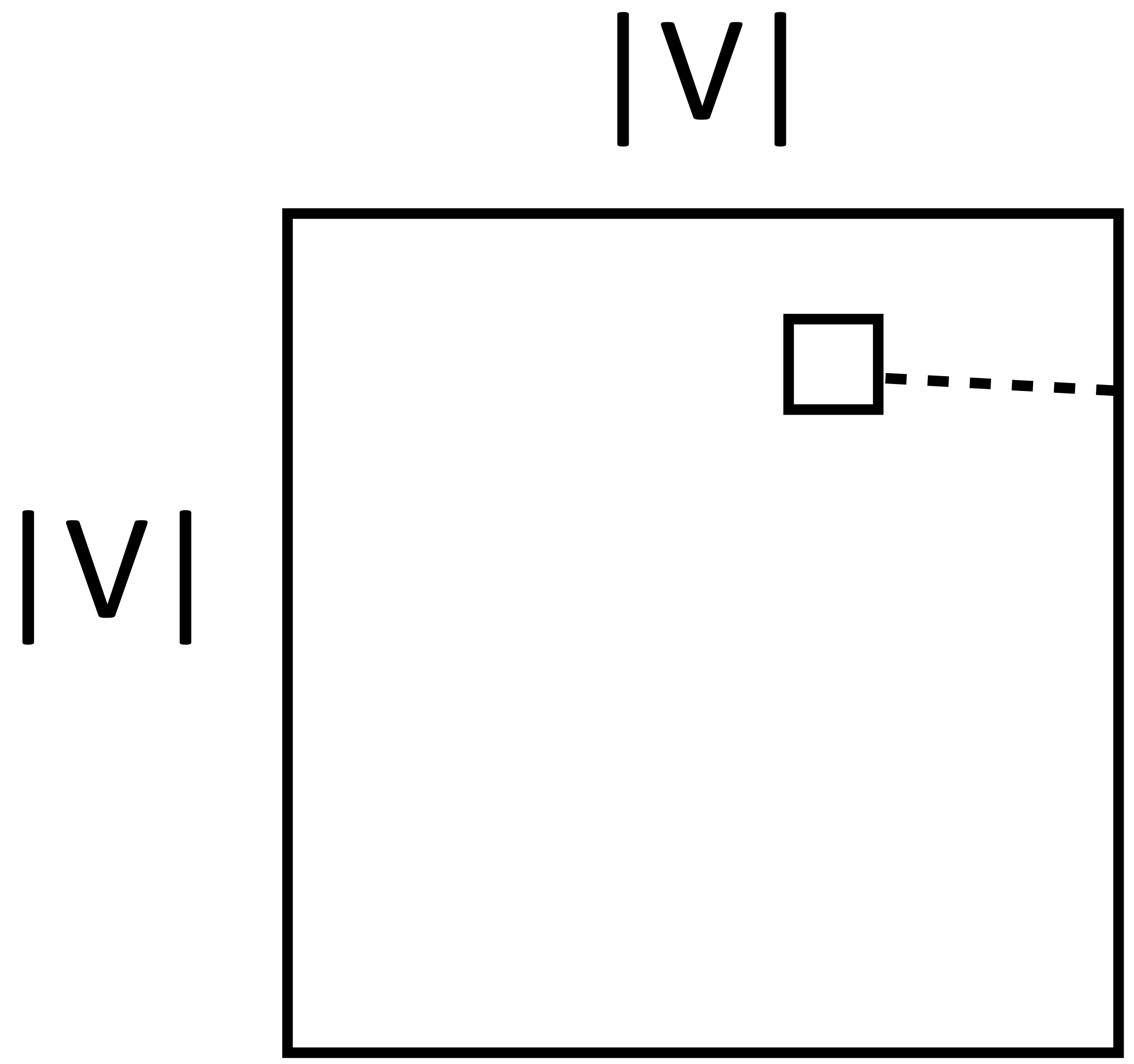
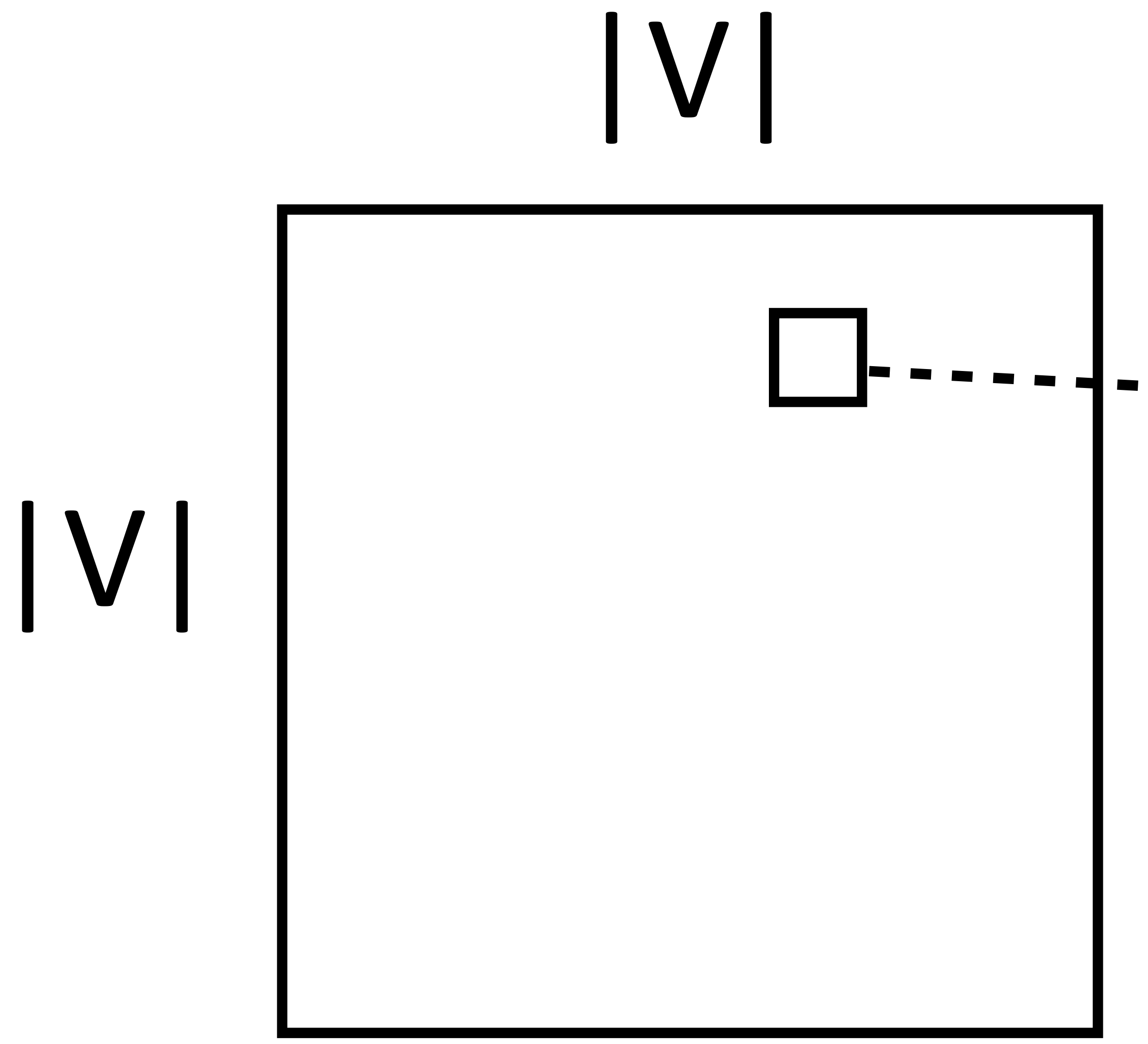


num negative samples

$$M_{ij} = \mathrm{PMI}(w_i, c_j) - \log k$$

Levy et al. (2014)

Skip-Gram as Matrix Factorization



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Levy et al. (2014)

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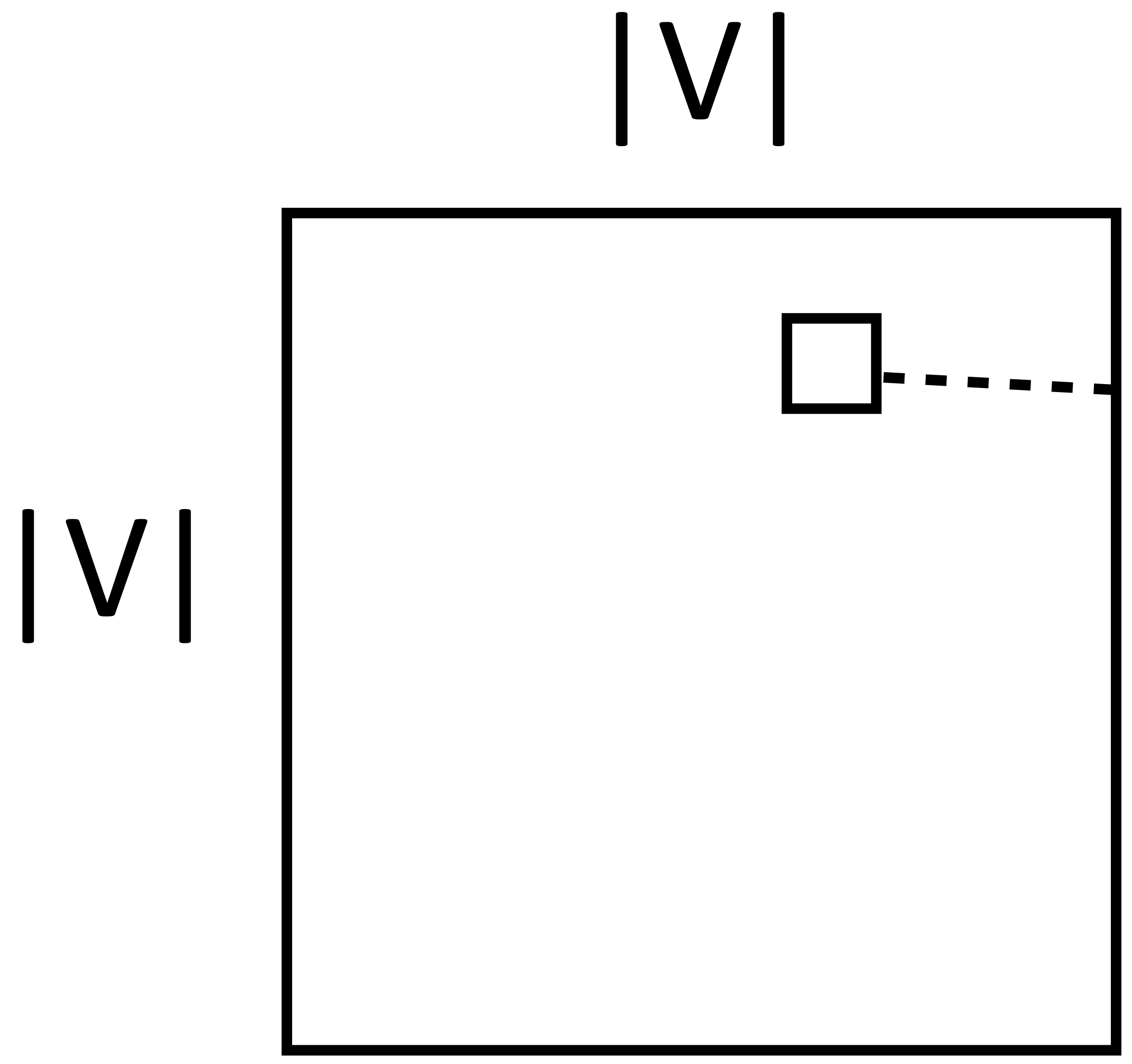

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Skip-gram objective *exactly* corresponds to factoring this matrix:

Levy et al. (2014)

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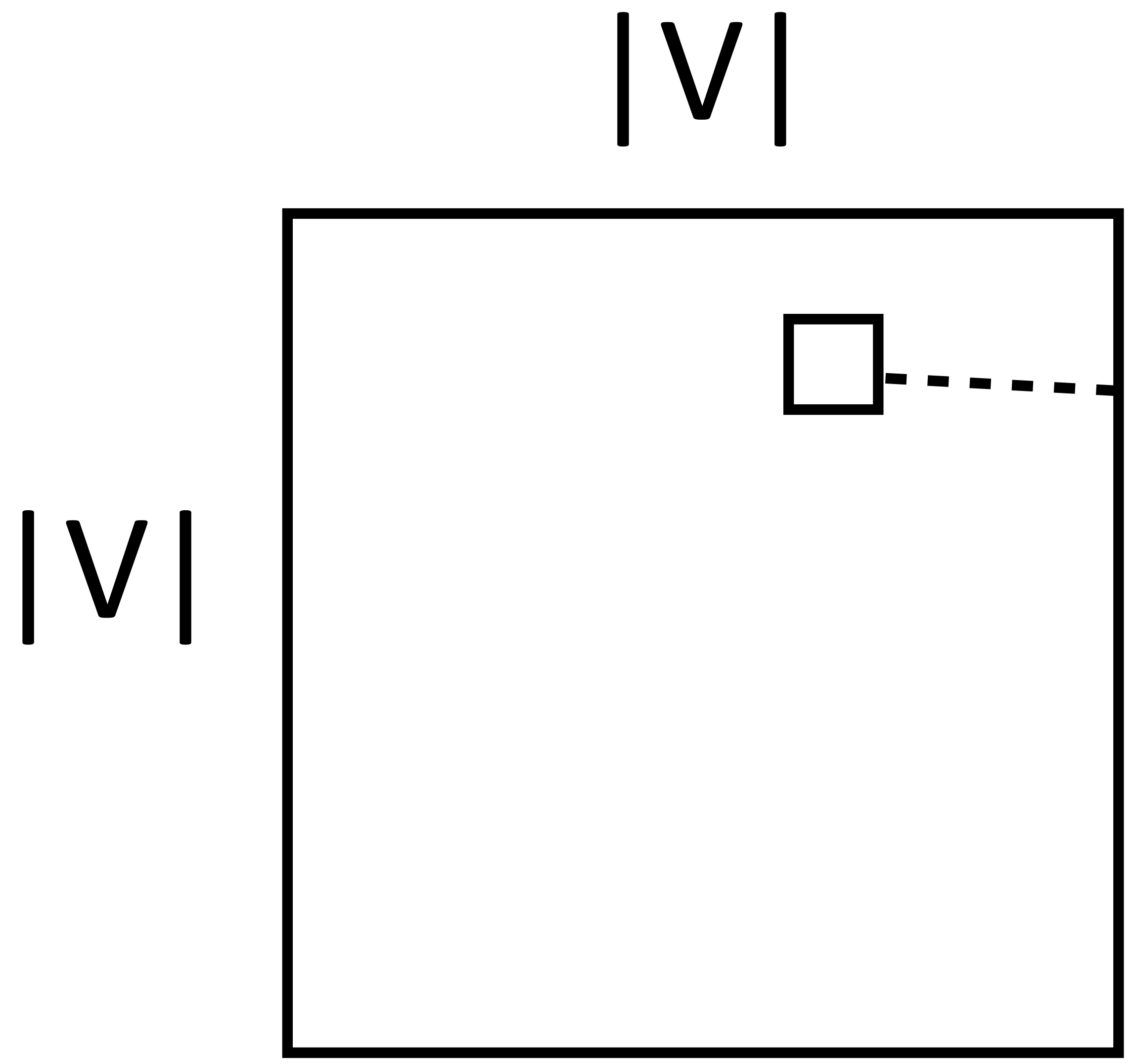

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- *If* we sample negative examples from the uniform distribution over words

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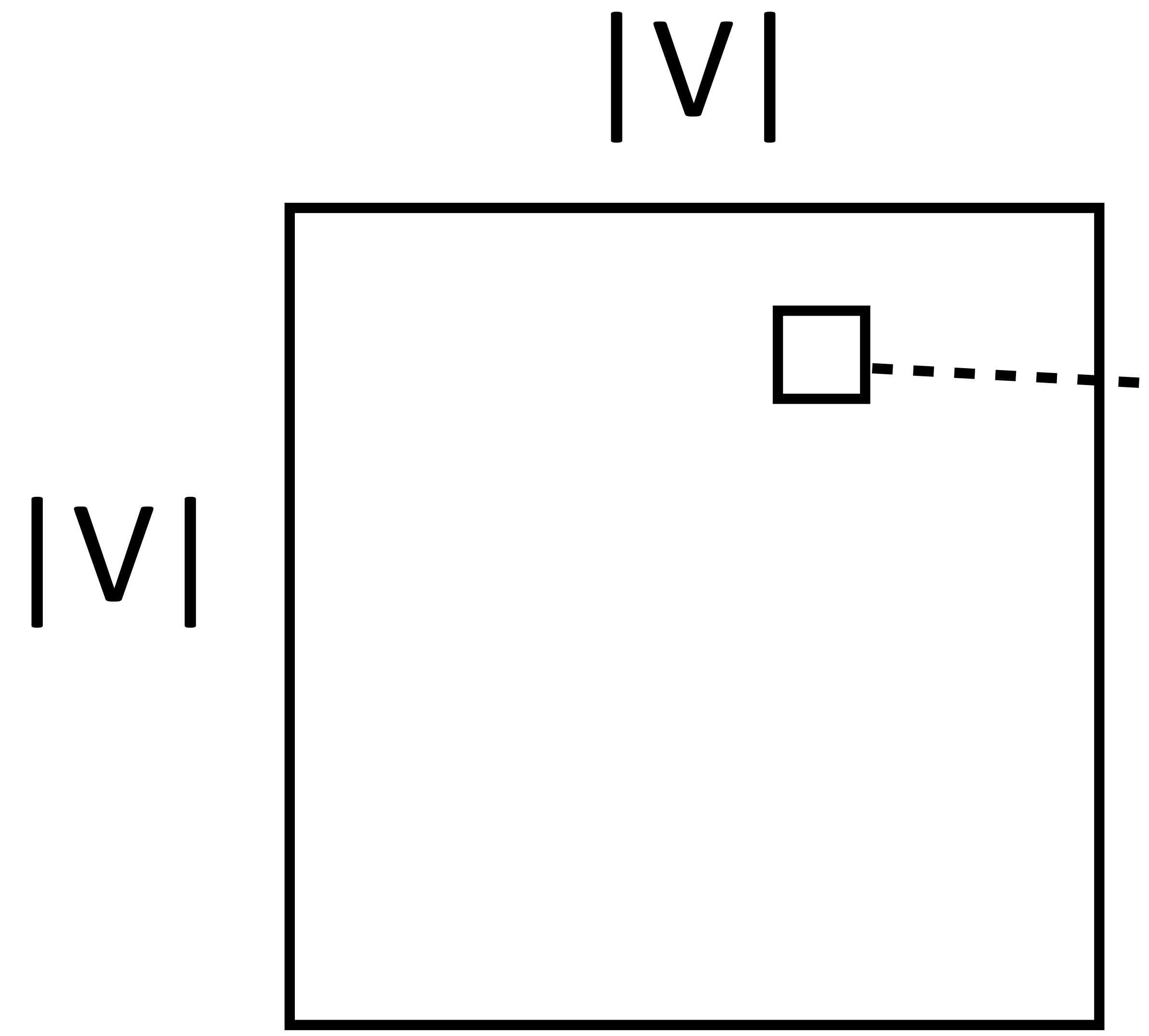

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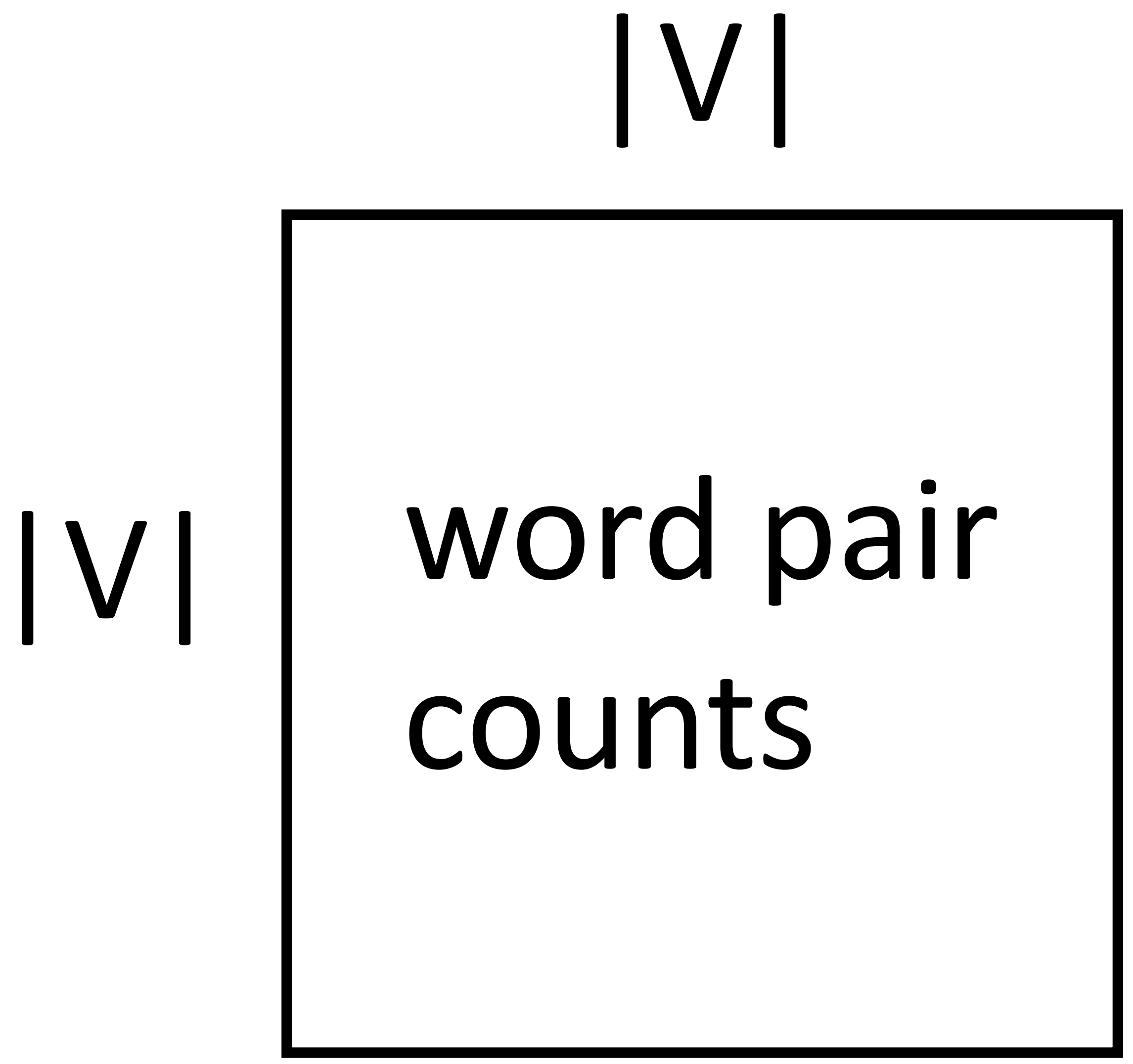
Skip-gram objective *exactly* corresponds to factoring this matrix:

- *If* we sample negative examples from the uniform distribution over words
- …and it's a *weighted* factorization problem (weighted by word freq)

Levy et al. (2014)

GloVe (**Glo**bal **Ve**ctors)

- Also operates on counts matrix, weighted regression on the log co-occurrence matrix



Pennington et al. (2014)

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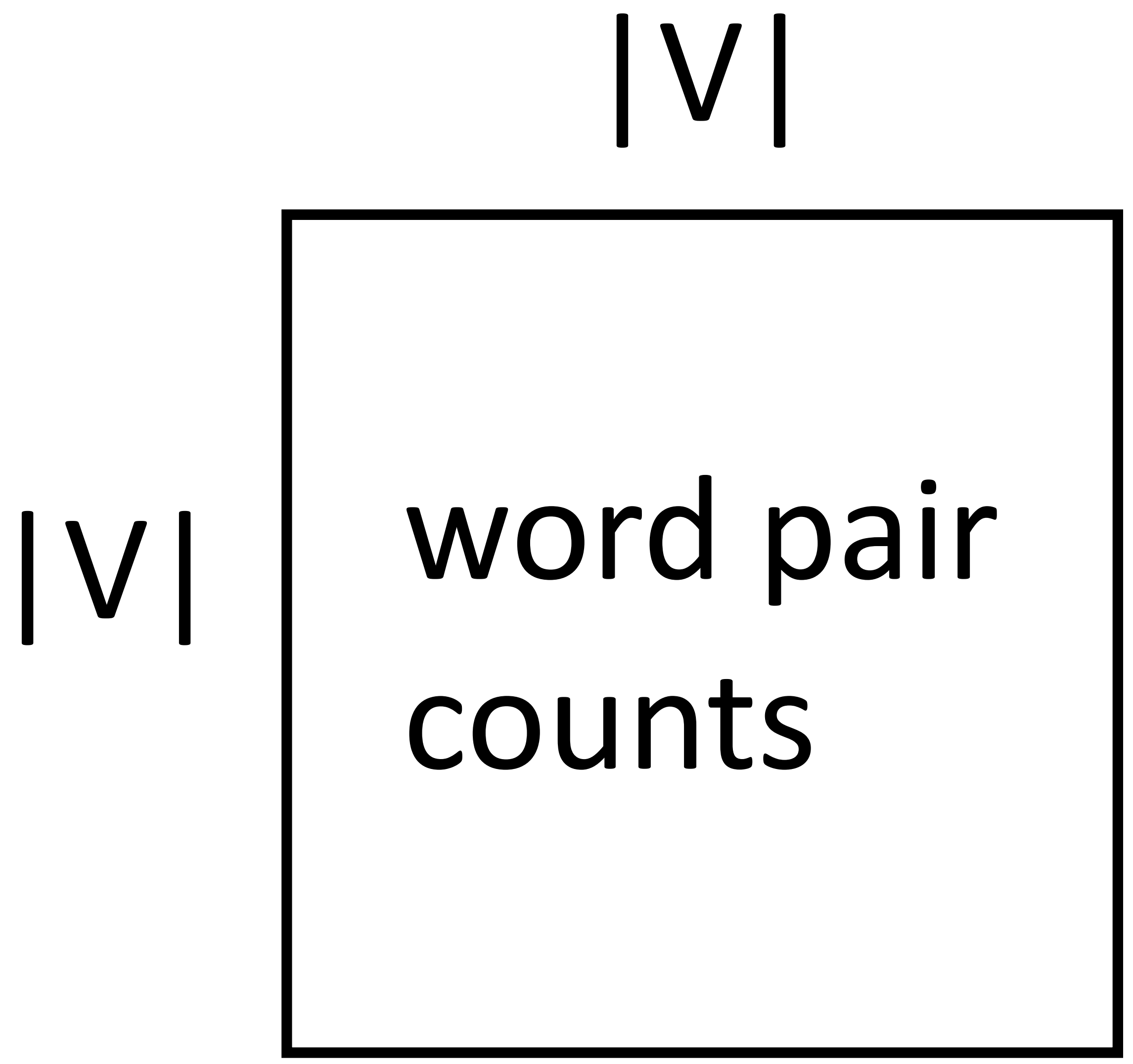

- Loss = $$\sum_{i,j} f(\mathrm{count}(w_i, c_j)) \left(w_i^\top c_j + a_i + b_j - \log \mathrm{count}(w_i, c_j)\right)^2$$

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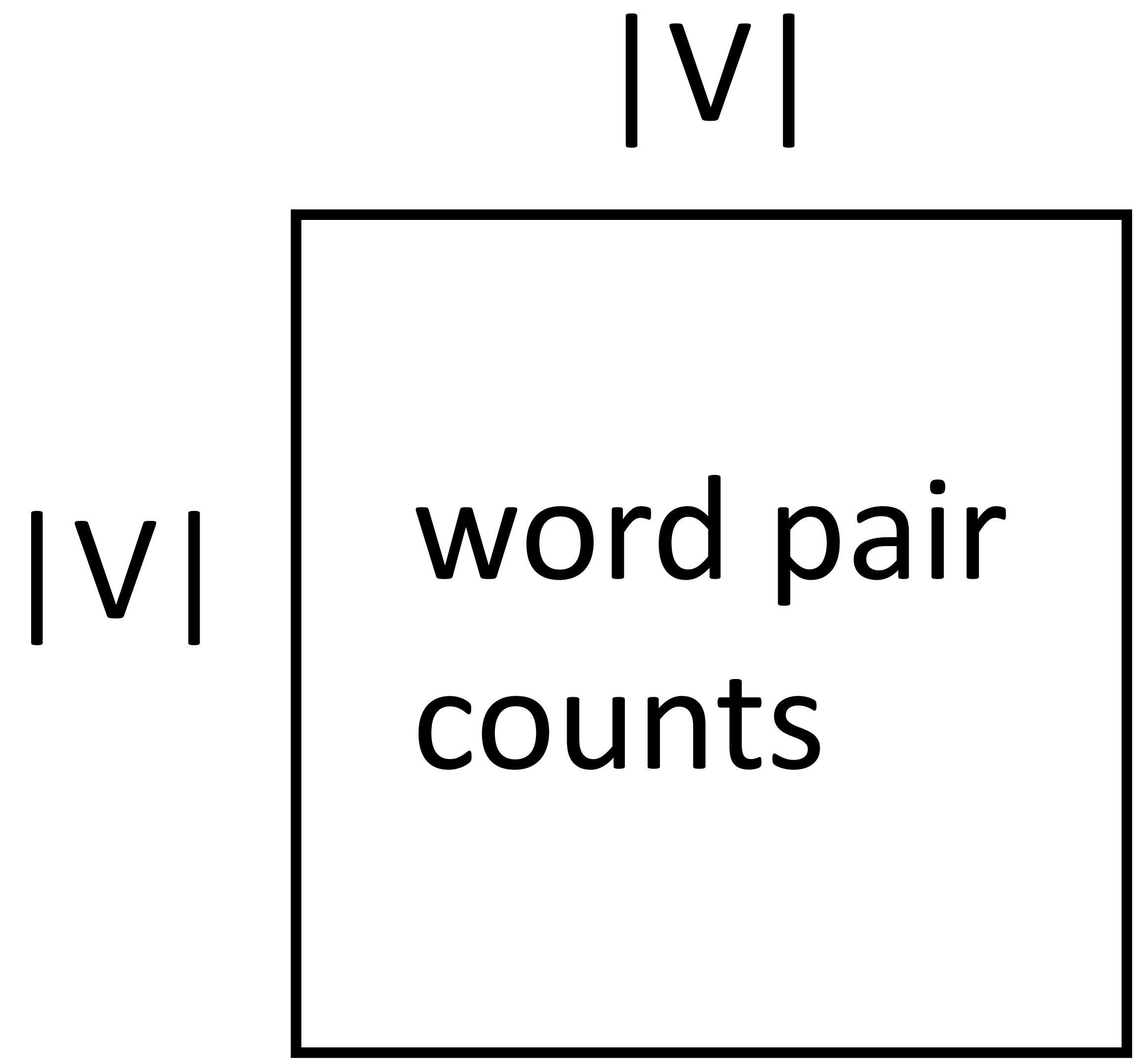

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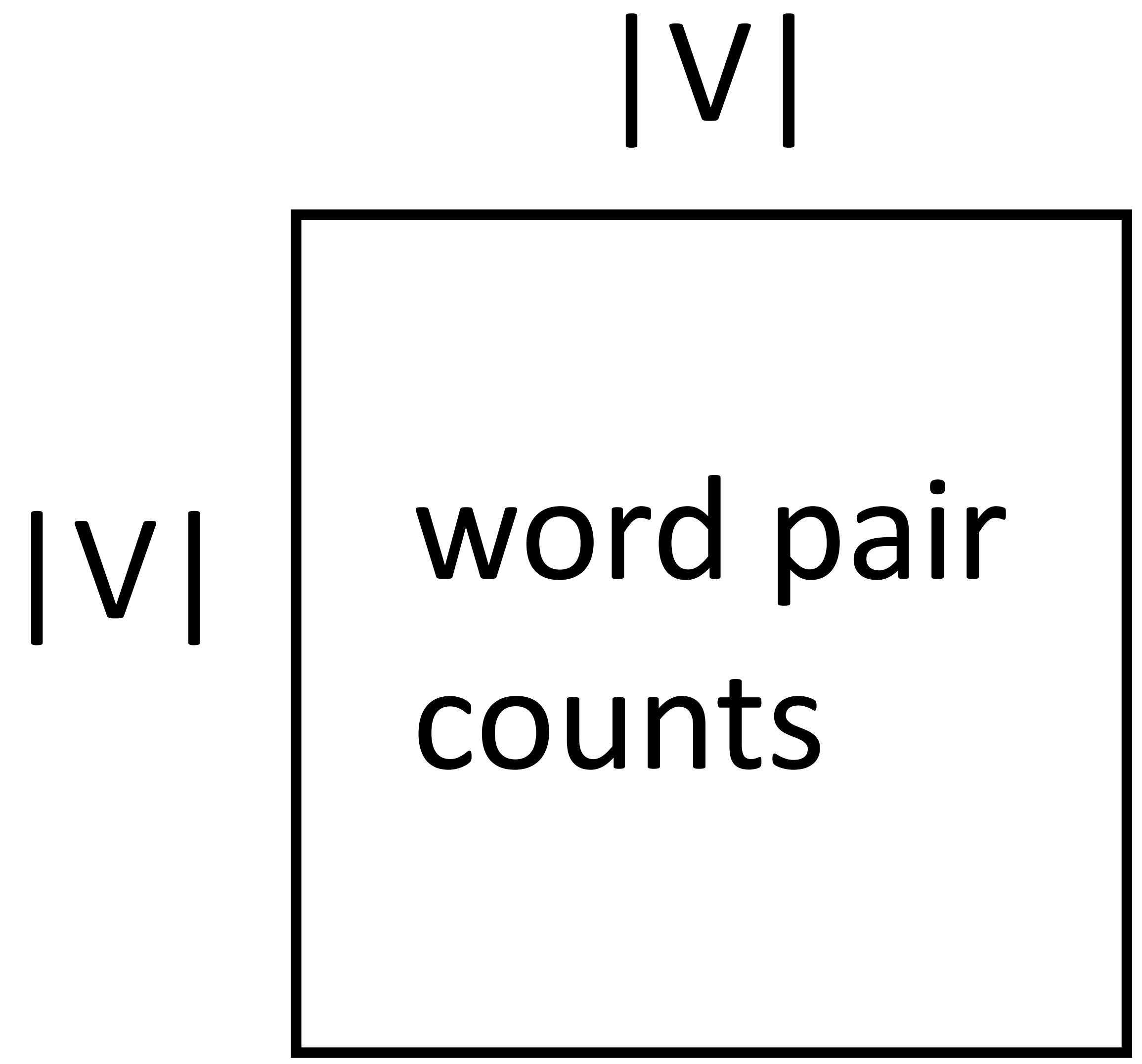

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- Constant in the dataset size (just need counts), quadratic in voc size
- By far the most common (uncontextualized) word vectors used today (20,000+ citations)

Pennington et al. (2014)

Preview: Context-dependent Embeddings

- How to handle different word senses? One vector for *balls*

they dance at balls they hit the balls

Peters et al. (2018)

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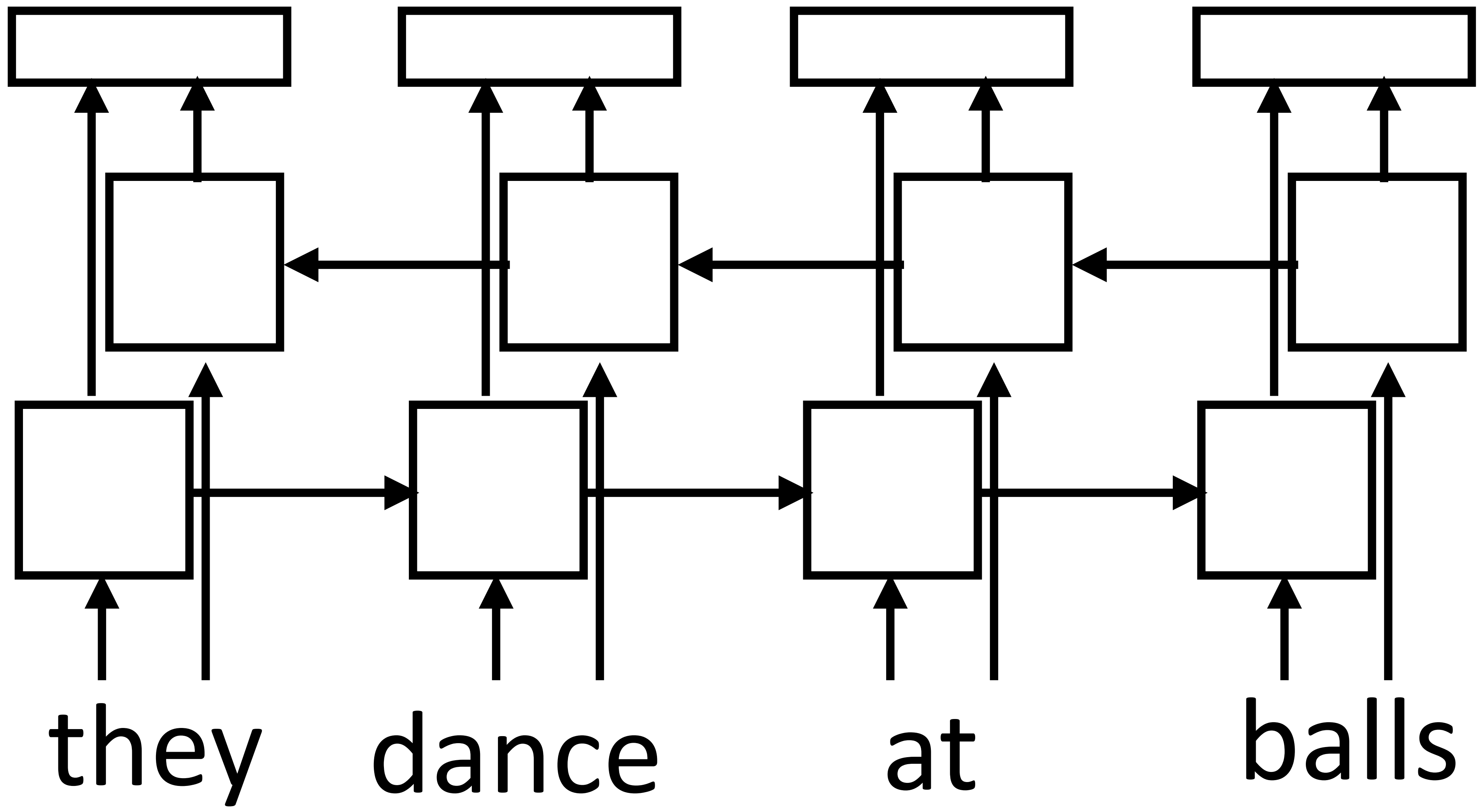

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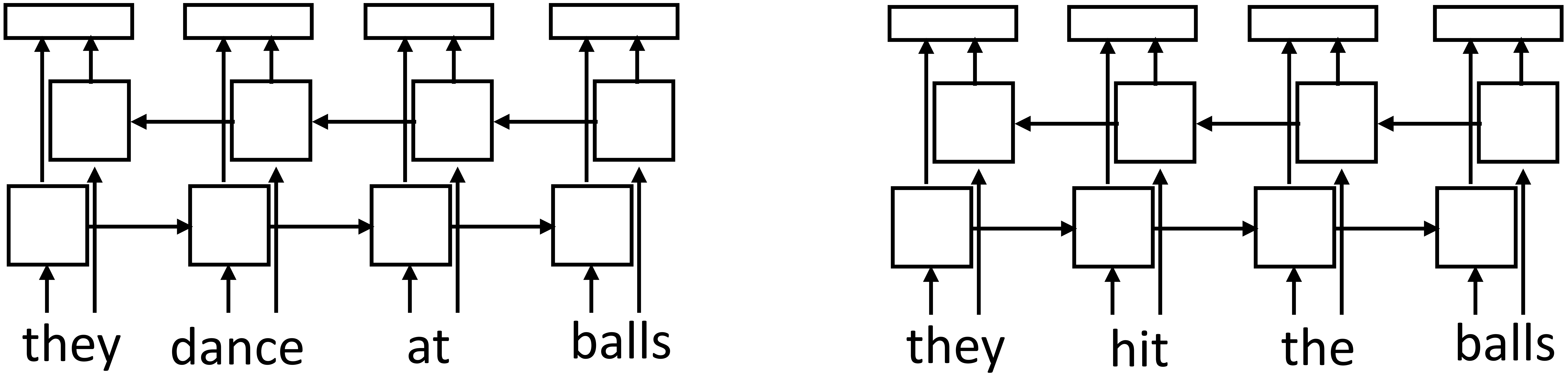

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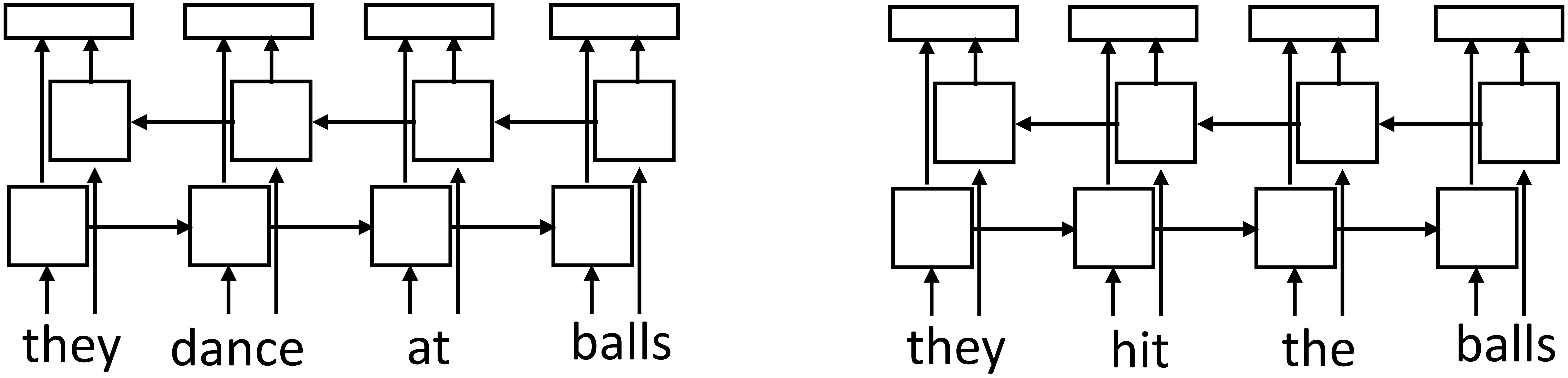

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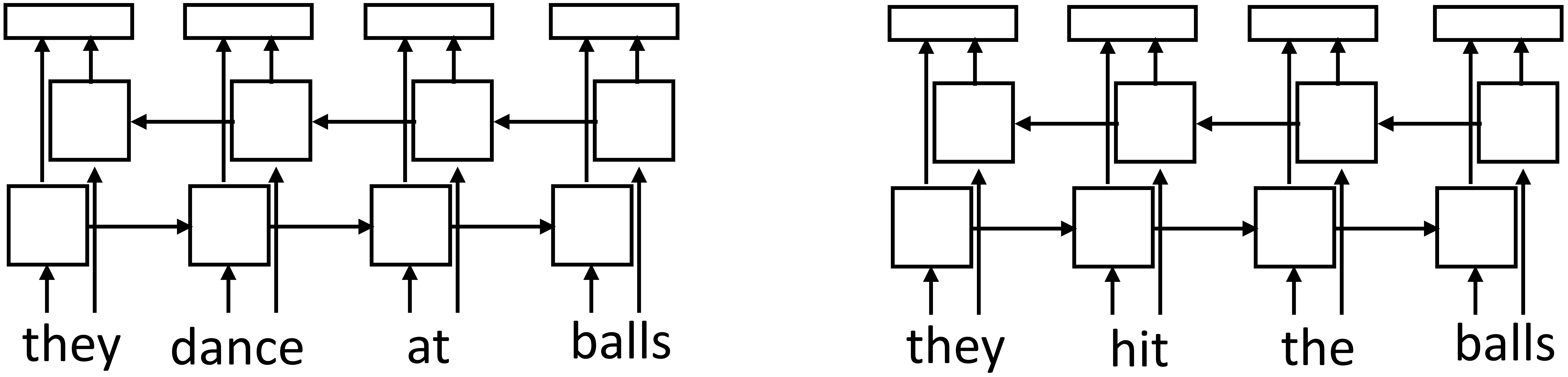

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- *Context-sensitive* word embeddings: depend on rest of the sentence
- *Huge* improvements across nearly all NLP tasks over GloVe

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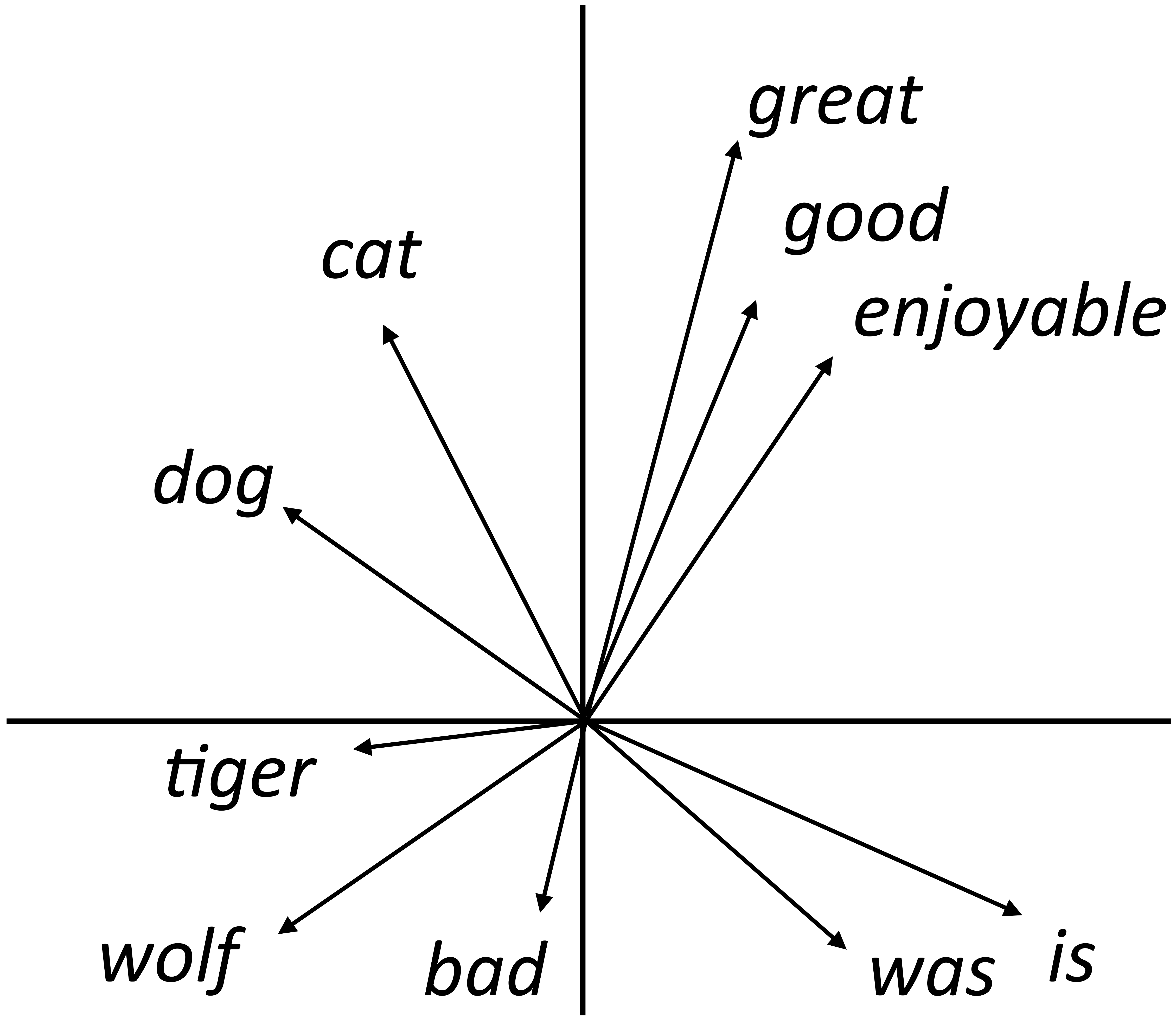
Evaluation

Evaluating Word Embeddings

- What properties of language should word embeddings capture?



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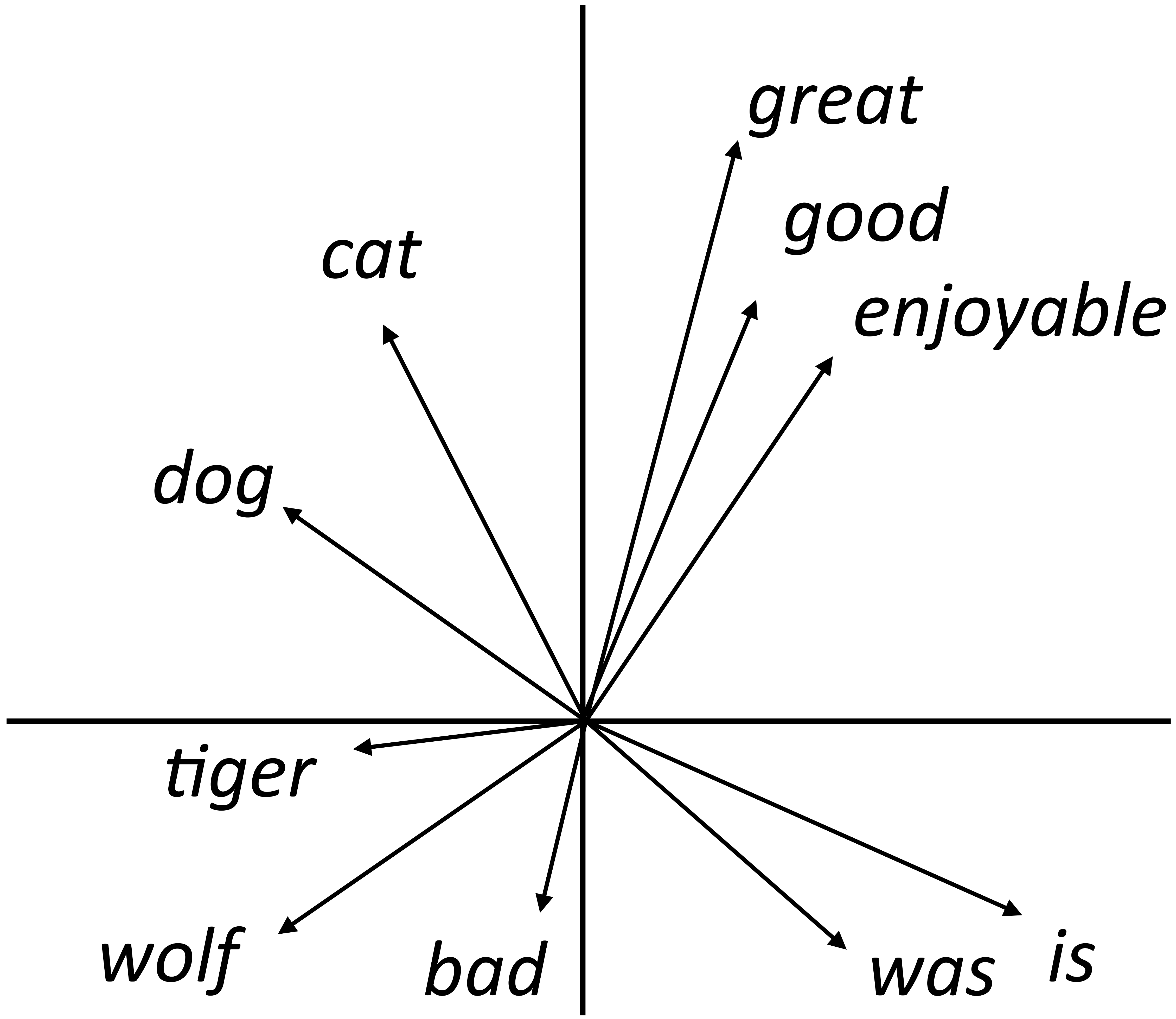

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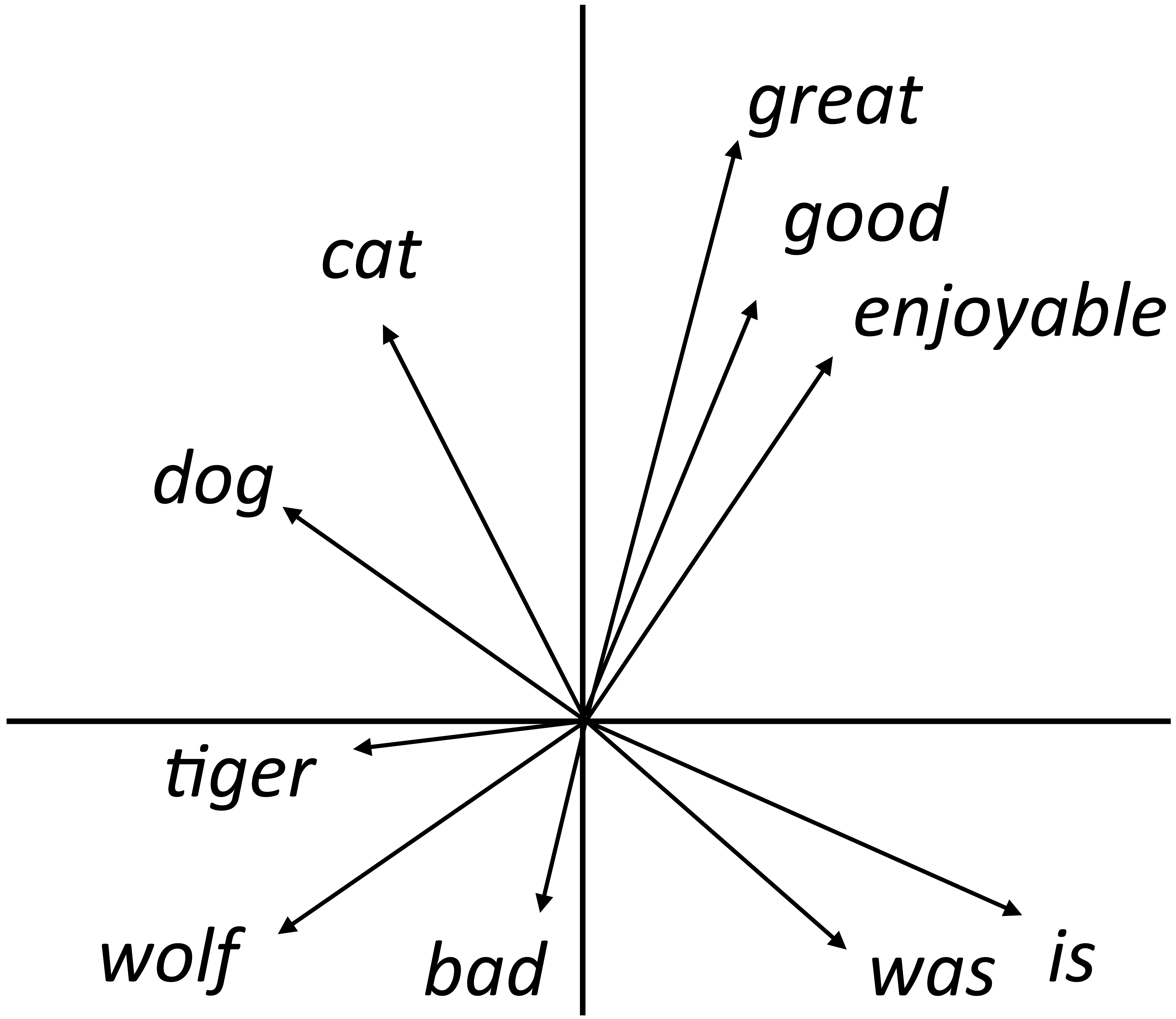

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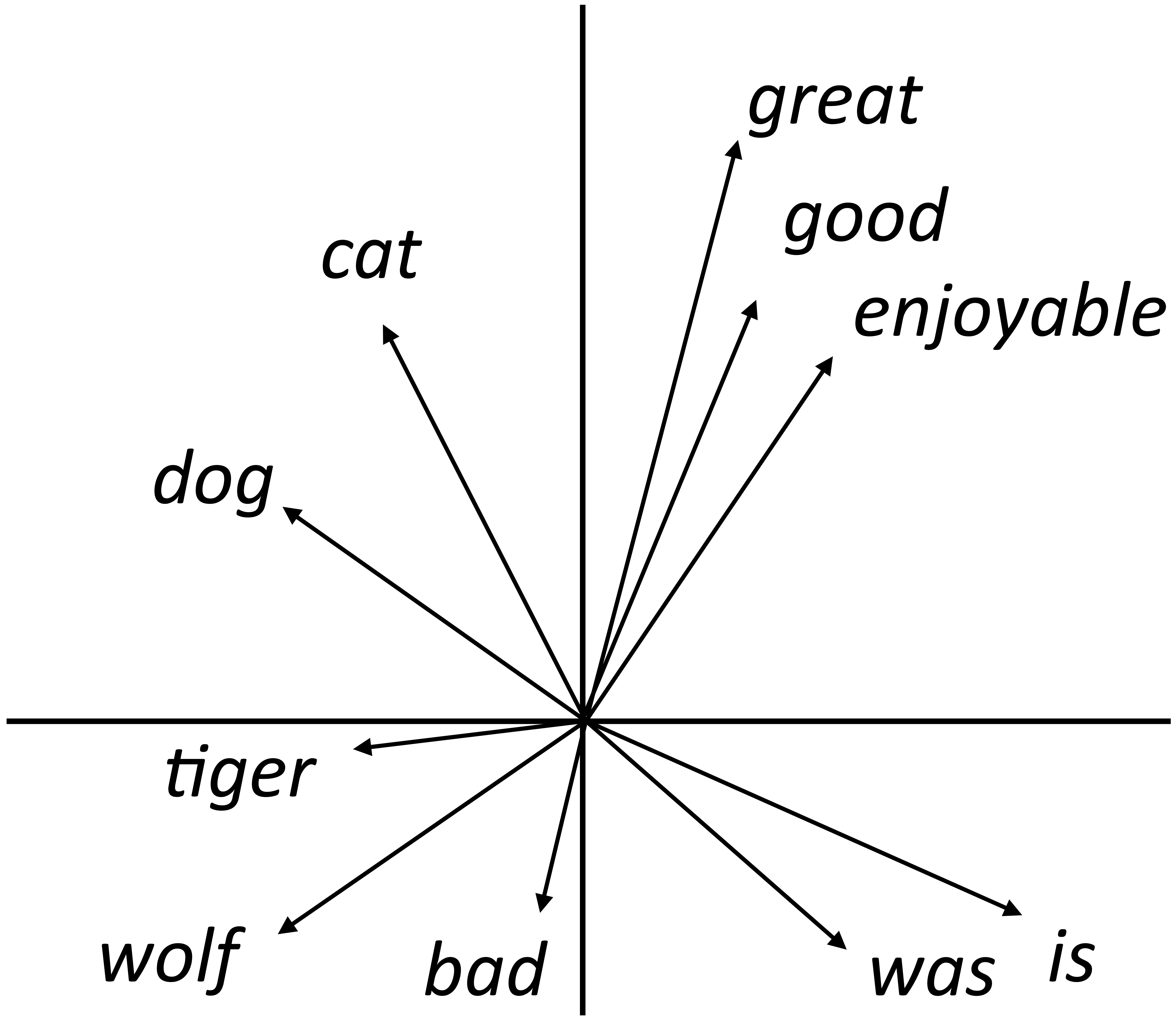

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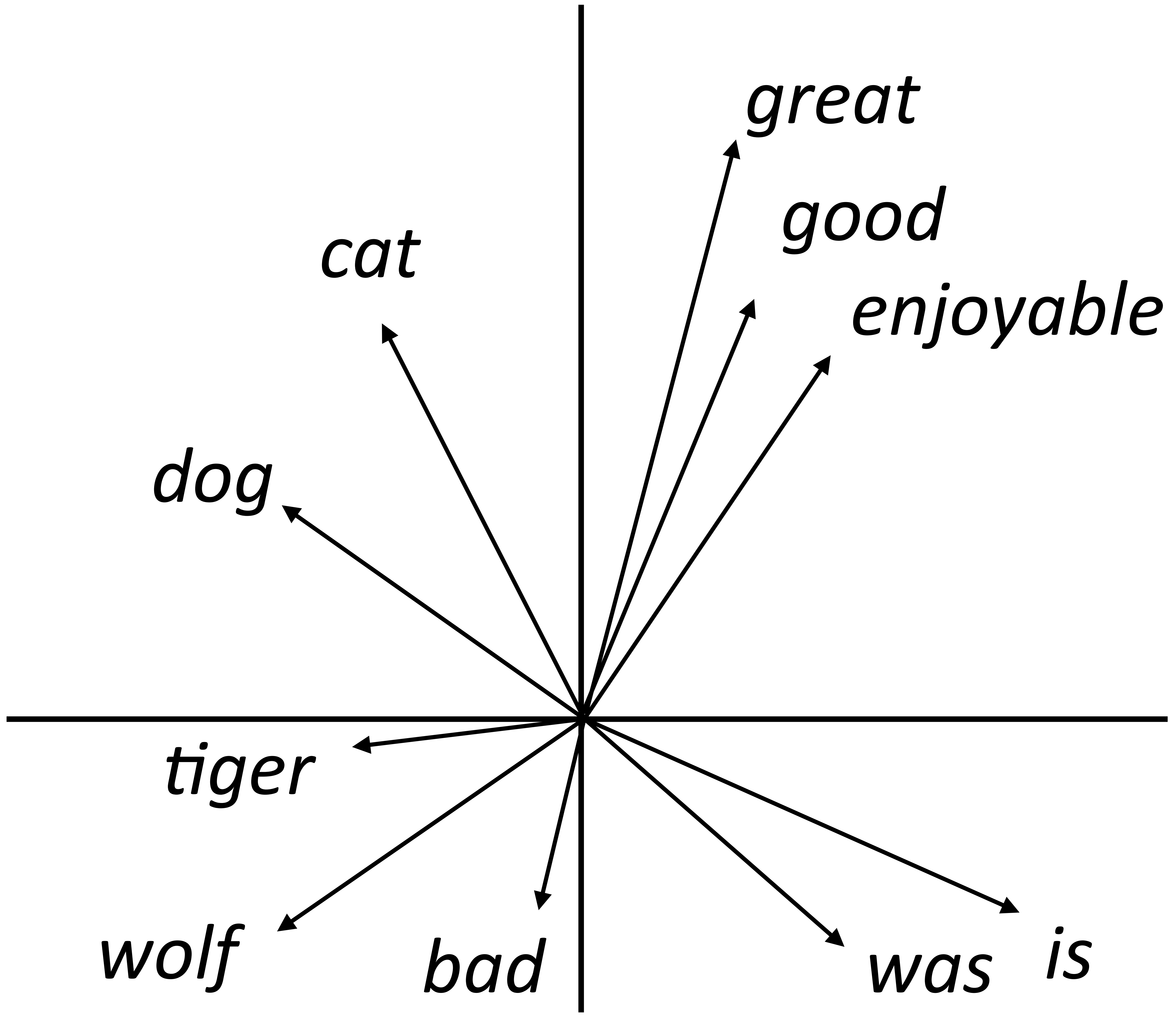

Similarity

Method	WordSim Similarity	WordSim Relatedness	Bruni et al. MEN	Radinsky et al. M. Turk	Luong et al. Rare Words	Hill et al. SimLex
PPMI	.755	**.697**	.745	.686	.462	.393
SVD	**.793**	.691	**.778**	.666	**.514**	.432
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- SVD = singular value decomposition on PMI matrix

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- SVD = singular value decomposition on PMI matrix
- GloVe does not appear to be the best when experiments are carefully controlled, but it depends on hyperparameters + these distinctions don't matter in practice

Levy et al. (2015)

Hypernymy Detection

- Hypernyms: detective *is a* person, dog *is a* animal

Chang et al. (2017)

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Dataset	TM14	Kotlerman 2010	HypeNet	WordNet	**Avg (10 datasets)**
Random	52.0	30.8	24.5	55.2	23.2
Word2Vec + C	52.1	**39.5**	20.7	**63.0**	25.3
GE + C	53.9	36.0	21.6	58.2	26.1
GE + KL	52.0	39.4	23.7	54.4	25.9
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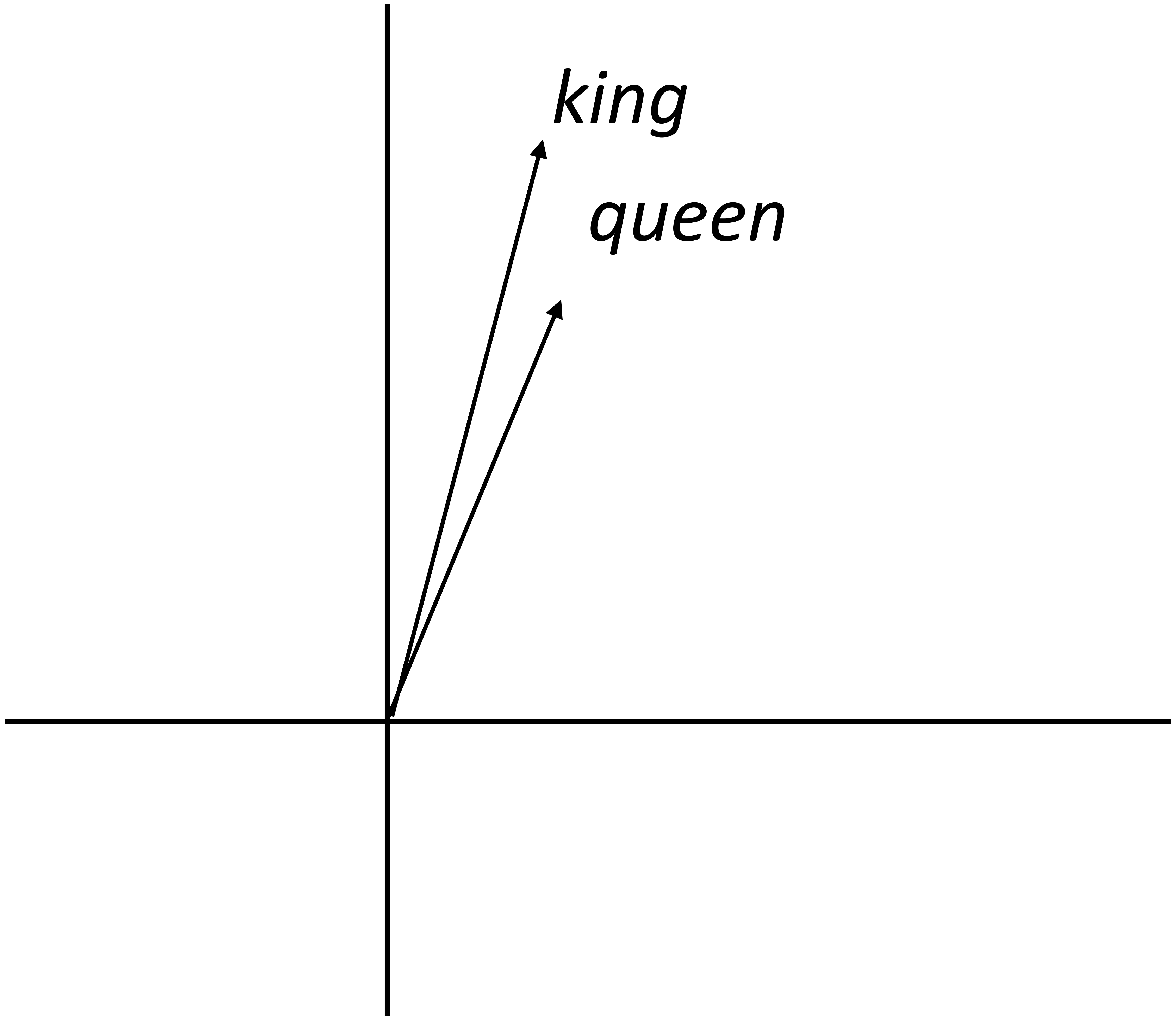
- word2vec (SGNS) works barely better than random guessing here

Chang et al. (2017)

Analogies



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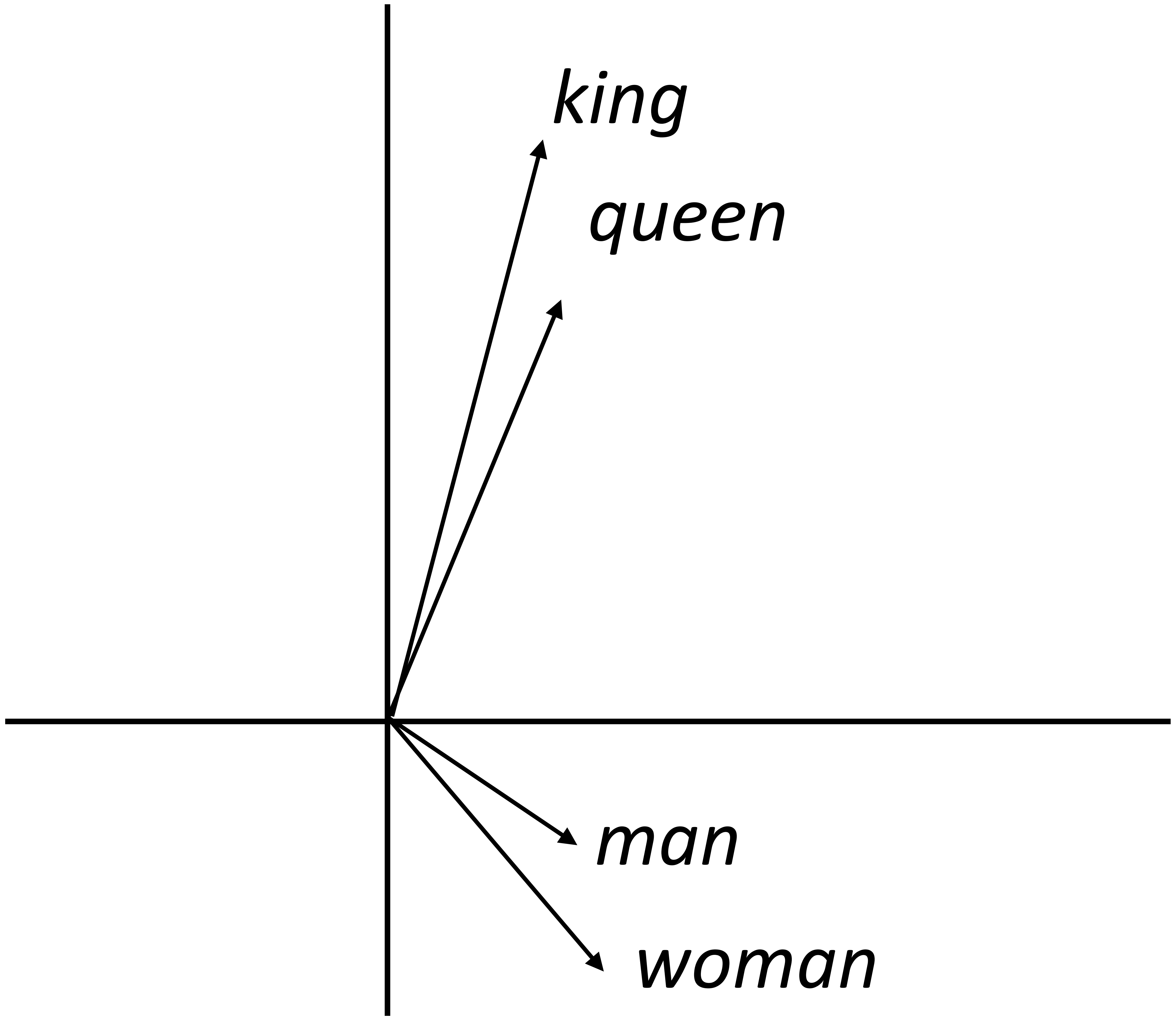
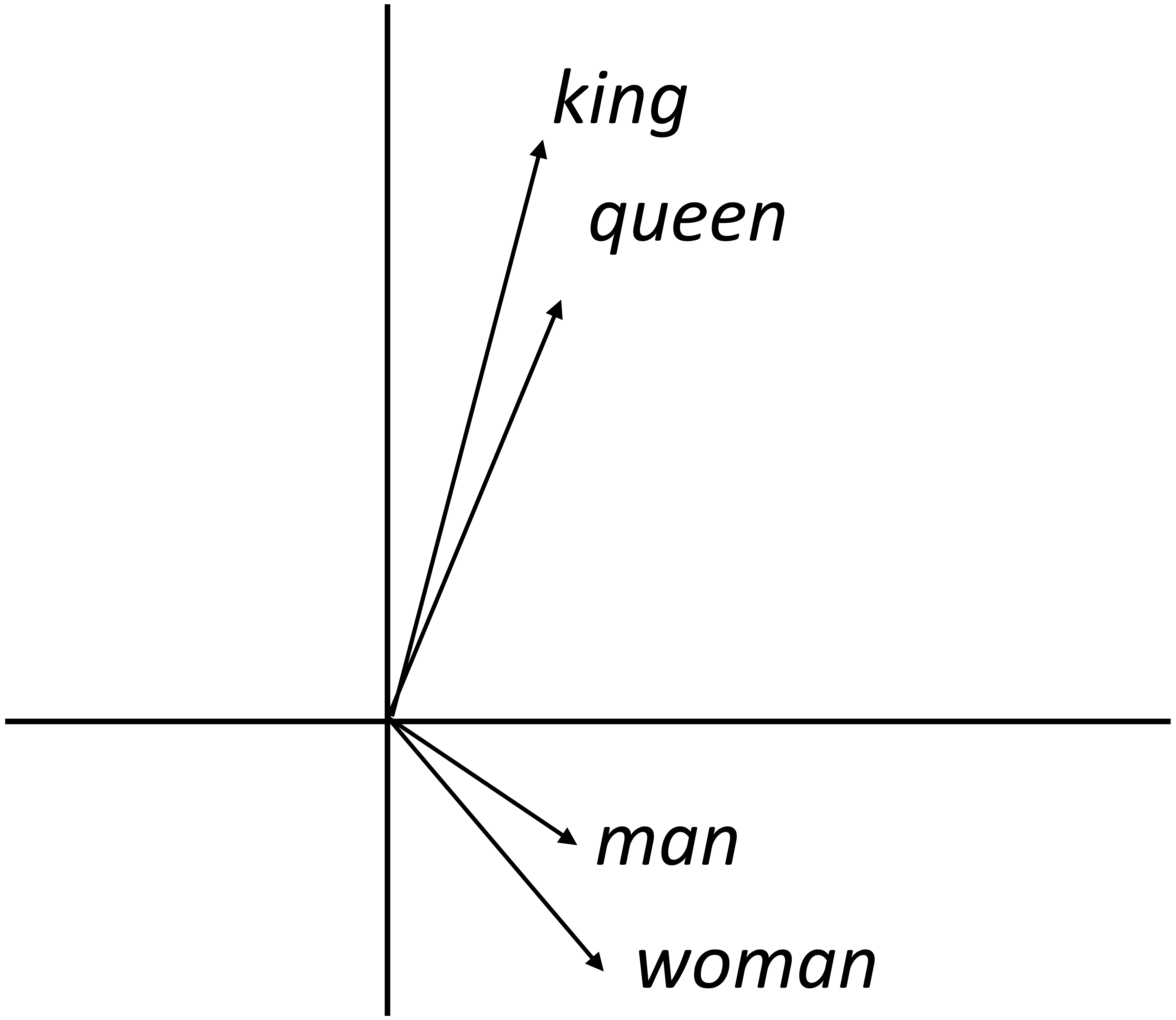


Analogies

(king - man) + woman = queen



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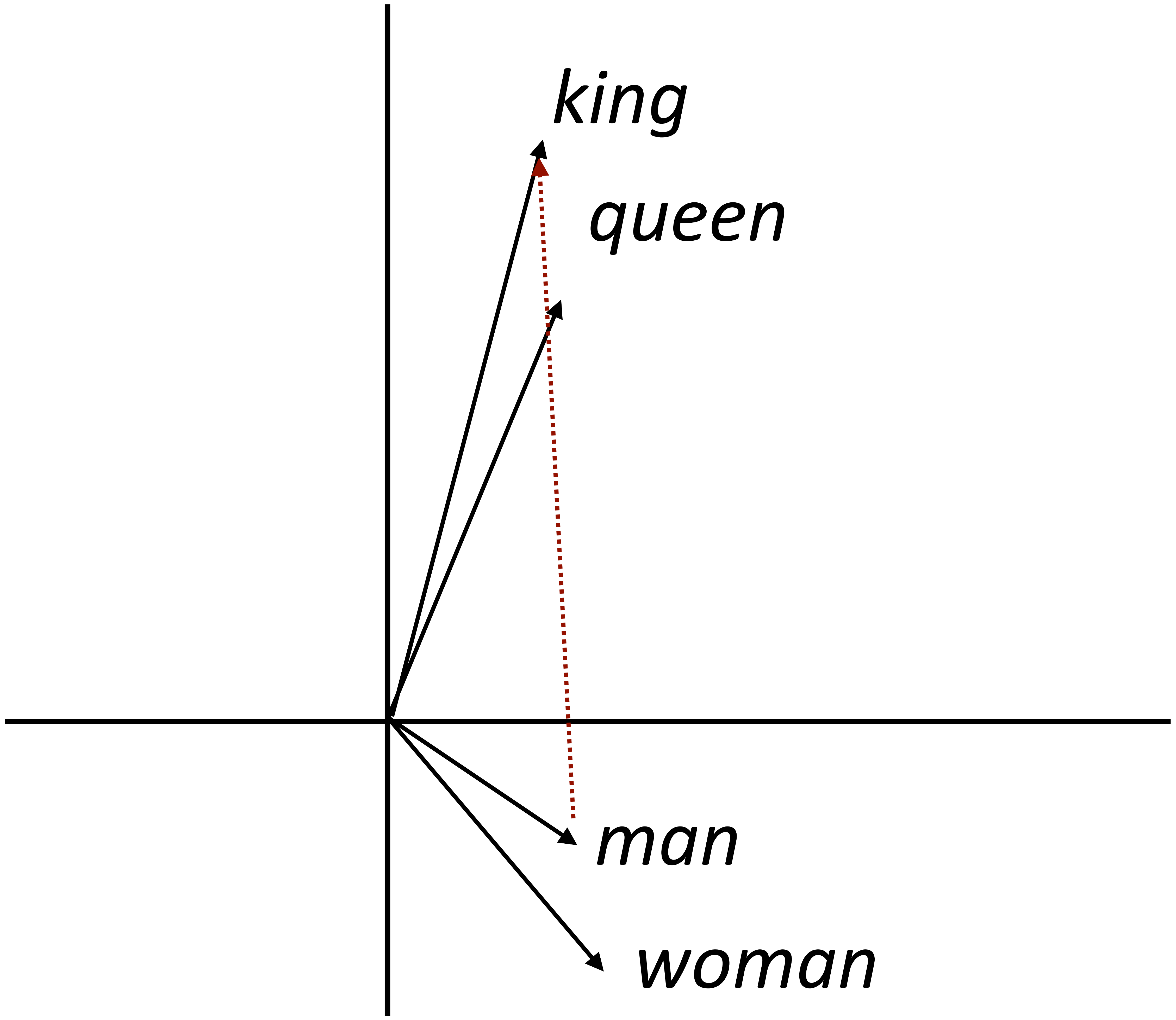

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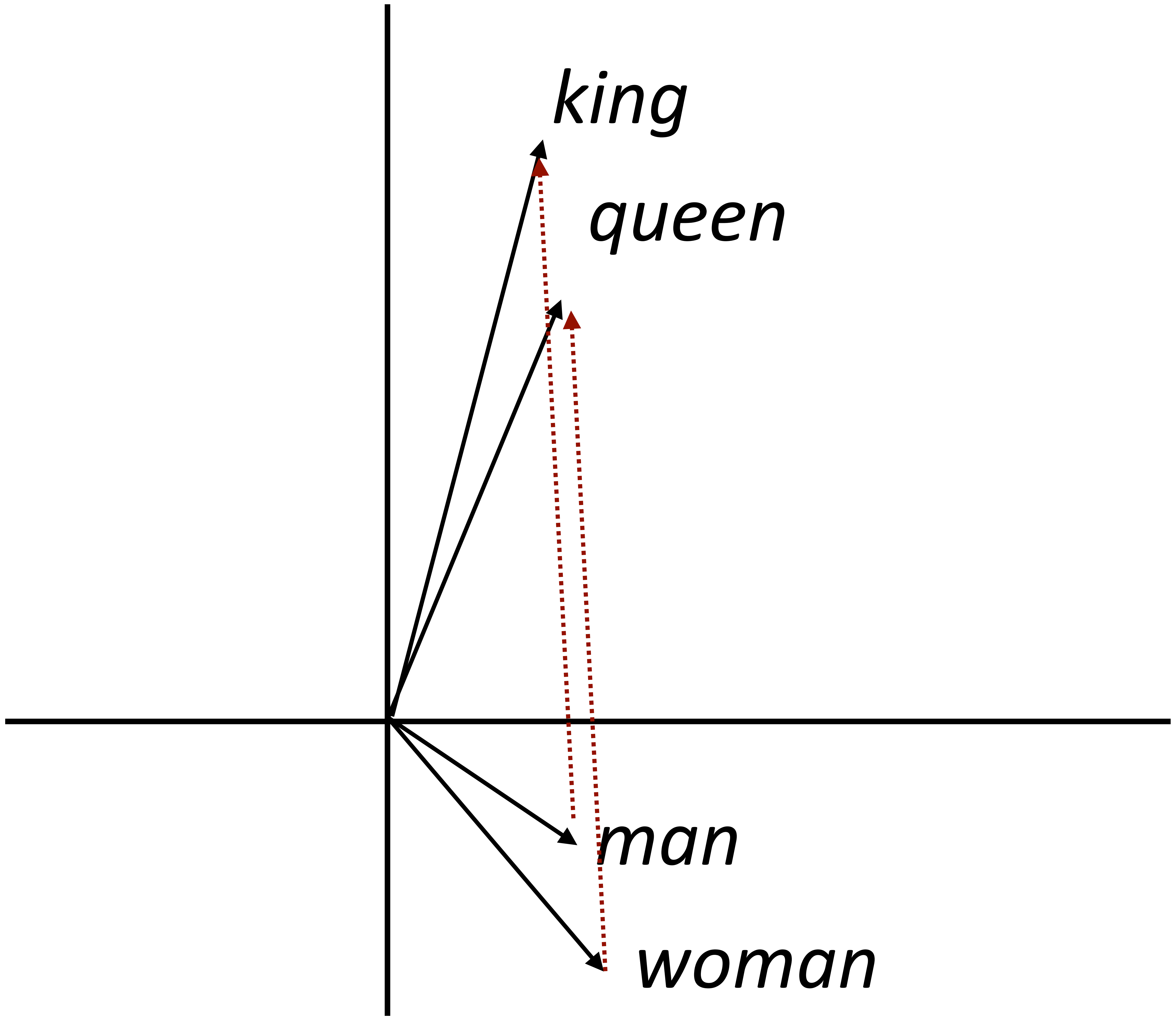

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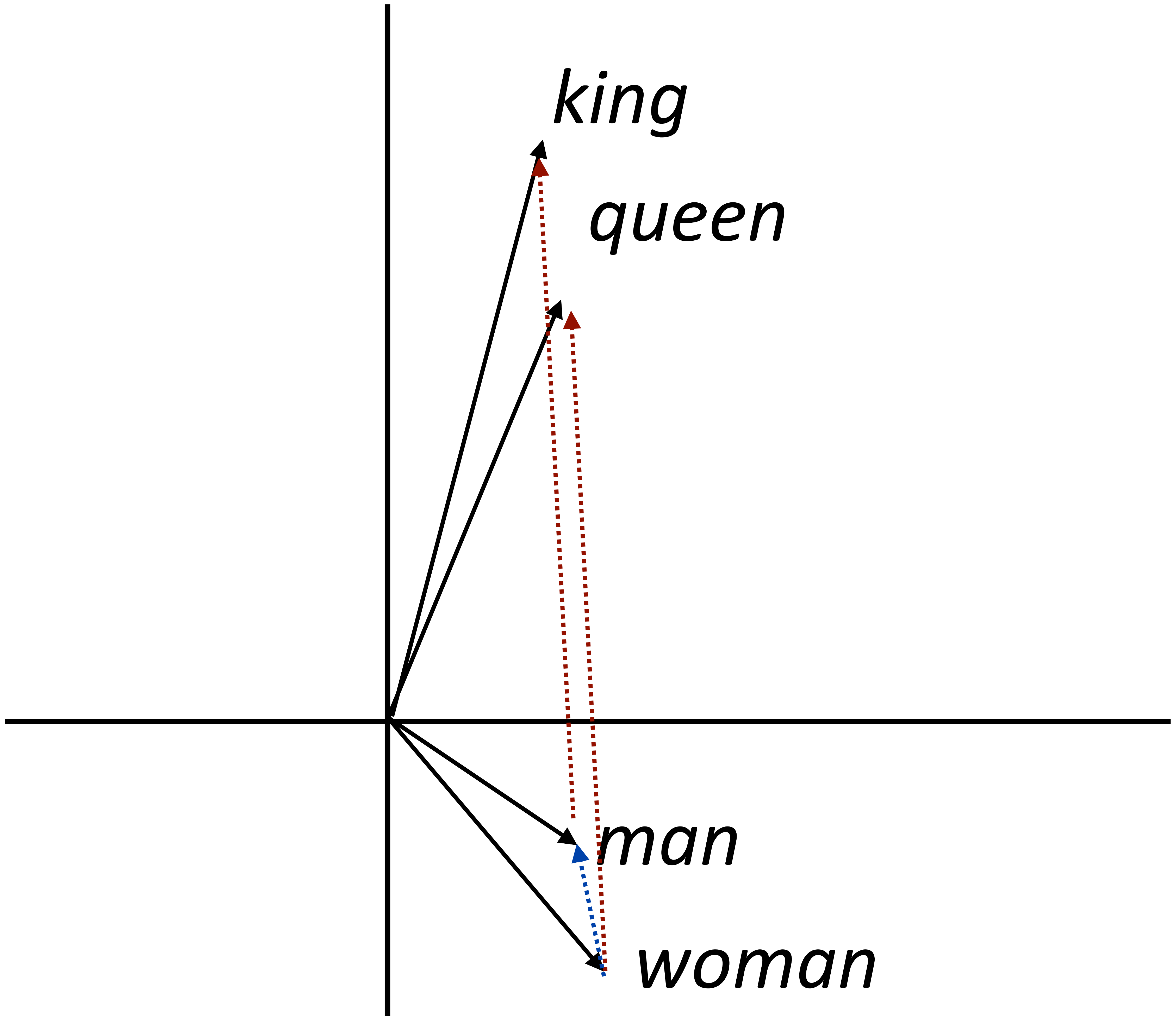

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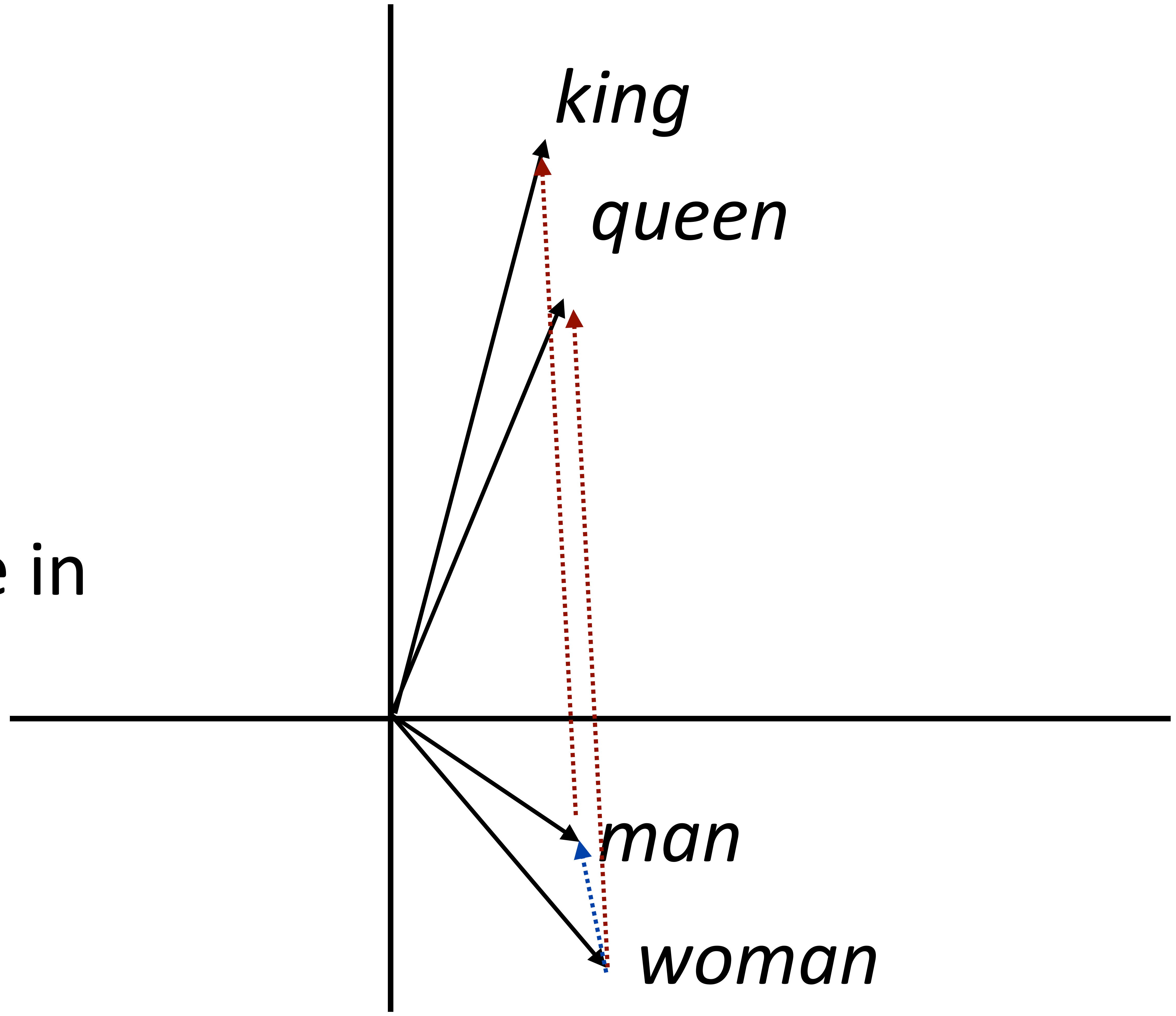

Analogies

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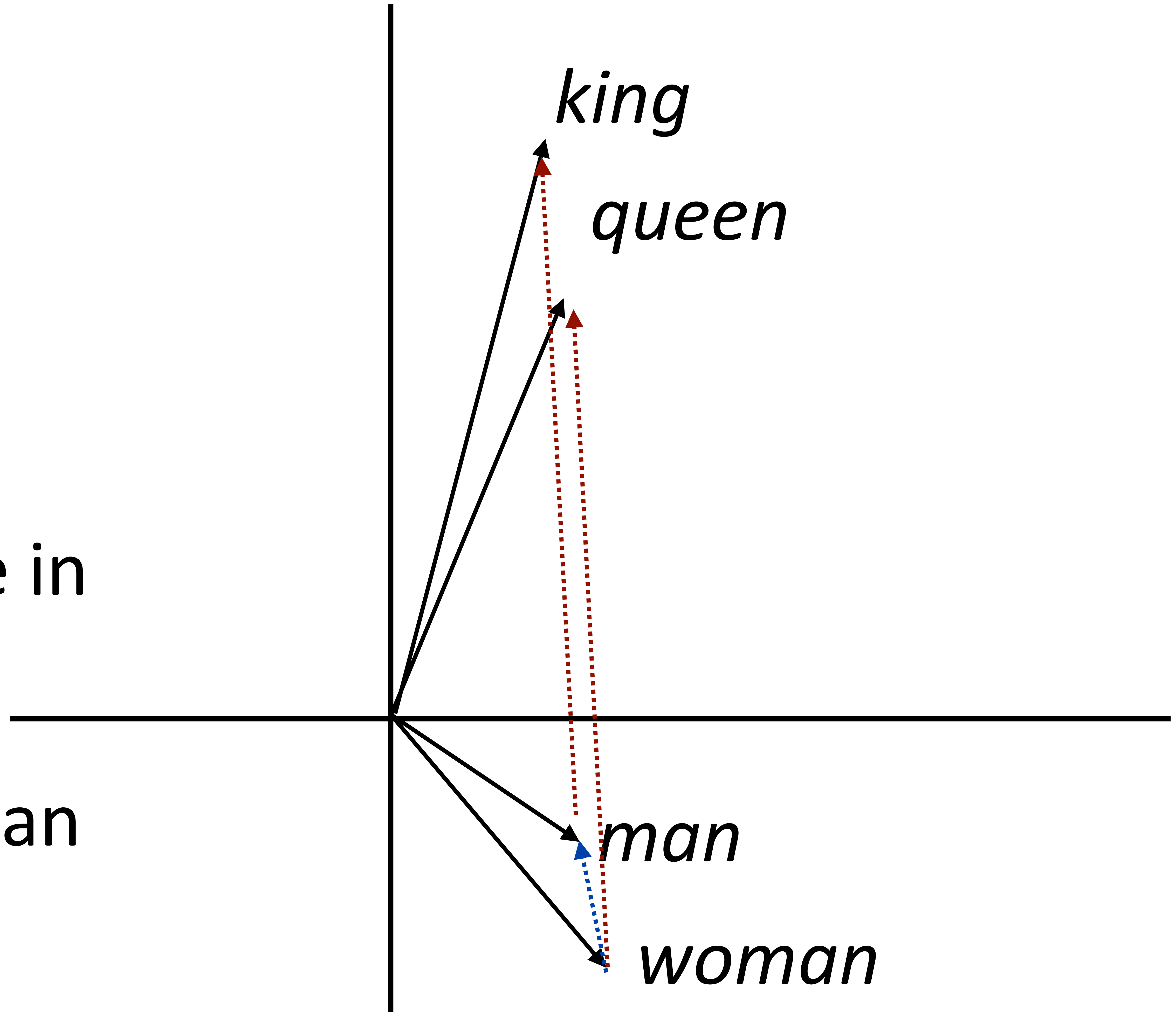
- Why would this be?
- woman - man captures the difference in the contexts that these occur in
- Dominant change: more “he” with man and “she” with woman — similar to difference between king and queen



Analogies

Method	Google Add / Mul	MSR Add / Mul
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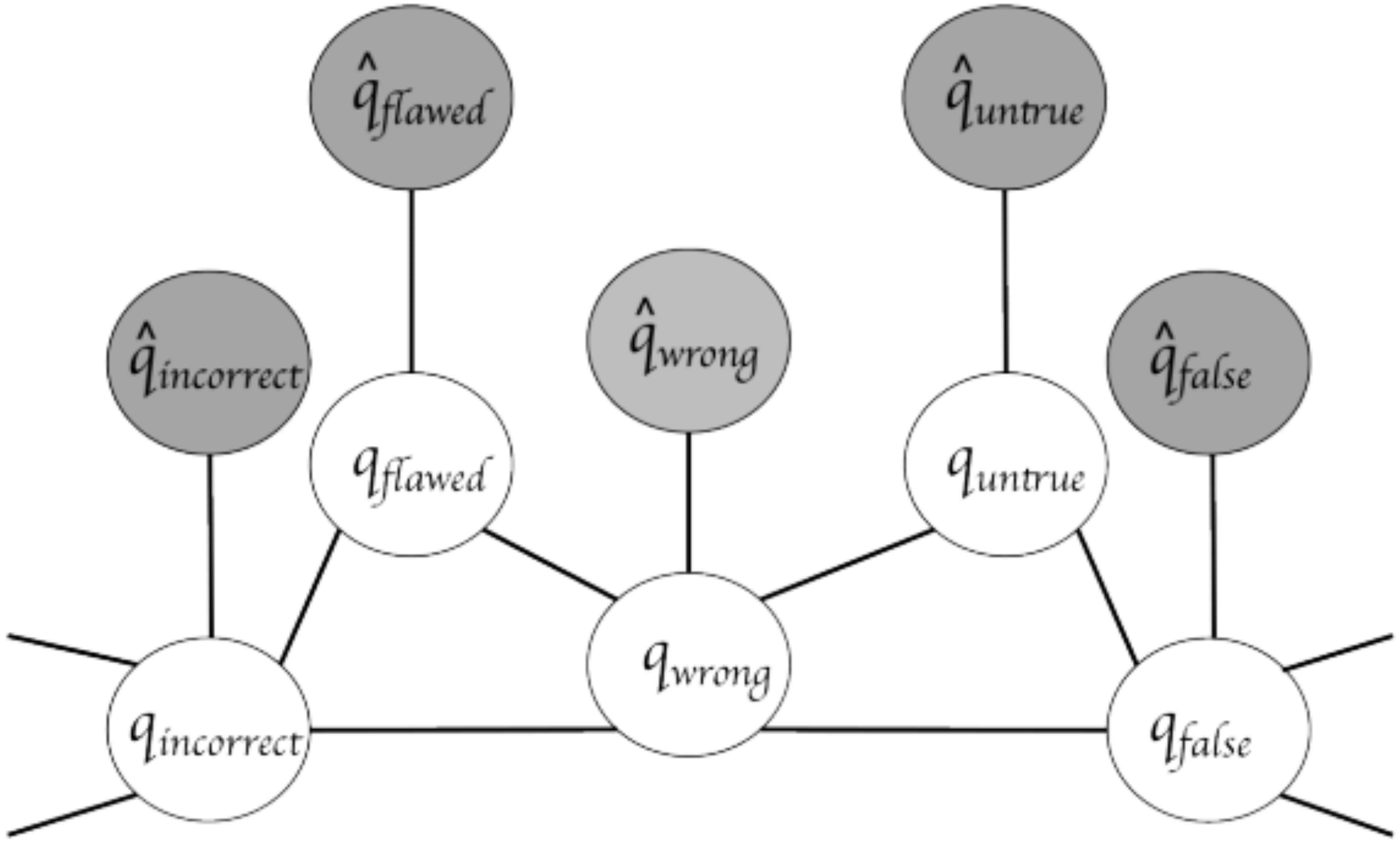
Maximizing for *b*: Add = $\cos(b, a_2 - a_1 + b_1)$ Mul = $\frac{\cos(b_2, a_2)\cos(b_2, b_1)}{\cos(b_2, a_1) + \epsilon}$

Levy et al. (2015)

Using Semantic Knowledge



Faruqui et al. (2015)

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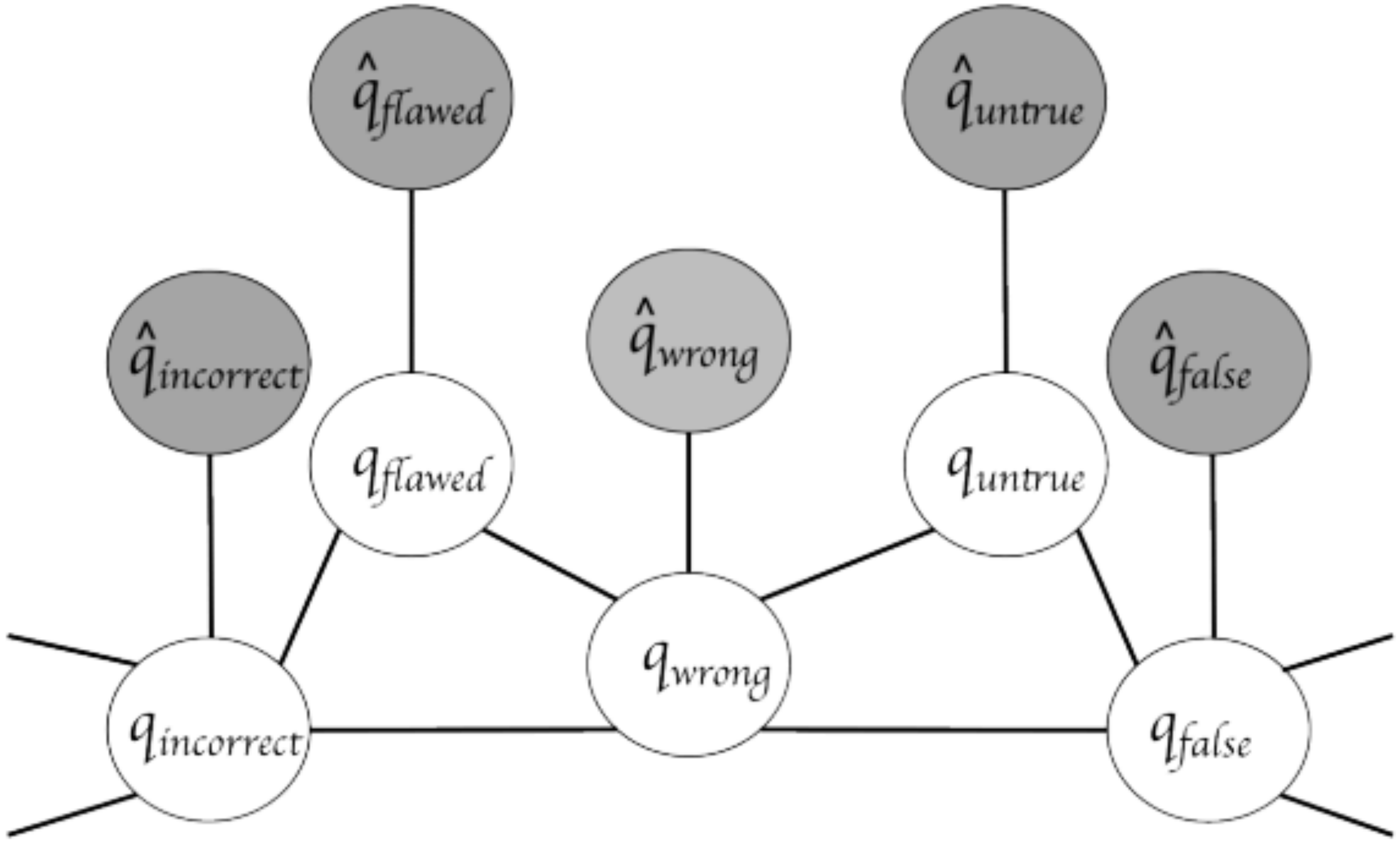

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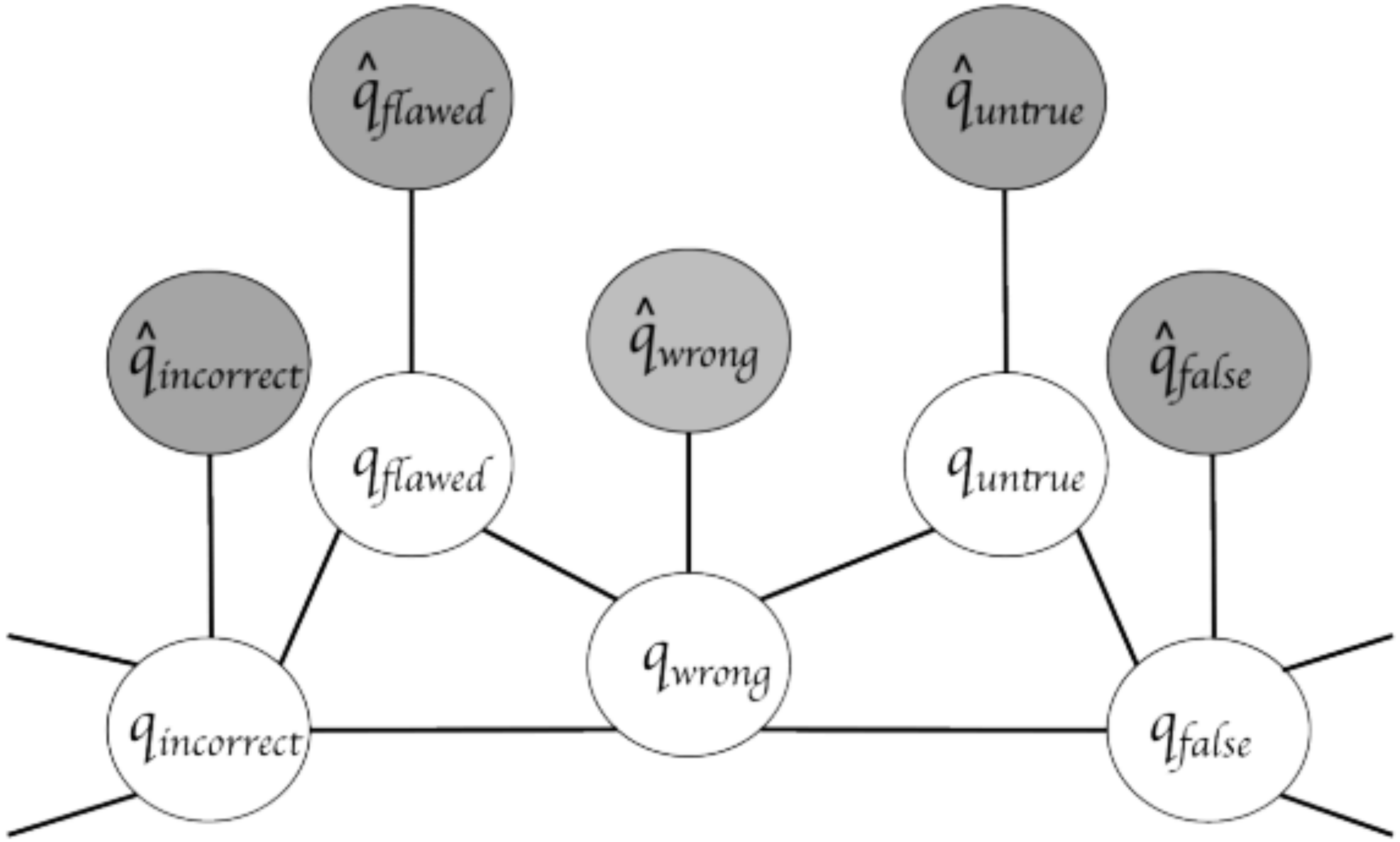

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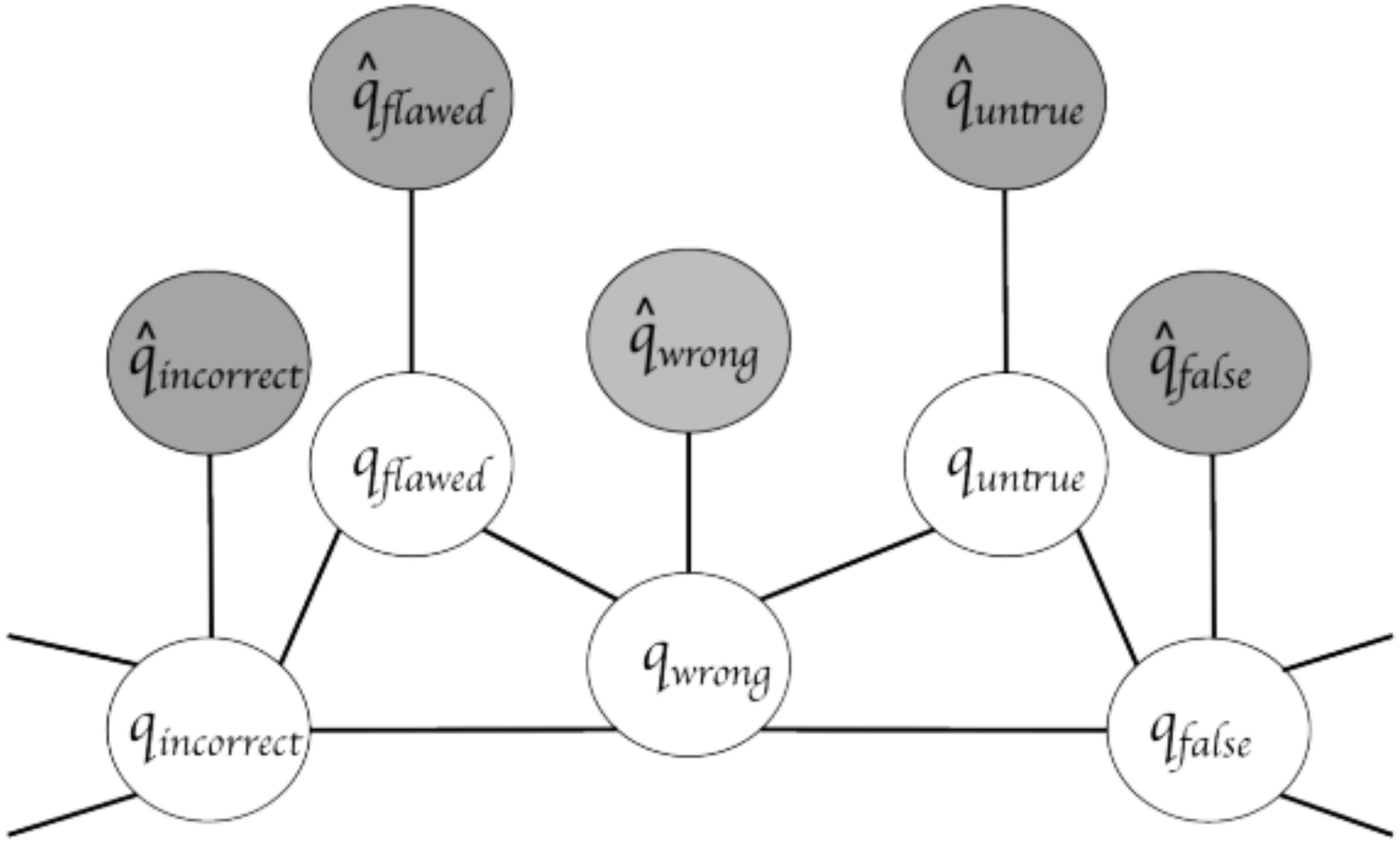

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- Structure derived from a resource like WordNet
- Doesn't help most problems

Faruqui et al. (2015)

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- Approach 3: initialize using GloVe, fine-tune
  - Works best for some tasks, but not used for ELMo

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- Will return to this in a few weeks

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- Next time: RNNs and CNNs